

Memory Organization

Spring 2024

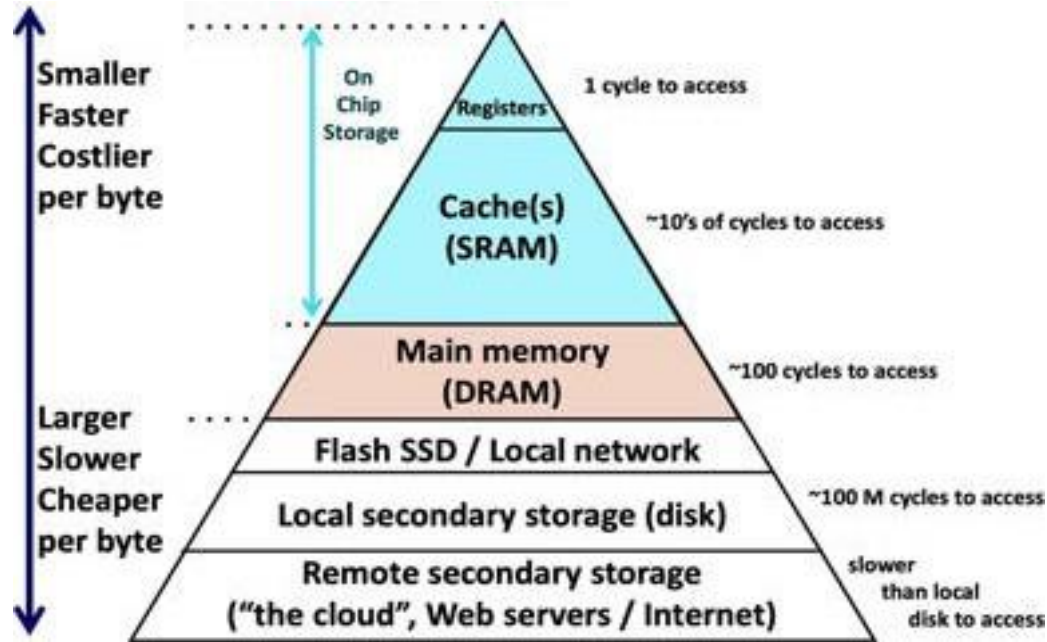
COMP201

Lab 8



**KOÇ
UNIVERSITY**

Recall: Memory Hierarchy



Why do we need Memory Hierarchies?

Some fundamental properties of computer systems

- Fast storage technologies cost more per byte, have less capacity, and require more power (heat!).
- The gap between CPU and main memory speed is widening.
- Locality comes to the rescue!

These fundamental properties of hardware and software suggest an approach for organizing memory and storage systems known as a memory hierarchy.

Fundamental idea of a memory hierarchy

- For each k , the faster, smaller device at level k serves as a cache for the larger, slower device at level $k+1$.
- Because of locality, programs tend to access the data at level k more often than they access the data at level $k+1$.

(Ideal): The memory hierarchy creates a large pool of storage that costs as much as the cheap storage near the bottom, but that serves data to programs at the rate of the fast storage near the top.

Caching in Memory Hierarchy

Cache Type	What is Cached?	Where is it Cached?	Latency (cycles)	Managed By
Registers	4-8 bytes words	CPU core	0	Compiler
TLB	Address translations	On-Chip TLB	0	Hardware MMU
L1 cache	64-byte blocks	On-Chip L1	4	Hardware
L2 cache	64-byte blocks	On-Chip L2	10	Hardware
Virtual Memory	4-KB pages	Main memory	100	Hardware + OS
Buffer cache	Parts of files	Main memory	100	OS
Disk cache	Disk sectors	Disk controller	100,000	Disk firmware
Network buffer cache	Parts of files	Local disk	10,000,000	NFS client
Browser cache	Web pages	Local disk	10,000,000	Web browser
Web cache	Web pages	Remote server disks	1,000,000,000	Web proxy server



Cache Example #1: TIO Breakdown

- Cache Size: 1 MB
- Block Size: 64 Bytes
- 4-way Set-Associative
- 36-bit byte-addressable address space.

Complete the TIO address breakdown:



Cache Example #2: TIO Breakdown

Assume a system with the following properties:

- Cache Size: 16 KB
- Line Size: 32 Bytes
- Direct Mapping

What would be the values of each of the three fields for the following addresses?

Address	Tag	Index	Offset
0x00B248AC			
0x5002AEF3			
0x10203000			
0x0023AF7C			

Cache Example #2: TIO Breakdown

Assume a system with the following properties:

- Cache Size: 16 KB
- Line Size: 32 Bytes
- Direct Mapping

What would be the values of each of the three fields for the following addresses?

Address	Tag	Index	Offset
0x00B248AC	0x2C9	0x45	0xC
0x5002AEF3	0x1400A	0x177	0x13
0x10203000	0x4080	0x180	0x0
0x0023AF7C	0x8E	0x17B	0x1C

Cache Simulator

- Simulates usage of Cache
- Step-by-step explanation
- Adjustable system parameters
- Cache hits, misses, counts and history
- Physical Memory and Cache Memory can be visualized

The screenshot displays the Cache Simulator interface, which is divided into several sections:

- System Parameters:** Includes controls for Address width (4 bits), Cache size (16 bytes), Block size (4 bytes), Associativity (4-way), Write Hit (Write back), Write Miss (Write-allocate), Replacement (Least Recently Used), and buttons for Reset System and Explain.
- Manual Memory Access:** Features Read and Write buttons with address and byte size inputs, an Explain checkbox, and a Flush button.
- History:** A text area for recording simulation events, with a Load button.
- Simulation Messages:** A text area for displaying system-generated messages.
- Cache and Memory Visualization:** Shows the state of the cache and physical memory. The cache is a 4x4 array with 4 sets (Set 0, 1, 2, 3) and 4 ways. The physical memory is a 16x4 array of hex values.

Cache State:

Set	Way 0	Way 1	Way 2	Way 3
Set 0	000	0	00	0
Set 1	0	0	0	0
Set 2	0	0	0	0
Set 3	0	0	0	0

Physical Memory State:

Address	Hex Value
0x00	20 f6 ef ea a2 5e 9f 1a
0x08	a2 d0 4f c4 a0 0c f7 27
0x10	b8 bd 1a ca 35 95 cb 80
0x18	84 3f 02 4f 8e f3 f6 e5
0x20	cd 4a f6 48 1a 6f 7e 63
0x28	e9 36 ae 32 0d 37 bc c9
0x30	93 dc b8 7a 3b 1a b2 0c
0x38	d3 a6 a4 71 e2 23 9c 59

System Parameters:

Address width: 6 bits

Cache size: 16 bytes

Block size: 2 4 8 bytes

Associativity: 1 2 4 way(s)

Write Hit: Write back

Write Miss: Write-allocate

Replacement: Least Recently Used

Explain

Manual Memory Access:

Addr: 0x23

Explain Addr: 0x Byte: 0x

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	11	0	0

Simulation Messages:

Read: 0x23
Split address into TIO breakdown.

History:

> R(0x23) = 3

m = 6, C = 16

K = 4, E = 2

Write back

Write-allocate

Eviction: LRU

VDT Cache Data

Set 0	00	---	---	---	---	2
	00	---	---	---	---	1
Set 1	00	---	---	---	---	2
	00	---	---	---	---	3

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x08	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x18	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x28	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x38	d3	a6	a4	71	e2	23	9c	59

System Parameters:

Address width: bits

Cache size: bytes

Block size: 2 4 8 bytes

Associativity: 1 2 4 way(s)

Write Hit:

Write Miss:

Replacement:

Explain

Manual Memory Access:

Addr: 0x23

Explain Addr: 0x, Byte: 0x

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	11	0	1

Simulation Messages:

```
Checking Set 0
Looking for Tag 4... MISS!
Invalid line 0 chosen for replacement.
```

History:

```
> R(0x23) = M
```

m = 6, C = 16

K = 4, E = 2

Write back

Write-allocate

Eviction: LRU

V D T Cache Data

Set 0	0	0	-	-	-	-	-	2
	0	0	-	-	-	-	-	1
Set 1	0	0	-	-	-	-	-	2
	0	0	-	-	-	-	-	1

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x08	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x18	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x28	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x38	d3	a6	a4	71	e2	23	9c	59

System Parameters:

Address width: bits

Cache size: bytes

Block size: 2 4 8 bytes

Associativity: 1 2 4 way(s)

Write Hit:

Write Miss:

Replacement:

Explain

Manual Memory Access:

Addr: 0x23

Explain Addr: 0x , Byte: 0x

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	11	0	1

Simulation Messages:

Invalid line 0 chosen for replacement.
Block read into cache from memory at address 0x20.

History:

```
> R(0x23) = R
```

m = 6, C = 16
K = 4, E = 2
Write back
Write-allocate
Eviction: LRU

V D T Cache Data

Set	0	1	2	3	4	5	6
Set 0	1	0	4	cd	4a	f6	48
	0	0	-	-	-	-	-
Set 1	0	0	-	-	-	-	-
	0	0	-	-	-	-	-

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x08	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x18	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x28	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x38	d3	a6	a4	71	e2	23	9c	59

System Parameters:

Address width: bits

Cache size: bytes

Block size: 2 4 8 bytes

Associativity: 1 2 4 way(s)

Write Hit:

Write Miss:

Replacement:

Explain

Manual Memory Access:

Addr:

Explain Addr: Byte:

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	11	0	1

Simulation Messages:

```
0x20.
LRU statuses updated.
Data: 0x48
```

History:

```
R(0x23) = H.
>
```

m = 6, C = 16
 K = 4, E = 2
 Write back
 Write-allocate
 Eviction: LRU

V D T Cache Data

Set 0	1	0	4	cd	4a	f6	48	1
		0	0	-	-	-	-	2
		0	0	-	-	-	-	2
Set 1	0	0	-	-	-	-	-	1

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x05	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x15	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x25	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x35	d3	a6	a4	71	e2	23	9c	59

Cache Simulator: Writing 0x13 at 0x22

System Parameters:

Address width: 6 bits
Cache size: 16 bytes
Block size: 2 4 8 bytes
Associativity: 1 2 4 way(s)
Write Hit: Write back
Write Miss: Write-allocate
Replacement: Least Recently Used

Explain

Manual Memory Access:

Addr: 0x23
 Explain Addr: 0x22, Byte: 0x13

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	11	0	1

Simulation Messages:

Write: 0x13 at address 0x22

History:

```
R(0x23) = H  
> W(0x22, 0x13) = ?
```

m = 6, C = 16
K = 4, E = 2
Write back
Write-allocate
Eviction: LRU

VDT Cache Data

Set	0	1	2	3	4	5	6
Set 0	104	cd	4a	f6	48		
	00	-	-	-	-	-	-
Set 1	00	-	-	-	-	-	-
	00	-	-	-	-	-	-

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x08	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x18	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x28	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x38	d3	a6	a4	71	e2	23	9c	59

System Parameters:

Address width: bits

Cache size: bytes

Block size: 2 4 8 bytes

Associativity: 1 2 4 way(s)

Write Hit:

Write Miss:

Replacement:

Explain

Manual Memory Access:

Addr:

Explain Addr: , Byte:

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	10	0	1

Simulation Messages:

Writer: 0x13 at address 0x22
Split address into TIO breakdown.

History:

```
R(0x23) = M
> M(0x22, 0x13) = ?
```

m = 6, C = 16

K = 4, E = 2

Write back

Write-allocate

Eviction: LRU

V D T Cache Data

Set	0	1	2	3	4	5	6
Set 0	1	0	4	cd	4a	f6	48
	0	0	-	-	-	-	-
Set 1	0	0	-	-	-	-	-
	0	0	-	-	-	-	-

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x08	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x18	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x28	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x38	d3	a6	a4	71	e2	23	9c	59

System Parameters:

Address width: bits

Cache size: bytes

Block size: 2 4 8 bytes

Associativity: 1 2 4 way(s)

Write Hit:

Write Miss:

Replacement:

Explain

Manual Memory Access:

Addr: 0x23

Explain Addr: 0x22, Byte: 0x13

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	10	1	1

Simulation Messages:

```
Split address into T10 breakdown.
Checking Set 0
Looking for Tag 4... HIT in Line 0!
```

History:

```
R(0x23) = H
> M(0x22, 0x13) = H
```

m = 6, C = 16

K = 4, E = 2

Write back

Write-allocate

Eviction: LRU

VDT Cache Data

Set 0	→	1	0	4	cd	4a	f6	48	:0
		0	0	--	--	--	--	--	:1
		0	0	--	--	--	--	--	:2
Set 1		0	0	--	--	--	--	--	:3
		0	0	--	--	--	--	--	:4

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x08	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x18	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x28	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x38	d3	a6	a4	71	e2	23	9c	59

System Parameters:

Address width: bits

Cache size: bytes

Block size: 2 4 8 bytes

Associativity: 1 2 4 way(s)

Write Hit:

Write Miss:

Replacement:

Explain

Manual Memory Access:

Addr:

Explain Addr: Byte:

Tag	Index	Offset	Cache Hits	Cache Misses
100	0	10	1	1

Simulation Messages:

```
Checking Set 0
Looking for Tag 4... HIT in Line 0!
LRU statuses updated.
Write back! set Dirty bit.
```

History:

```
R(0x23) = H
W(0x22, 0x13) = H
```

m = 6, C = 16

K = 4, E = 2

Write back

Write-allocate

Eviction: LRU

V D T Cache Data

Set	0	1	2	3	4	5
Set 0	1	1	4	cd	4a	13 48
	0	0	--	--	--	--
Set 1	0	0	--	--	--	--
	0	0	--	--	--	--

Physical Memory

0x00	20	f6	ef	ea	a2	5e	9f	1a
0x08	a2	d0	4f	c4	a0	0c	f7	27
0x10	b8	bd	1a	ca	35	95	cb	80
0x18	84	3f	02	4f	8e	f3	f6	e5
0x20	cd	4a	f6	48	1a	6f	7e	63
0x28	e9	36	ae	32	0d	37	bc	c9
0x30	93	dc	b8	7a	3b	1a	b2	0c
0x38	d3	a6	a4	71	e2	23	9c	59

Recall: General Caching Concepts: 3 Types of Cache Misses

- **Cold (compulsory) miss**
 - Cold misses occur because the cache starts empty and this is the first reference to the block.
- **Capacity miss**
 - Occurs when the set of active cache blocks (**working set**) is larger than the cache.
- **Conflict miss**
 - Most caches limit blocks at level $k+1$ to a small subset (sometimes a singleton) of the block positions at level k .
 - E.g. Block i at level $k+1$ must be placed in block $(i \bmod 4)$ at level k .
 - Conflict misses occur when the level k cache is large enough, but multiple data objects all map to the same level k block.
 - E.g. Referencing blocks 0, 8, 0, 8, 0, 8, ... would miss every time.



Cache Example #3: Effective Access Time

Find the EAT for a system with the following properties:

- Cache access time: 10 ns
- Cache miss rate: 1%
- Main Memory access time: 200 ns

$$\begin{aligned} \text{EAT} &= T_{\text{cache}} + (1 - \text{Hit Rate}) * T_{\text{Memory}} \\ &= 10 + 0.01 * 200 \\ &= 10 + 2 \\ &= 12 \text{ ns} \end{aligned}$$

Locality in Programs

Principle of Locality:

- Programs tend to use data and instructions with addresses near or equal to those they have used recently.
- **Temporal locality:**
 - Recently referenced items are likely be referenced in the near future.
- **Spatial locality:**
 - Items with nearby addresses tend to be referenced close together in time.

```
int main(){
    int l = 0;
    int square_sum = 0;
    for (l = 0; l < 10; l++){
        int square = l * l;
        square_sum += square;
    }
    return 0;
}
```

```
000000000400512 <main>:
400512: 55                push   %rbp
400513: 48 89 e5          mov    %rsp,%rbp
400516: c7 45 fc 00 00 00 movl   $0x0,-0x4(%rbp)
40051d: c7 45 f8 00 00 00 movl   $0x0,-0x8(%rbp)
400524: c7 45 fc 00 00 00 movl   $0x0,-0x4(%rbp)
40052b: eb 14            jnp   400541 <main+0x2f>
40052d: 8b 45 fc          mov    -0x4(%rbp),%eax
400530: 0f af 45 fc      inl   -0x4(%rbp),%eax
400534: 89 45 f4          mov    %eax,-0xc(%rbp)
400537: 8b 45 f4          mov    -0xc(%rbp),%eax
40053a: 01 45 f8          add   %eax,-0x8(%rbp)
40053d: 83 45 fc 01      addl  $0x1,-0x4(%rbp)
400541: 83 7d fc 09      cmpl  $0x9,-0x4(%rbp)
400545: 7e e6            jle   40052d <main+0x1b>
400547: b8 00 00 00 00  mov   $0x0,%eax
40054c: 5d                pop   %rbp
40054d: c3                retq
40054e: 66 90            xchg  %ax,%ax
```

Temporal or Spatial Locality?

Locality in Programs

Principle of Locality:

- Programs tend to use data and instructions with addresses near or equal to those they have used recently.
- **Temporal locality:**
 - Recently referenced items are likely be referenced in the near future.
- **Spatial locality:**
 - Items with nearby addresses tend to be referenced close together in time.

```
int main(){
    int i = 0;
    int square_sum = 0;
    for (i = 0; i < 10; i++){
        int square = i * i;
        square_sum += square;
    }
    return 0;
}
```

```
000000000400512 <main>:
400512: 55                push   %rbp
400513: 48 89 e5          mov    %rsp,%rbp
400516: c7 45 fc 00 00 00 movl   $0x0,-0x4(%rbp)
40051d: c7 45 f8 00 00 00 movl   $0x0,-0x8(%rbp)
400524: c7 45 fc 00 00 00 movl   $0x0,-0x4(%rbp)
40052b: eb 14            jnp   400541 <main+0x2f>
40052d: 8b 45 fc          mov    -0x4(%rbp),%eax
400530: 0f af 45 fc      inl   -0x4(%rbp),%eax
400534: 89 45 f4          mov    %eax,-0xc(%rbp)
400537: 8b 45 f4          mov    -0xc(%rbp),%eax
40053a: 01 45 f8          add   %eax,-0x8(%rbp)
40053d: 83 45 fc 01      addl  $0x1,-0x4(%rbp)
400541: 83 7d fc 09      cmpl  $0x9,-0x4(%rbp)
400545: 7e e6            jle   40052d <main+0x1b>
400547: b8 00 00 00 00  mov   $0x0,%eax
40054c: 5d                pop    %rbp
40054d: c3                retq
40054e: 66 90            xchg  %ax,%ax
```

Temporal or Spatial Locality?

Both!

Recall: Spatial Locality in Arrays

```
1 int sumarraycols(int a[M][N])
2 {
3     int i, j, sum = 0;
4
5     for (j = 0; j < N; j++)
6         for (i = 0; i < M; i++)
7             sum += a[i][j];
8     return sum;
9 }
```

(a)

Address	0	4	8	12	16	20
Contents	a_{00}	a_{01}	a_{02}	a_{10}	a_{11}	a_{12}
Access order	1	3	5	2	4	6

(b)

order

Good Locality?

No! (Stride-N pattern)

Recall: Spatial Locality in Arrays

```
1 int sumarrayrows(int a[M][N])
2 {
3     int i, j, sum = 0;
4
5     for (i = 0; i < M; i++)
6         for (j = 0; j < N; j++)
7             sum += a[i][j];
8     return sum;
9 }
```

(a)

Address	0	4	8	12	16	20
Contents	a_{00}	a_{01}	a_{02}	a_{10}	a_{11}	a_{12}
Access order	1	2	3	4	5	6

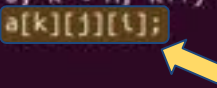
(b)

order

Good Locality?

Recall: Spatial Locality in Arrays

```
int sum3d(int a[M][M][M]){
    int sum;
    for(int l = 0; l < M; l++)
        for(int j = 0; j < M; j++)
            for(int k = 0; k < M; k++)
                sum += a[k][j][l];
    return sum;
}
```



Good Locality?

No!

Locality in Data

```
int A[10][10], B[10][10], C[10][10];  
  
for(int i = 0; i < 10; i++){  
    for(int j = 0; j < 10; j++){  
        for(int k = 0; k < 10; k++){  
            C[i][k] = C[i][k] + A[i][j] + B[j][k];  
        }  
    }  
}
```

Good Locality?

Locality in Data

```
int A[10][10], B[10][10], C[10][10];
int temp;

for(int i = 0; i < 10; i++){
    for (int j = 0; j < 10; j++){
        temp = A[i][j];
        for (int k = 0; k < 10; k++){
            C[i][k] = C[i][k] + temp * B[j][k]
        }
    }
}
```

How about this one?

Concluding Observations

Programmer can optimize for cache performance

- How data structures are organized
- How data are accessed
 - Nested loop structure
 - Blocking is a general technique

All systems favor “cache friendly code”

- Getting absolute optimum performance is very platform specific
 - Cache sizes, line sizes, associatives, etc.
- Can get most of the advantage with generic code
 - Keep working set reasonably small (**temporal locality**)
 - Use small strides (**spatial locality**)

Callgrind



Code Profiling

- A **code profiler** is a tool to analyze a program and report on its resource usage
 - "resource" could be memory, CPU cycles, network bandwidth, and so on
- The program is run under control of a profiling tool
- During application development, a common step is to improve runtime performance using profiling tools.
- To not waste time on optimizing functions which are rarely used, one needs to know in which parts of the program most of the time is spent.
- Some example:
 - Callgrind, GProf, JConsol, CLR

Valgrind

the Valgrind framework supports a variety of runtime analysis tools

- memcheck
 - detects memory errors/leaks
- massif
 - reports on heap usage
- helgrind
 - detects multithreaded race conditions
- callgrind/cachegrind
 - profiles CPU/cache performance

Callgrind/cachegrind

- The Valgrind profiling tools are **cachegrind** and **callgrind**
- The **cachegrind** tool simulates the L1/L2 caches and counts cache misses/hits.
- The **callgrind** tool counts function calls and the CPU instructions executed within each call and builds a function callgraph
- The callgrind tool includes a cache simulation feature adopted from cachegrind, so you can actually use **callgrind** for both **CPU** and **cache profiling**.

Basic Usage of Callgrind

- First, we need to compile our program with debugging enabled
 - `gcc -g -ggdb name.c -o name.out`
- You first need to run your program under Valgrind and explicitly request the callgrind tool (if unspecified, the tool defaults to memcheck)

```
valgrind --tool=callgrind [possible options]
name.out program-arguments
```

- The result will be stored on the files `callgrind.out.PID`, where PID will be the process identifier.

Process identifier

```
==22417== Events      : Ir
==22417== Collected : 7247606
==22417==
==22417== I   refs:    7,247,606
```

Number of Instruction read (Ir)

Basic Usage of Callgrind

Counting instructions with callgrind

- The callgrind output file is a text file, but its contents are not intended for you to read yourself.
- You can properly read the output using

callgrind_annotate

- `callgrind_annotate --auto=yes callgrind.out.PID`
- The `--auto=yes` option report counts for each C statement
- Do not forget to replace `PID` by the actual number.

Sorts a 1000-member array using selection sort

```
. void swap(int *a, int *b)
3,000 {
3,000     int tmp = *a;
4,000     *a = *b;
3,000     *b = tmp;
2,000 }
.
. int find_min(int arr[], int start, int stop)
3,000 {
2,000     int min = start;
2,005,000     for(int i = start+1; i <= stop; i++)
4,995,000         if (arr[i] < arr[min])
6,178             min = i;
1,000     return min;
2,000 }
. void selection_sort(int arr[], int n)
3 {
4,005     for (int i = 0; i < n; i++) {
9,000         int min = find_min(arr, i, n-1);
7,014,178 => sorts.c:find_min (1000x)
10,000         swap(&arr[i], &arr[min]);
15,000 => sorts.c:swap (1000x)
.     }
2 }
.
```


Interpreting the results

- The Ir counts are basically the count of assembly instructions executed.
- By default, the counts are *exclusive*
- The counts for a function include only the time spent in that function and not in the functions that it calls.
- By using exclusive counts you can detect the bottlenecks.
- Here, the work is concentrated in the loop to find the min value

```
. void swap(int *a, int *b)
3,000 {
3,000     int tmp = *a;
4,000     *a = *b;
3,000     *b = tmp;
2,000 }

.
.
. int find_min(int arr[], int start, int stop)
3,000 {
2,000     int min = start;
2,005,000 for(int i = start+1; i <= stop; i++)
4,995,000     if (arr[i] < arr[min])
6,178         min = i;
1,000     return min;
2,000 }

. void selection_sort(int arr[], int n)
3 {
4,005     for (int i = 0; i < n; i++) {
9,000         int min = find_min(arr, i, n-1);
7,014,178 => sorts.c:find_min (1000x)
10,000         swap(&arr[i], &arr[min]);
15,000 => sorts.c:swap (1000x)
.     }
2 }
.
```

Basic Usage of Callgrind

Adding in cache simulation

- Invoke valgrind `--simulate-cache=yes` by
valgrind --tool=callgrind --simulate-cache=yes name.out args
- The cache simulator models a machine with a split L1 cache (separate instruction I1 and data D1), backed by a unified second-level cache (L2).
- Similar to the previous example, `callgrind_annotate` should be used to interpret the output.

Callgrind Example

```
==16409== Events      : Ir Dr Dw I1mr D1mr D1mw I2mr D2mr D2mw
==16409== Collected : 7163066 4062243 537262 591 610 182 16 103 94
==16409==
==16409== I   refs:      7,163,066
==16409== I1  misses:      591
==16409== L2i misses:      16
==16409== I1  miss rate:    0.0%
==16409== L2i miss rate:  0.0%
==16409==
==16409== D   refs:      4,599,505 (4,062,243 rd + 537,262 wr)
==16409== D1  misses:      792 (   610 rd +   182 wr)
==16409== L2d misses:      197 (   103 rd +    94 wr)
==16409== D1  miss rate:    0.0% (   0.0% +   0.0% )
==16409== L2d miss rate:  0.0% (   0.0% +   0.0% )
==16409==
==16409== L2 refs:      1,383 (   1,201 rd +    182 wr)
==16409== L2  misses:      213 (    119 rd +    94 wr)
==16409== L2  miss rate:    0.0% (   0.0% +   0.0% )
```

It sounds like we have a cache friendly code.

Ir: I cache reads (instructions executed)

I1mr: I1 cache read misses (instruction wasn't in I1 cache but was in L2)

I2mr: L2 cache instruction read misses (instruction wasn't in I1 or L2 cache, had to be fetched)

Dr: D cache reads (memory reads)

D1mr: D1 cache read misses (data location not in D1 cache, but in L2)

D2mr: L2 cache data read misses (location not in D1 or

L2) **Dw:** D cache writes (memory writes)

D1mw: D1 cache write misses (location not in D1 cache, but in L2)

D2mw: L2 cache data write misses (location not in D1 or L2)

Callgrind Example

```

----- Auto-annotated source: sorts.c -----
-----
      Ir      Or      Dw I1mr D1mr D1mw I2mr D2mr D2mw
      .      .      . . . . . . . . . . void swap(int *a, int *b)
3,000      0      1,000      1      0      0      1      . . {
3,000      2,000      1,000      . . . . . . . . . . int tmp = *a;
4,000      3,000      1,000      . . . . . . . . . . *a = *b;
3,000      2,000      1,000      . . . . . . . . . . *b = tmp;
2,000      2,000      . . . . . . . . . . }
      .
      . . . . . . . . . . int find_min(int arr[], int start, int st
op)
3,000      0      1,000      1      0      0      1      . . {
2,000      1,000      1,000      0      0      1      0      0      1      int min = start;
2,005,000 1,002,000 500,500      . . . . . . . . . . for(int i = start+1; i <= st
op; i++)
4,995,000 2,997,000      0      0      32      0      0      19      .      if (arr[i] < arr[m
in])
6,144      3,072      3,072      . . . . . . . . . . min = i;
1,000      1,000      . . . . . . . . . . return min;
2,000      2,000      . . . . . . . . . . }
      .
      . . . . . . . . . . void selection_sort(int arr[], int n)
3      0      1      1      0      0      1      . . {
4,005      2,002      1,001      . . . . . . . . . . for (int i = 0; i < n; i++) {
9,000      3,000      5,000      . . . . . . . . . . int min = find_min(arr, i, n
-1);
7,014,144 4,006,072 505,572      1      32      1      1      19      1 => sorts.c:find_min
(1000x)
10,000      4,000      3,000      . . . . . . . . . . swap(&arr[i], &arr[min]);
15,000      9,000      4,000      1      0      0      1      . . => sorts.c:swap(1000x)
      .
      . . . . . . . . . . }
2      2      . . . . . . . . . . }

```

Ir: I cache reads (instructions executed)

I1mr: I1 cache read misses (instruction wasn't in I1 cache but was in L2)

I2mr: L2 cache instruction read misses (instruction wasn't in I1 or L2 cache, had to be fetched)

Dr: D cache reads (memory reads)

D1mr: D1 cache read misses (data location not in D1 cache, but in L2)

D2mr: L2 cache data read misses (location not in D1 or

L2) **Dw:** D cache writes (memory writes)

D1mw: D1 cache write misses (location not in D1 cache, but in L2)

D2mw: L2 cache data write misses (location not in D1 or L2)

Additional Points

- L2 misses are much more expensive than L1 misses, so pay attention to passages with high **D2mr** or **D2mw** counts.
- Even a small number of misses can be quite important, as a L1 miss will typically cost around 5-10 cycles, an L2 miss can cost as much as 100-200 cycles
- Callgrind cannot detect the bottleneck of your program if it is related to file I/O
- Try to examine different paths of your program

Profile data file 'callgrind.out.18974' (creator: callgrind-3.15.0)

L1 cache: 32768 B, 64 B, 4-way associative
L2 cache: 32768 B, 64 B, 8-way associative
L3 cache: 8388608 B, 64 B, 16-way associative
Memrange: Basic block 0 - 17981881
Trigger: Program termination
Profiled target: ./matrix_good.out (PID 18974, part 1)
Events recorded: Ir Dr Dw IIR DLR DIMW IILR DLRR DLRW
Events shown: Ir Dr Dw IIR DLR DIMW IILR DLRR DLRW
Event sort order: Ir Dr Dw IIR DLR DIMW IILR DLRR DLRW
Thresholds: 99 0 0 0 0 0 0 0 0
Exclude dirs:
User annotated:
Auto-annotation: on

```
-----  
Ir      Dr      Dw      IILR DLR  DIMW  IILR DLRR DLRW  
-----  
885,238,763 25,487,284 13,054,426 887 63,834 63,075 798 1,065 42,937 PROGRAM TOTALS  
-----
```

```
-----  
Ir      Dr      Dw      IILR DLR  DIMW  IILR DLRR DLRW  file:function  
-----  
85,979,729 5,829,269 3,028,218 4 1 62,501 4 0 62,489 matrix_good.c:main [./Users/mcokolek21/201/Lab8/matrix_good.out]  
25,967,742 8,888,888 4,088,888 2 3 0 2 2 . /usr/src/debug/glibc-2.17-c758a86/stdlib/random_r.c:random_r [./usr  
32,090,913 7,840,485 2,028,205 2 62,501 0 2 . - matrix_good.c:efficient_sum [./Users/mcokolek21/201/Lab8/matrix_good  
17,088,080 4,888,888 3,088,888 3 0 1 3 0 1 /usr/src/debug/glibc-2.17-c758a86/stdlib/random.c:random [./usr/lib  
4,088,888 1,888,888 1,088,888 1 0 0 1 . . /usr/src/debug/glibc-2.17-c758a86/stdlib/rand.c:rand [./usr/lib64/l  
-----
```

-- Auto-annotated source: matrix_good.c

```
-----  
Ir      Dr      Dw      IILR DLR  DIMW  IILR DLRR DLRW  
-----  
.      .      .      .      .      .      .      .      .      #include <stdio.h>  
.      .      .      .      .      .      .      .      .      #include <stdlib.h>  
.      .      .      .      .      .      .      .      .      .  
.      .      .      .      .      .      .      .      .      .  
3      0      2 1 0 0 1 . .      int efficient_sum(int arr[100][100][100]){  
.      .      .      .      .      .      .      .      .      .      int i, j, k;  
1      0      1 . . . . .      int size = 100;  
1      0      1 . . . . .      int sum = 0;  
485 282 181 . . . . .      for(i = 0; i < size; i++){  
48,588 28,288 18,188 . . . . .      for(j = 0; j < size; j++){  
4,050,080 2,028,080 1,018,080 1 0 0 1 . .      for(k = 0; k < size; k++){  
18,088,080 5,888,080 1,088,080 0 62,500 . . . . .      sum += arr[i][j][k];  
.      .      .      .      .      .      .      .      .      .      }  
.      .      .      .      .      .      .      .      .      .      }  
.      .      .      .      .      .      .      .      .      .      }  
1      1      .      .      .      .      .      .      .      return sum;  
2      2      0 0 1 . . . . . }  
-----
```

Profile data file 'callgrind.out.27711' (creator: callgrind-3.15.0)

L1 cache: 32768 B, 64 B, 8-way associative
D1 cache: 32768 B, 64 B, 8-way associative
L2 cache: 26214400 B, 64 B, 32-way associative
Time range: basic block 0 - 17081676
Trigger: Program termination
Profiled target: ./matrix_bad.out (PID 27711, part 1)
Events recorded: Ir Dr Dw IInr DInr DIW ILnr DLnr DLW
Events shown: Ir Dr Dw IInr DInr DIW ILnr DLnr DLW
Event sort order: Ir Dr Dw IInr DInr DIW ILnr DLnr DLW
Thresholds: 99 0 0 0 0 0 0 0 0
Include dirs:
User annotated:
Auto-annotation: on

```
-----  
Ir      Dr      Dw      IInr DInr      DIW      ILnr DLnr DLW  
106,258,117 28,187,282 13,854,422 812 1,001,319 1,900,565 887 1,064 62,935  PROGRAM TOTALS  
-----
```

```
-----  
Ir      Dr      Dw      IInr DInr      DIW      ILnr DLnr DLW  file:function  
-----  
37,090,930 6,640,410 3,629,210  4      2 999,985  4  0 62,488  matrix_bad.c:main [/Users/mcokelek21/201/Labs/matrix_bad.out]  
25,967,742 8,000,000 4,000,000  2      3  0  2  2  -  /usr/src/debug/glibc-2.17-c758a686/stdlib/random_r.c:random_r [/usr/lib64/libc.so.6]  
22,090,913 7,040,485 2,828,285  2 999,980  0  2  -  -  matrix_bad.c:inefficient_sum [/Users/mcokelek21/201/Lab0/matrix_inefficient.c]  
17,000,000 4,000,000 3,000,000  3      0  1  3  0  1  /usr/src/debug/glibc-2.17-c758a686/stdlib/random.c:random [/usr/lib64/libc.so.6]  
 4,000,000 1,000,000 1,000,000  1      0  0  1  -  -  /usr/src/debug/glibc-2.17-c758a686/stdlib/rand.c:rand [/usr/lib64/libc.so.6]  
-----
```

Auto-annotated source: matrix_bad.c

```
-----  
Ir      Dr      Dw      IInr DInr      DIW      ILnr DLnr DLW  
-----  
-      -      -      -      -      -      -      -      -      #include <stdio.h>  
-      -      -      -      -      -      -      -      -      #include <stdlib.h>  
-      -      -      -      -      -      -      -      -      -  
-      -      -      -      -      -      -      -      -      -  
 3      0      2  1  0  0  1  -      -      int inefficient_sum(int arr[100][100][100]){  
-      -      -      -      -      -      -      -      -      -      int i, j, k;  
 1      0      1  -      -      -      -      -      -      int size = 100;  
 1      0      1  -      -      -      -      -      -      int sum = 0;  
 495  282  101  -      -      -      -      -      -      for(k = 0; k < size; k++){  
 40,500 20,250 10,100  -      -      -      -      -      -      -      for(i = 0; i < size; i++){  
4,050,000 2,025,000 1,010,000  1  0  0  1  -      -      for(j = 0; j < size; j++){  
18,000,000 5,000,000 3,000,000  0 999,986  -      -      -      -      -      sum += arr[i][j][k];  
-      -      -      -      -      -      -      -      -      -      }  
-      -      -      -      -      -      -      -      -      -      }  
-      -      -      -      -      -      -      -      -      -      }  
 1      1  -      -      -      -      -      -      -      -      return sum;  
 2      2  -      -      -      -      -      -      -      -      }  
-----
```

References

1. Some of the slides are borrowed from materials in Stanford CS107, CMU15-213 and CS201, Portland State University
2. <https://stackoverflow.com/questions/16699247/what-is-a-cache-friendly-code>
3. <https://www.valgrind.org/docs/manual/manual.html>
4. The Cache Simulator and its demos are borrowed from materials in University of Washington, CSE 351