

# COMP541

# DEEP LEARNING

Lecture #05 – Convolutional Neural Networks



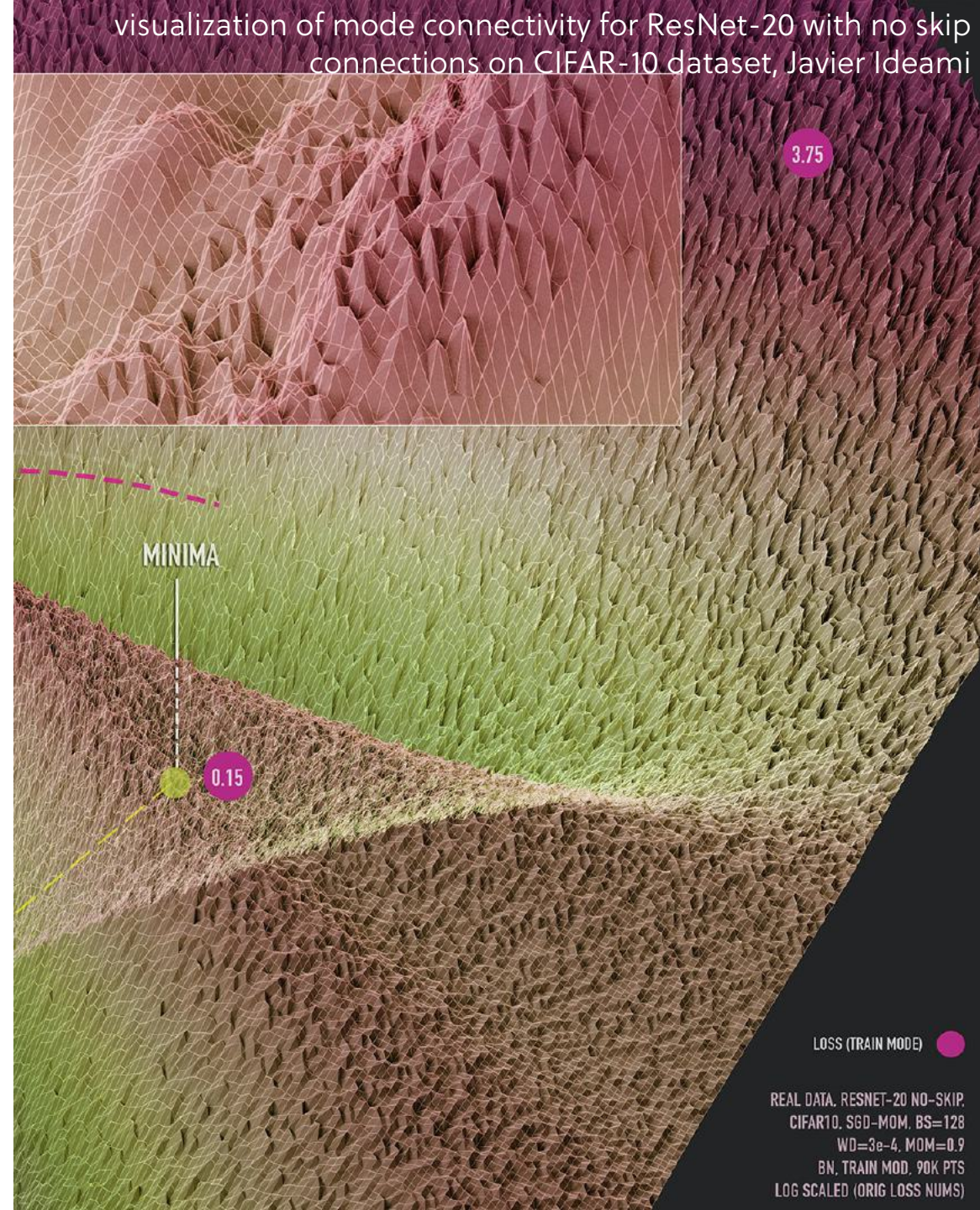
**KOÇ**  
**UNIVERSITY**

Aykut Erdem // Koç University // Fall 2024



# Previously on COMP541

- data preprocessing and normalization
- weight initializations
- ways to improve generalization
- optimization



# Lecture Overview

- convolution layer
- pooling layer
- cnn architectures
- design guidelines
- residual connections
- semantic segmentation networks
- addressing other tasks

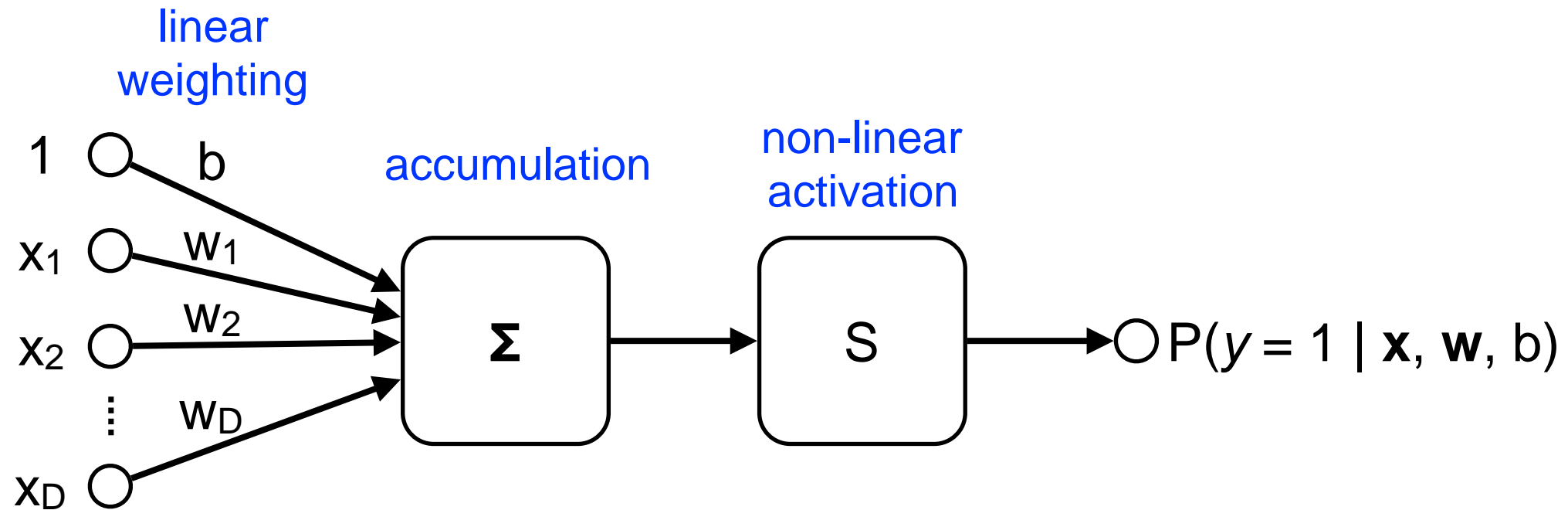
**Disclaimer:** Much of the material and slides for this lecture were borrowed from

- Andrea Vedaldi's tutorial on Convolutional Networks for Computer Vision Applications
- Kaiming He's ICML 2016 tutorial on Deep Residual Networks: Deep Learning Gets Way Deeper
- Fei-Fei Li, Andrej Karpathy and Justin Johnson's CS231n class
- Justin Johnson's EECS 498/598 class

# Perceptron

[Rosenblatt 57]

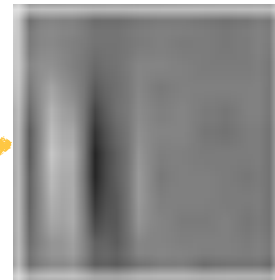
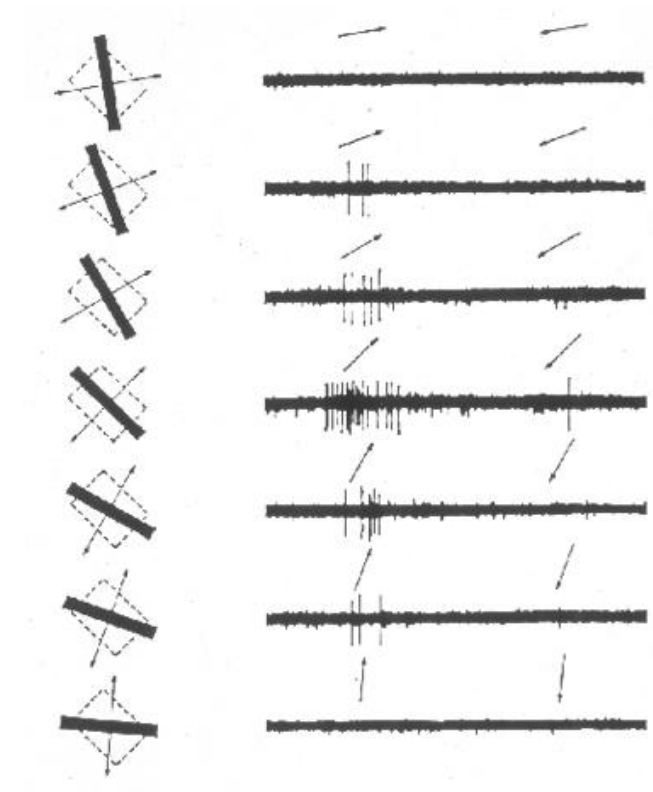
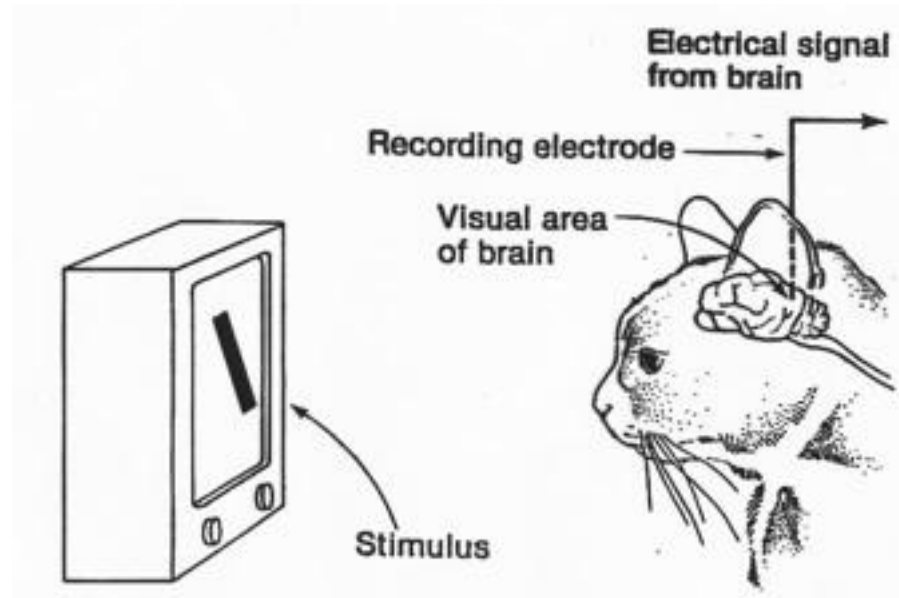
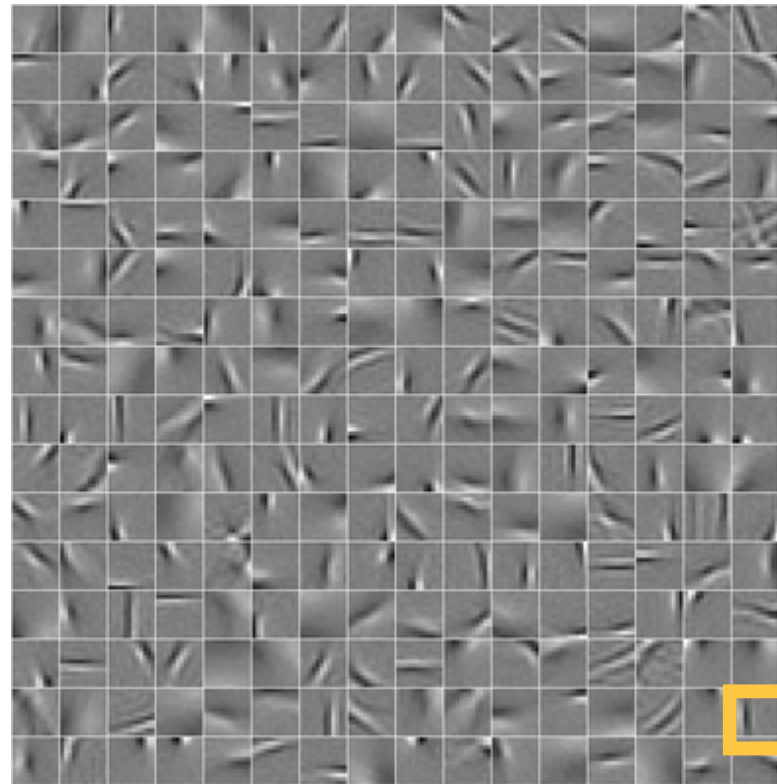
- The goal is estimating the posterior probability of the binary label  $y$  of a vector  $\mathbf{x}$ :





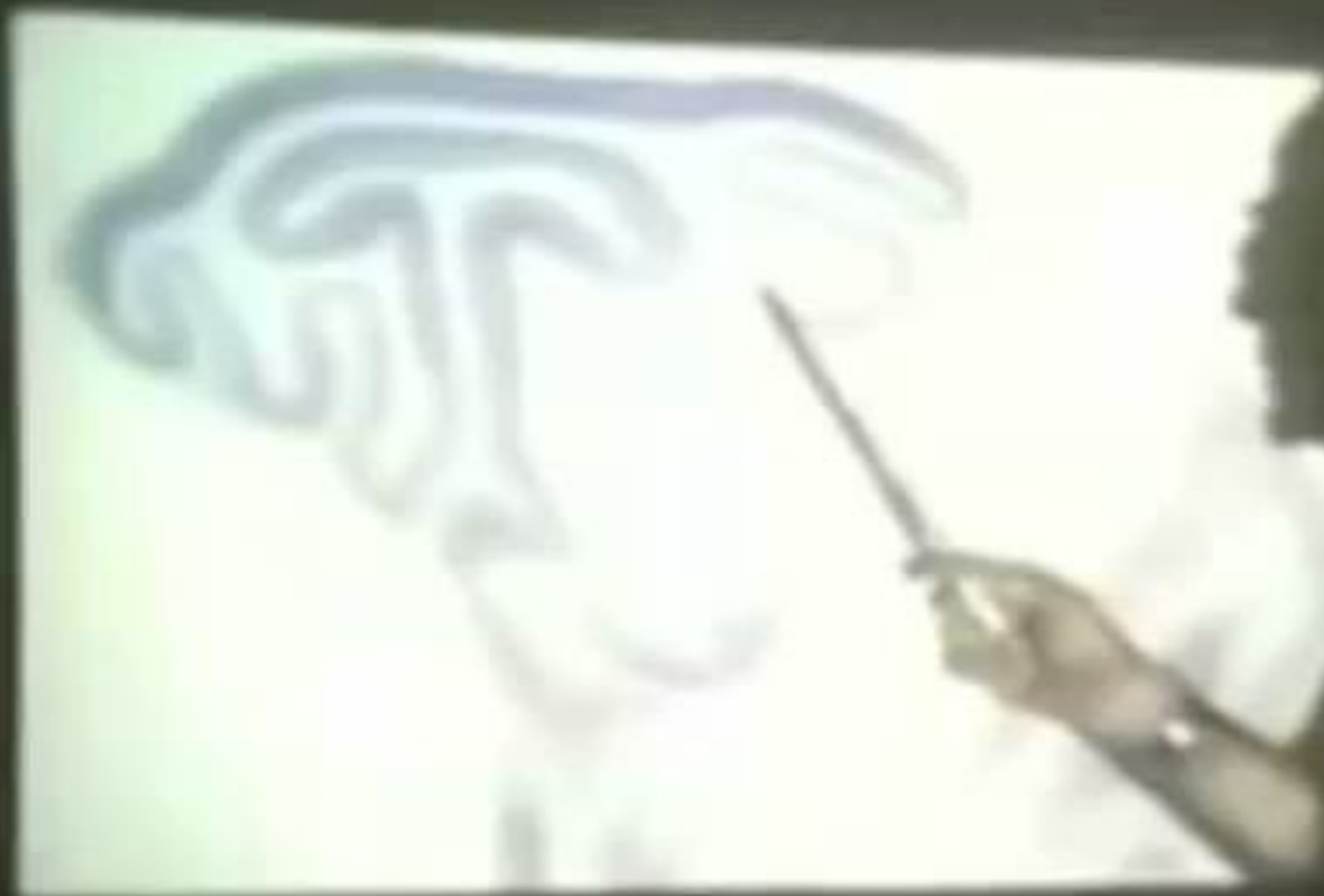
# Discovery of oriented cells in the visual cortex

[Hubel and Wiesel 59]



oriented filter



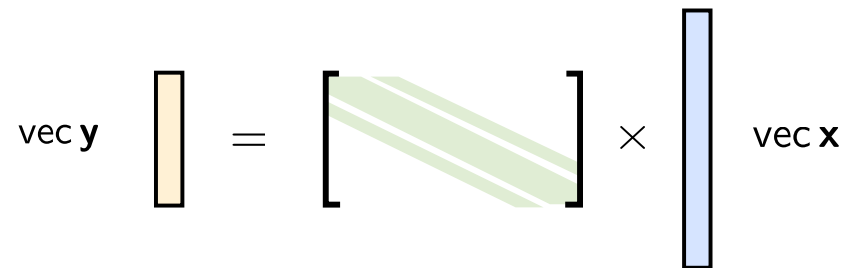








# Convolution



- Convolution = Spatial filtering

$$(a \star b)[i, j] = \sum_{i', j'} a[i', j'] b[i - i', j - j']$$

- Different filters (weights) reveal a different characteristics of the input.

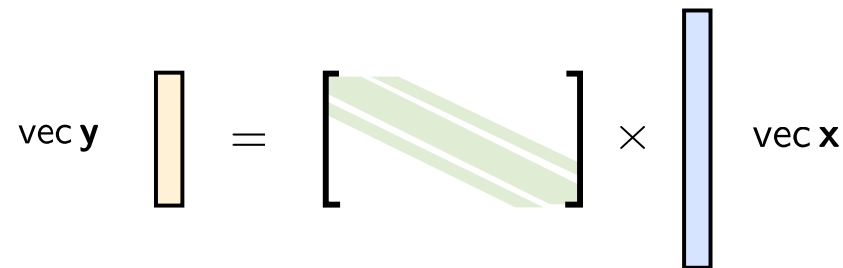


$\star^{1/8}$

0	1	0
1	4	1
0	1	0



# Convolution



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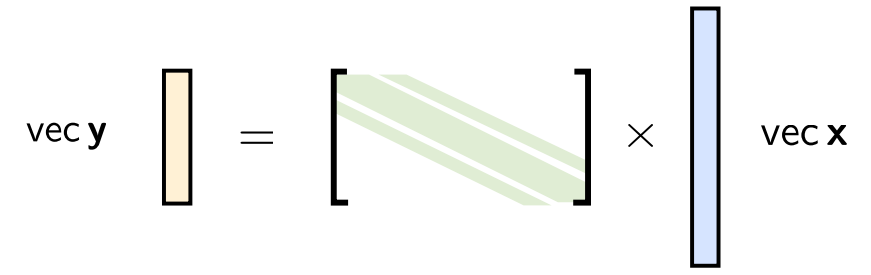
\*

0	-1	0
-1	4	-1
0	-1	0





# Convolution



- Convolution = Spatial filtering

$$(a \star b)[i, j] = \sum_{i', j'} a[i', j'] b[i - i', j - j']$$

- Different filters (weights) reveal a different characteristics of the input.



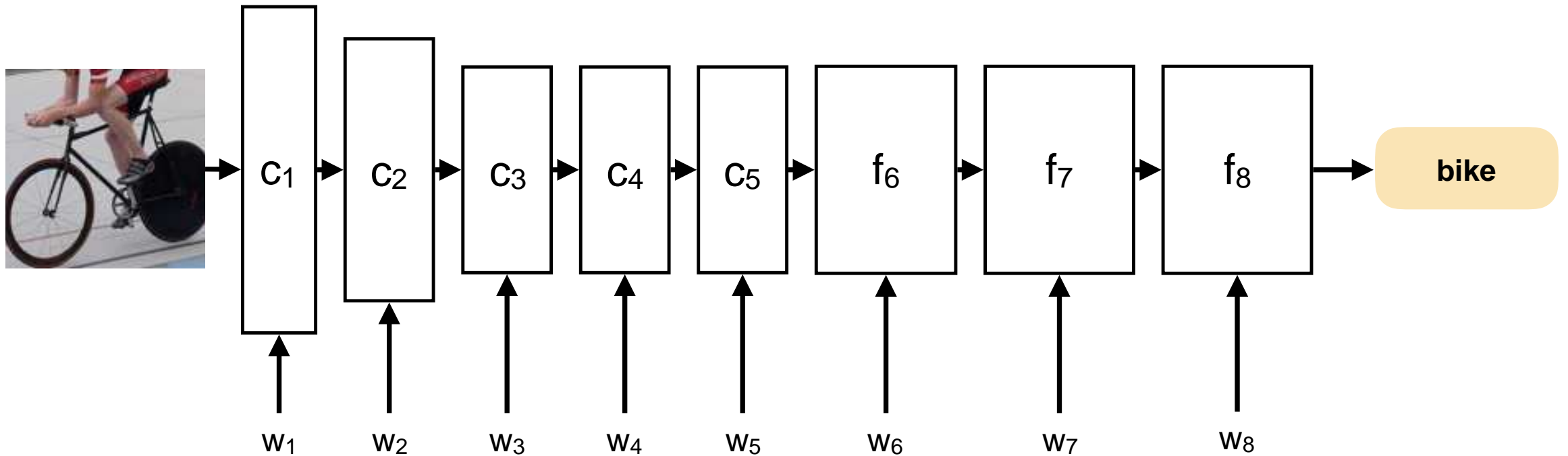
\*

1	0	-1
2	0	-2
1	0	-1



# Convolutional Neural Networks in a Nutshell

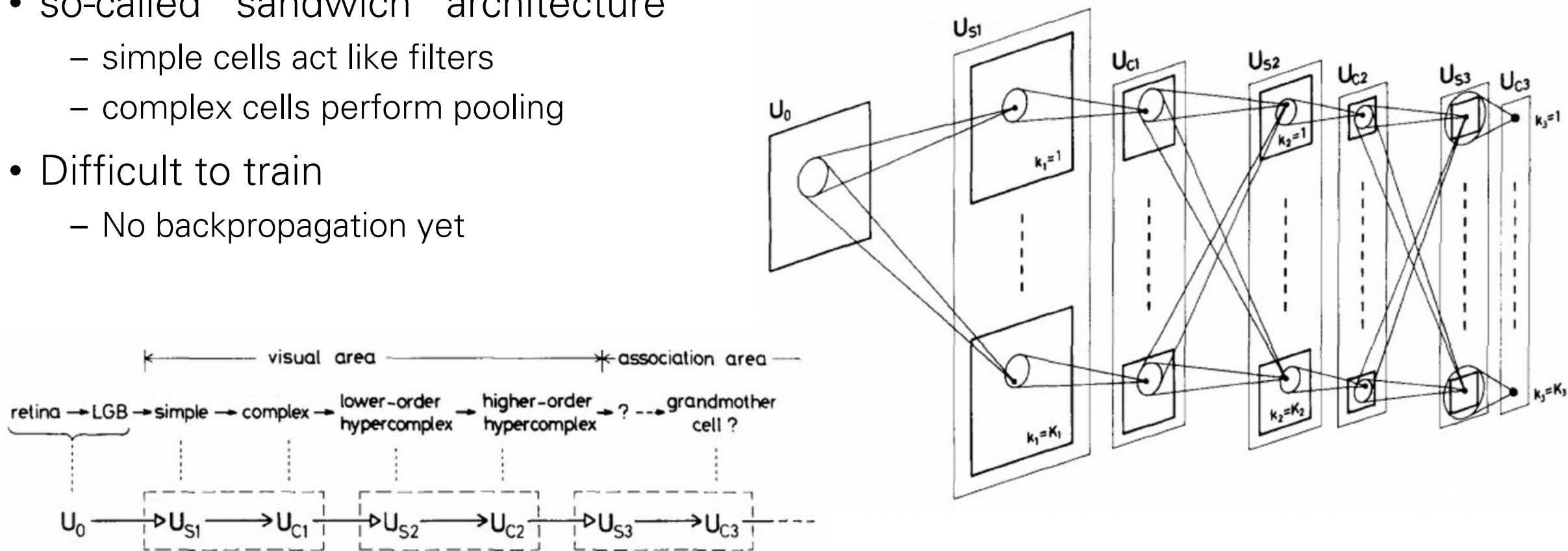
- A neural network model that consists of a sequence of local & translation-invariant layers
  - Many identical copies of the same neuron: Weight/parameter sharing
  - Hierarchical feature learning





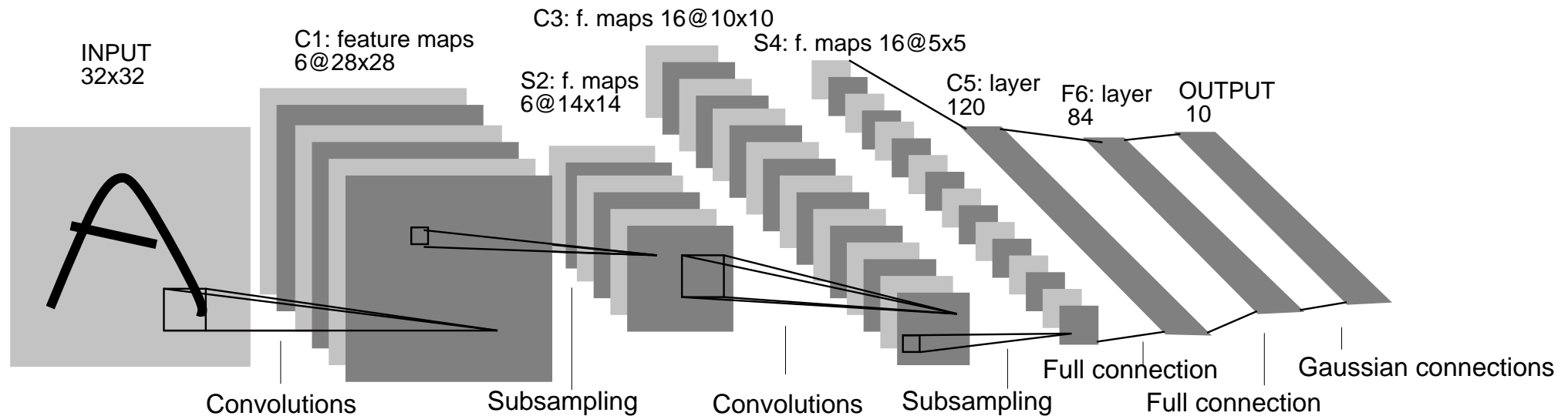
# A bit of history

- Neocognitron model by Fukushima (1980)
- The first convolutional neural network (CNN) model
- so-called “sandwich” architecture
  - simple cells act like filters
  - complex cells perform pooling
- Difficult to train
  - No backpropagation yet



# A bit of history

- LeNet-5 model

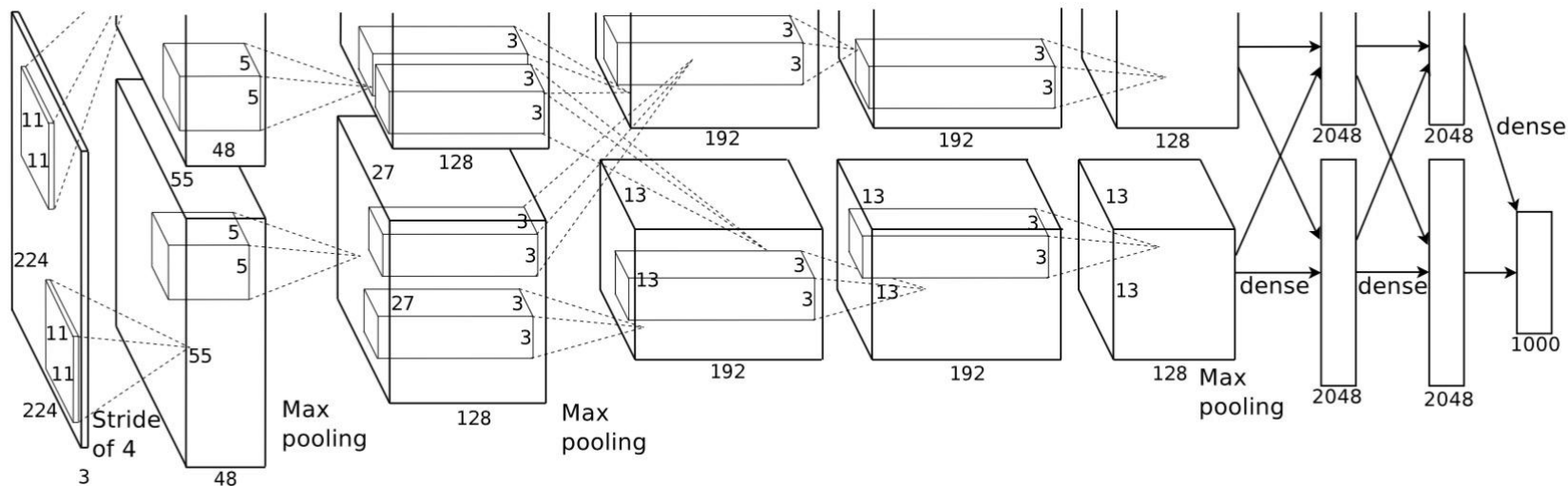


Y. LeCun, L. Bottou, Y. Bengio, and P. Haffner. **Gradient-based learning applied to document recognition.** Proceedings of the IEEE. **86** (11): 2278–2324, 1998.

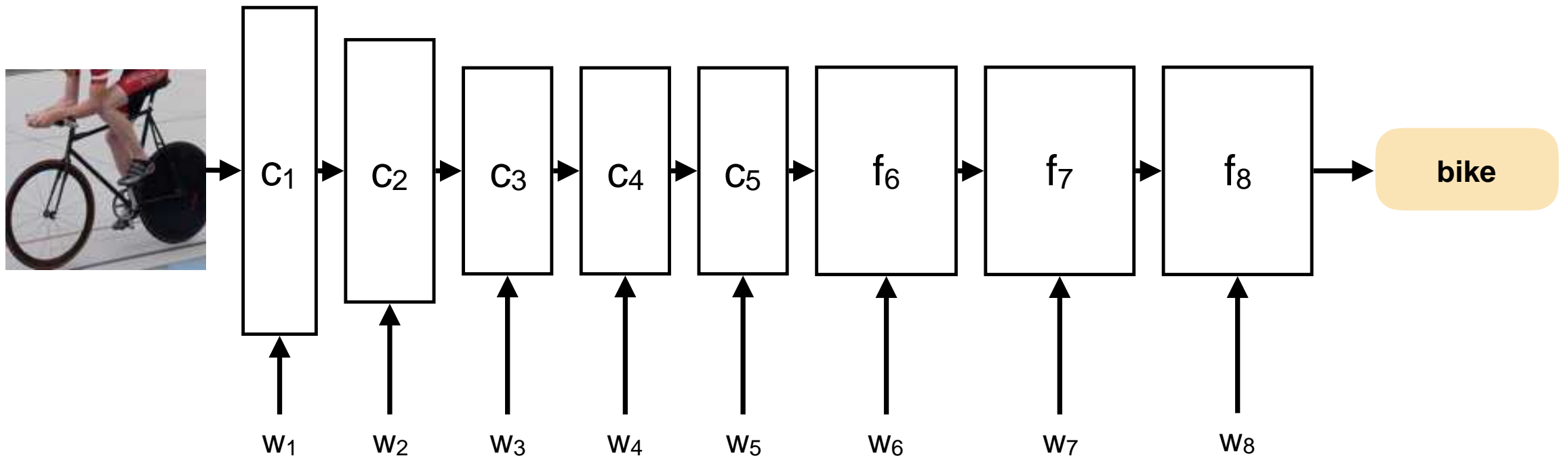


# A bit of history

- AlexNet model



# Convolutional Neural Network

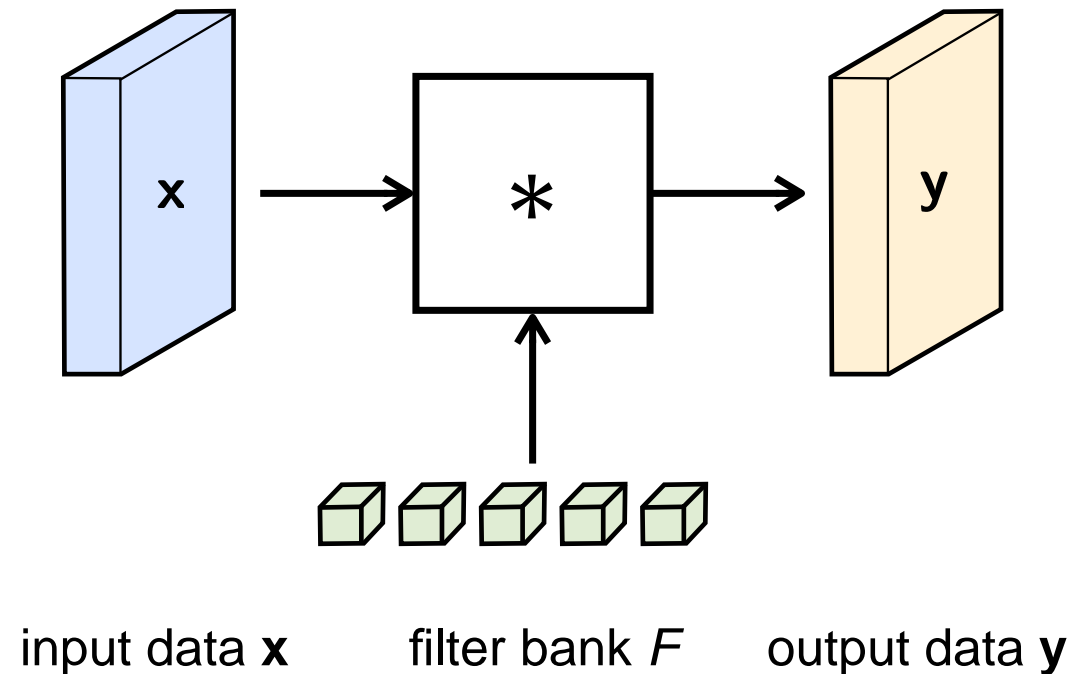


A. Krizhevsky, I. Sutskever, and G. E. Hinton. **Imagenet classification with deep convolutional neural networks**. In NIPS 2012.

# Convolutional layer

- Learn a filter bank (a set of filters) once
- Use them over the input data to extract features

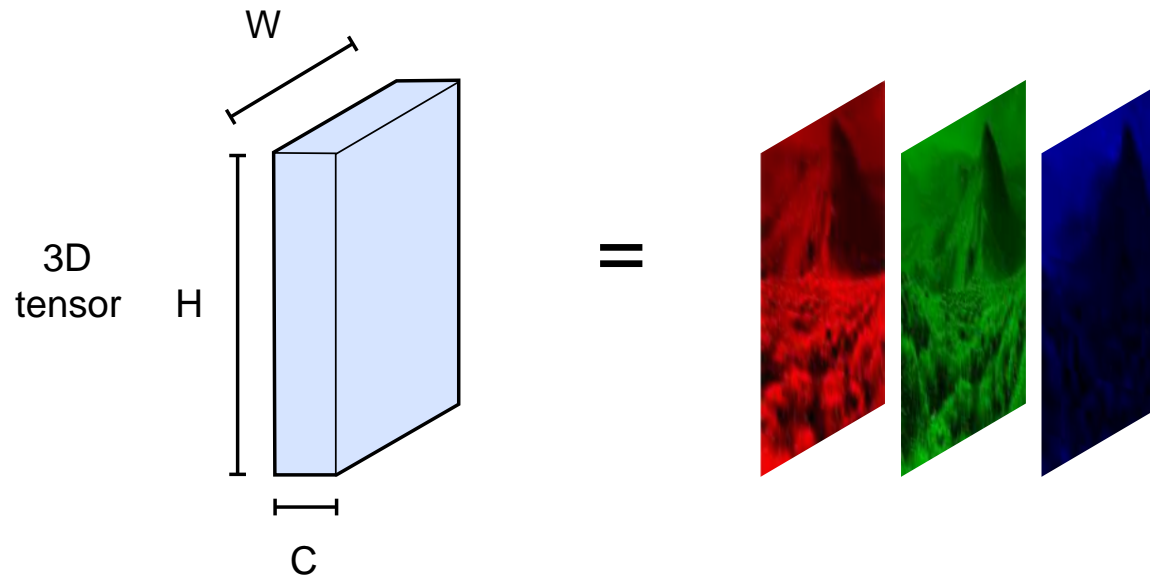
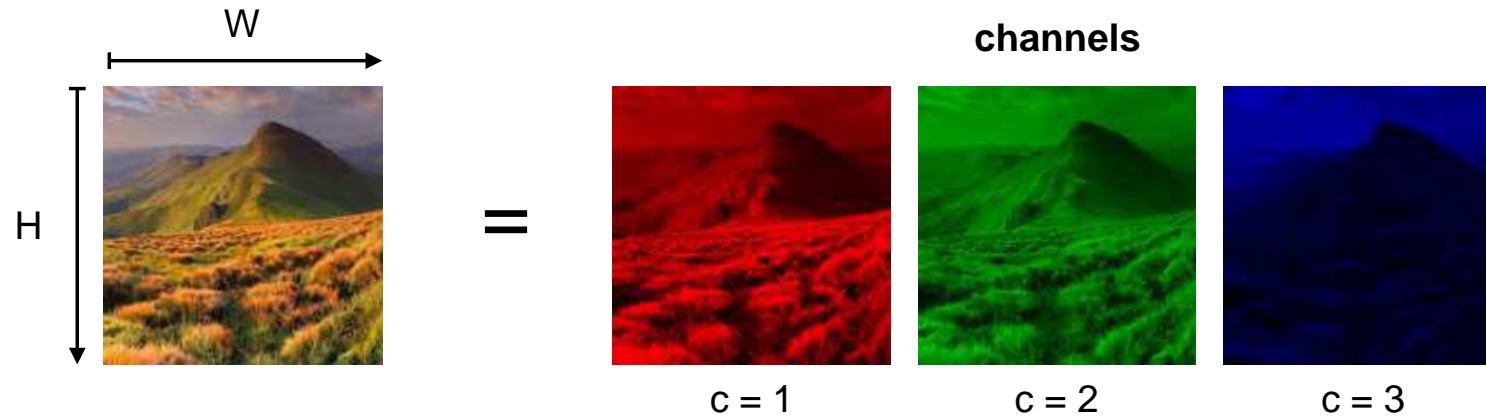
$$y = F * x + b$$





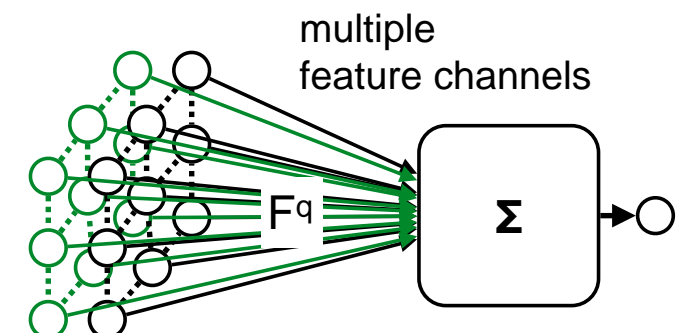
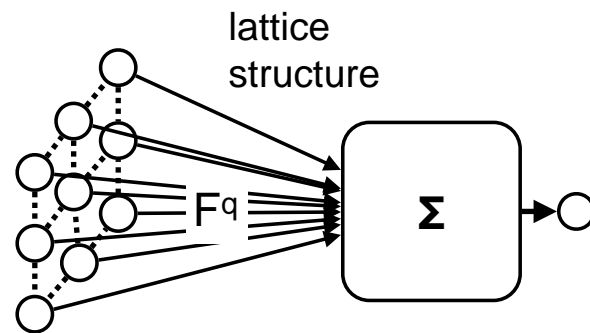
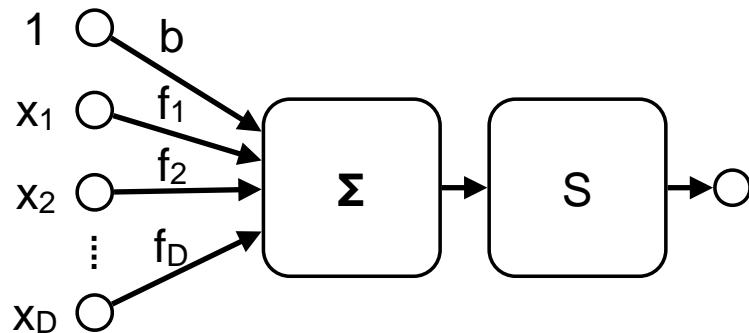
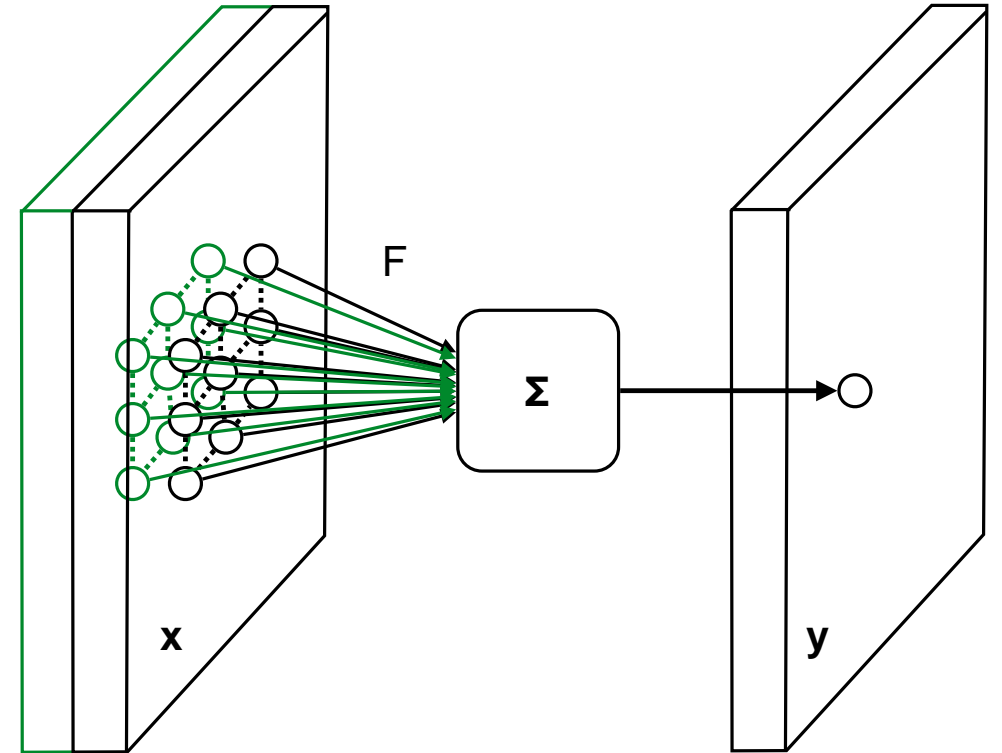
# Data = 3D Tensors

- There is a vector of feature channels (e.g. RGB) at each spatial location (pixel).



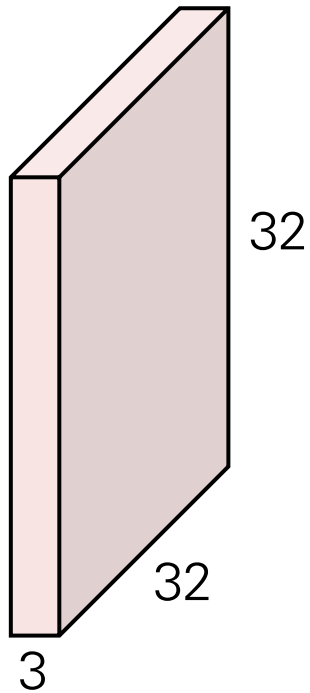
# Convolutions with 3D Filters

- Each filter acts on multiple input channels
- **Local**  
Filters look locally
- **Translation invariant**  
Filters act the same everywhere



# Convolutional Layer

32x32x3 input



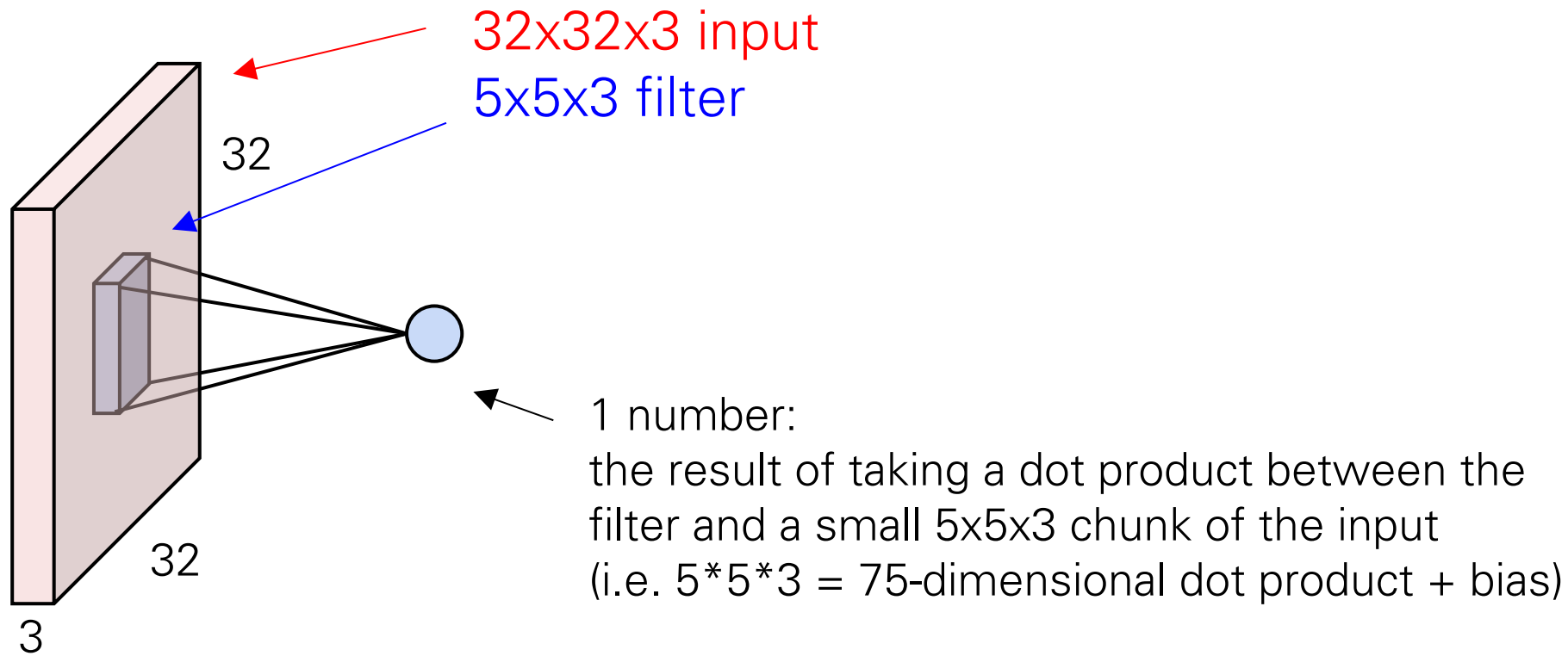
5x5x3 filter



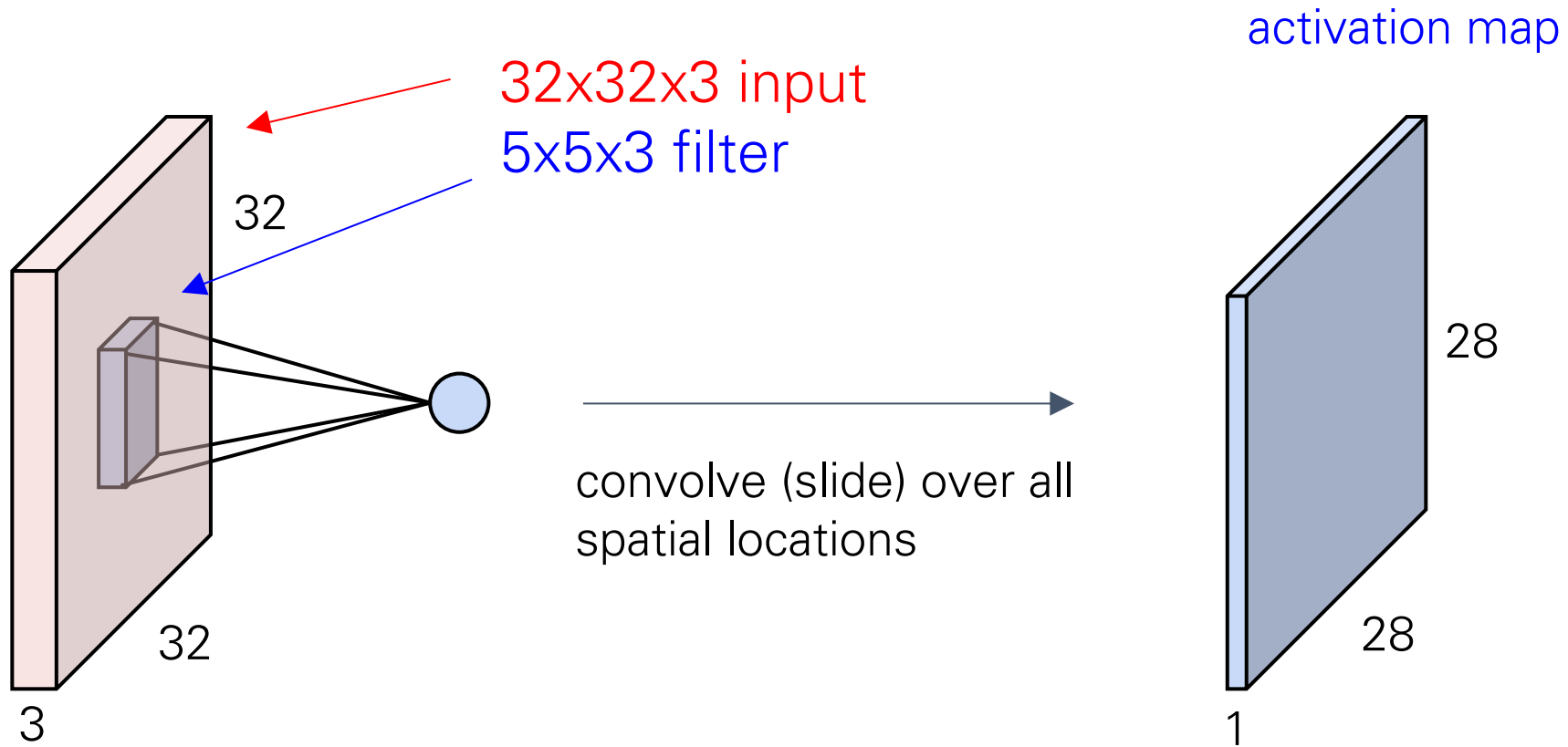
Convolve the filter with the input  
i.e. "slide over the image spatially,  
computing dot products"



# Convolutional Layer

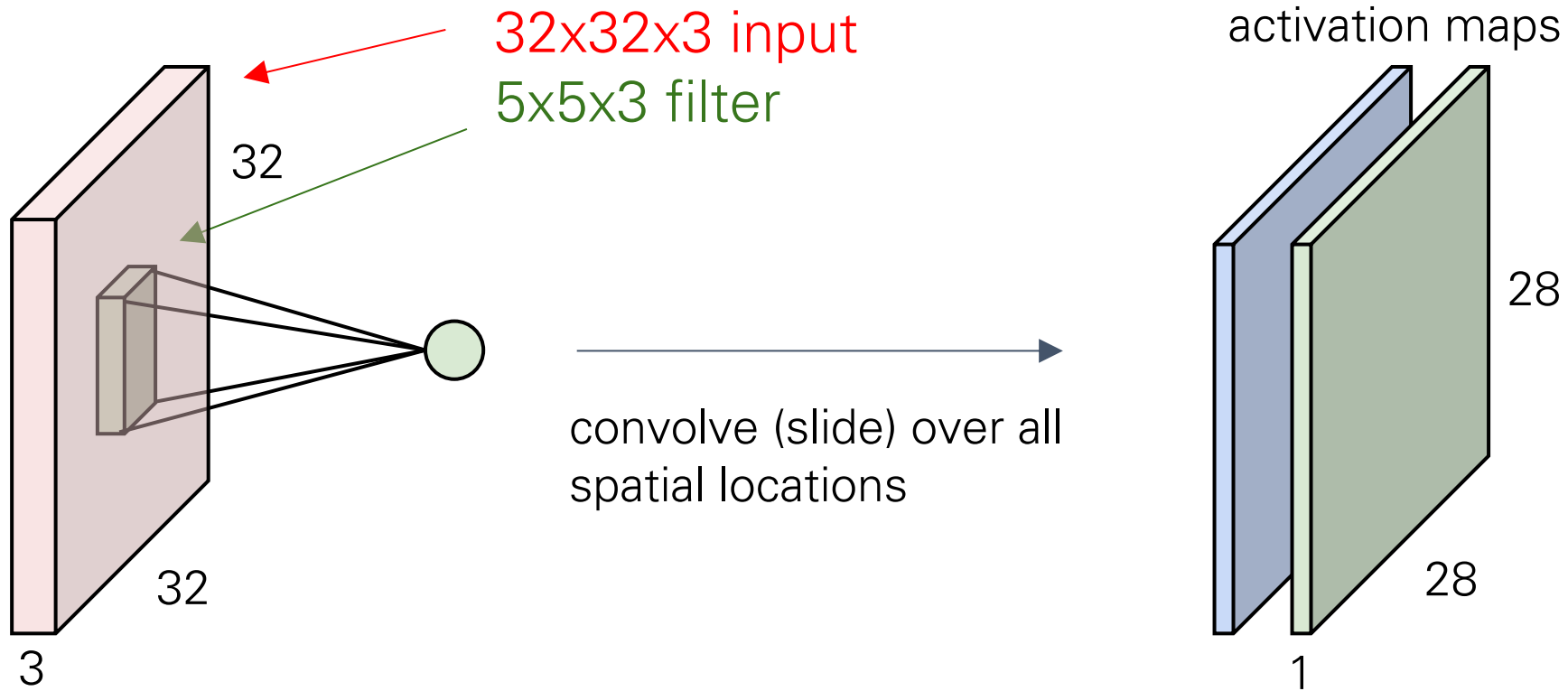


# Convolutional Layer



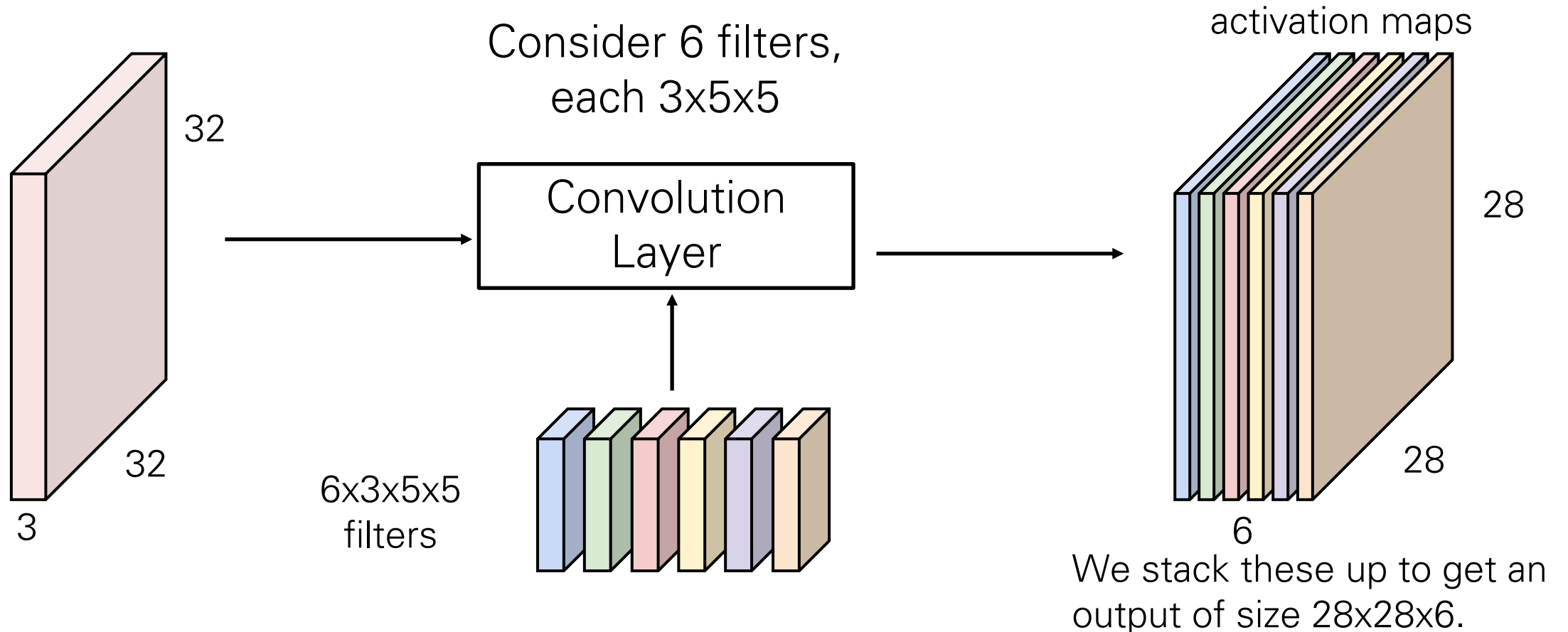
# Convolutional Layer

consider a second, **green** filter



# Convolutional Layer

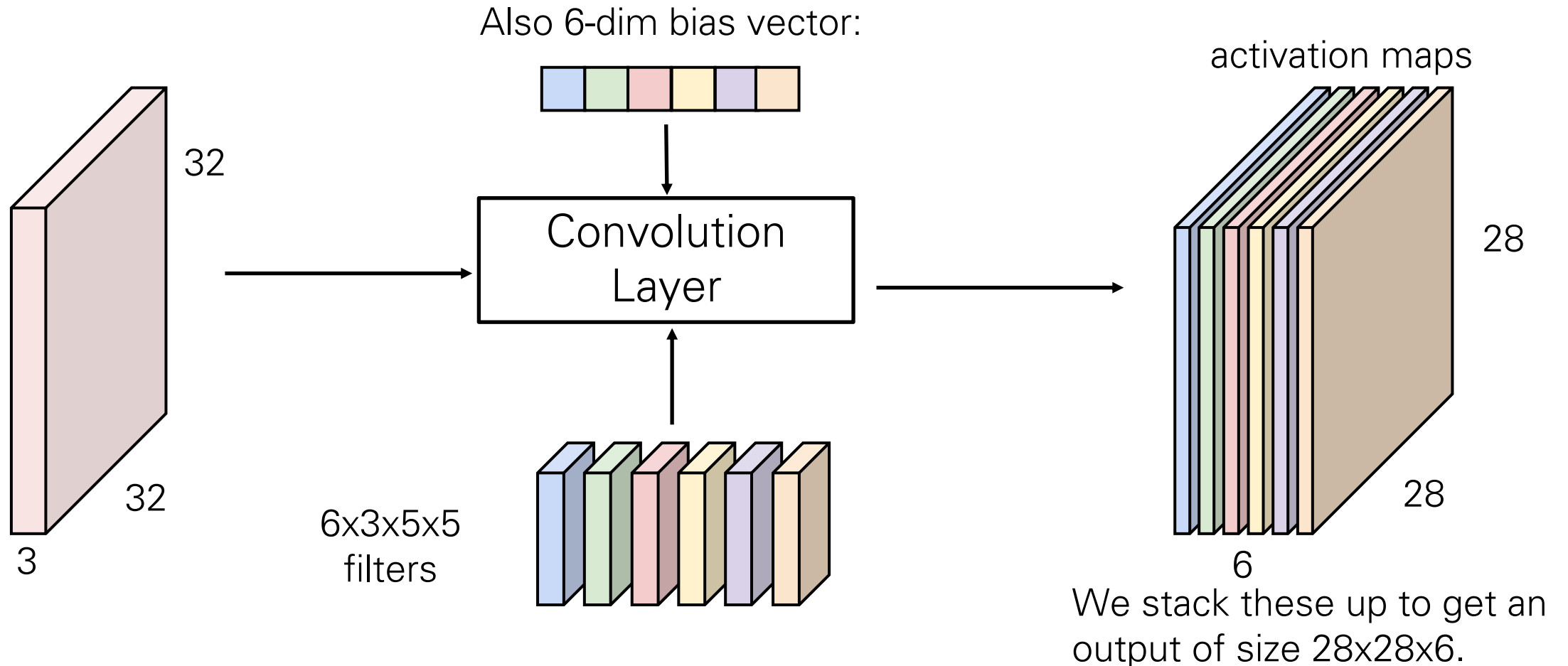
- Multiple filters produce multiple output channels





# Convolutional Layer

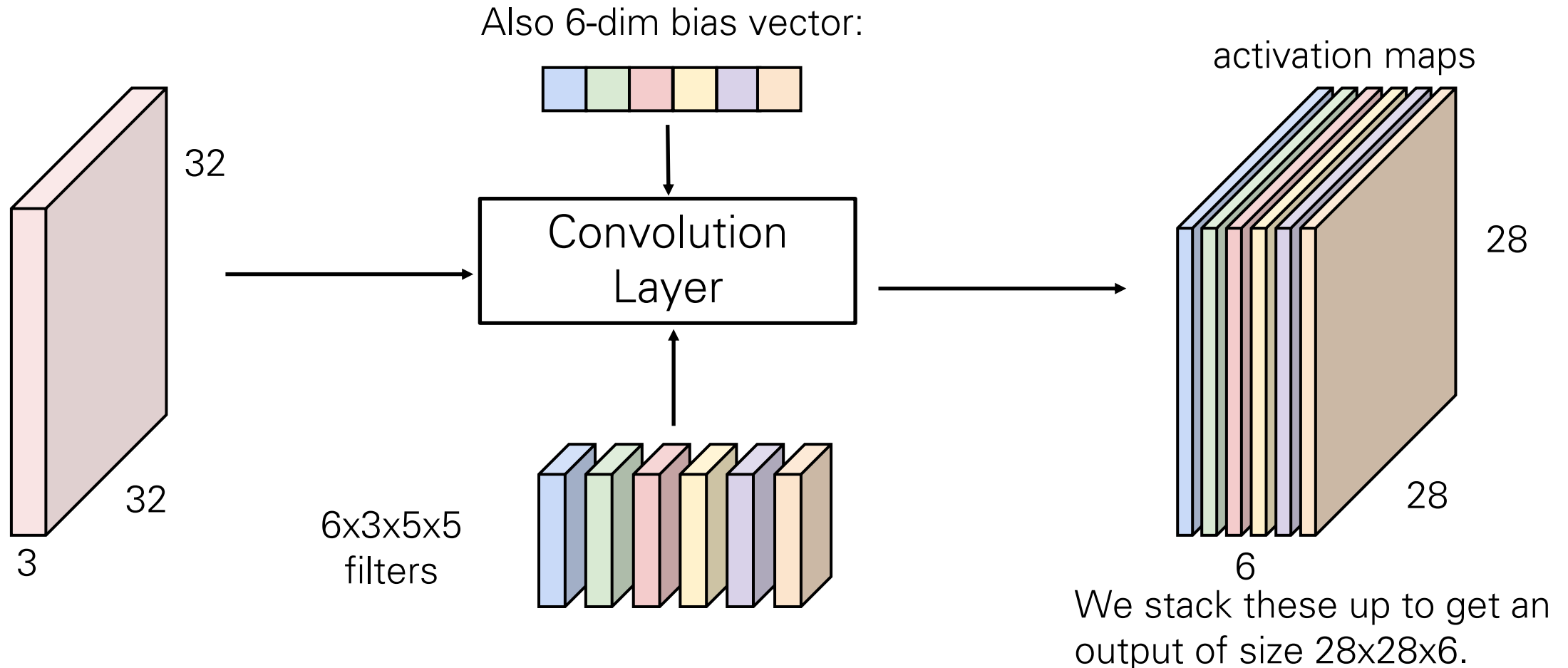
- Multiple filters produce multiple output channels



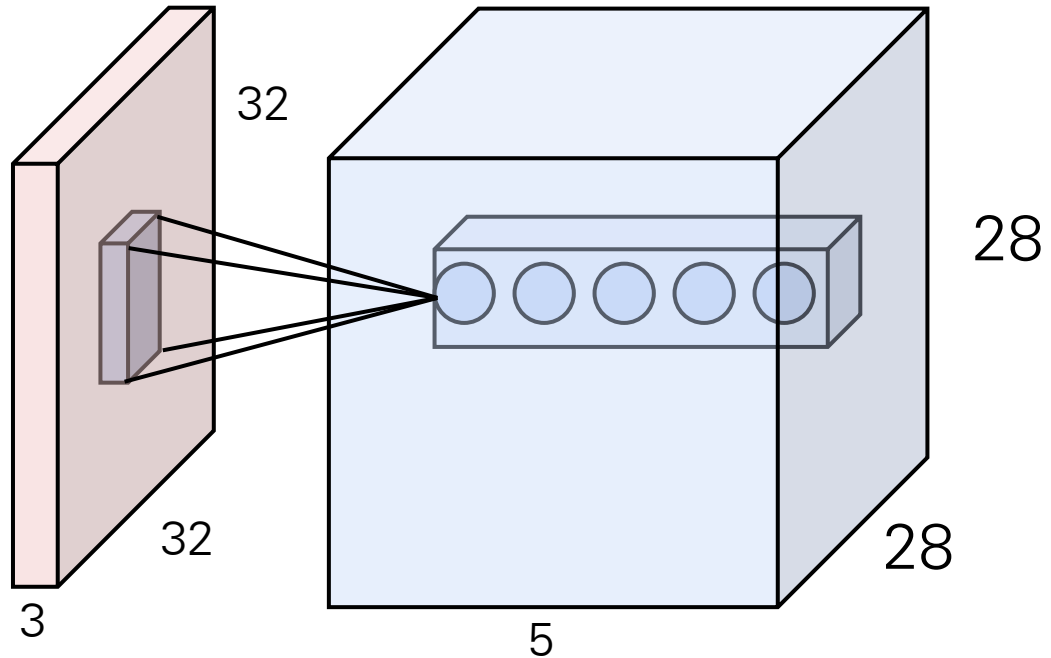
# Convolutional Layer

- Multiple filters produce multiple output channels

28x28 grid, at each point a 6-dim vector



# Spatial Arrangement of Output Volume



- **Depth:** number of filters
- **Stride:** filter step size (when we "slide" it)
- **Padding:** zero-pad the input

Input Volume (+pad 1) (7x7x3)

x[:, :, 0]						
0	0	0	0	0	0	0
0	1	2	0	0	0	0
0	2	2	0	0	0	0
0	2	2	2	1	0	0
0	1	0	0	2	0	0
0	1	1	0	1	0	0
0	0	0	0	0	0	0
x[:, :, 1]						
0	0	0	0	0	0	0
0	1	0	0	1	0	0
0	1	0	0	0	1	0
0	0	0	1	2	0	0
0	0	1	0	1	0	0
0	1	1	1	1	2	0
0	0	0	0	0	0	0
x[:, :, 2]						
0	0	0	0	0	0	0
0	0	0	2	2	2	0
0	1	2	2	2	0	0
0	1	1	1	1	0	0
0	1	2	0	0	0	0
0	2	2	2	1	0	0
0	0	0	0	0	0	0

Filter W0 (3x3x3)

w0[:, :, 0]		
0	0	-1
-1	0	0
-1	-1	-1
w0[:, :, 1]		
1	1	-1
0	0	0
-1	1	1
w0[:, :, 2]		
-1	-1	-1
0	1	1
0	-1	0
Bias b0 (1x1x1)		
b0[:, :, 0]		
1		

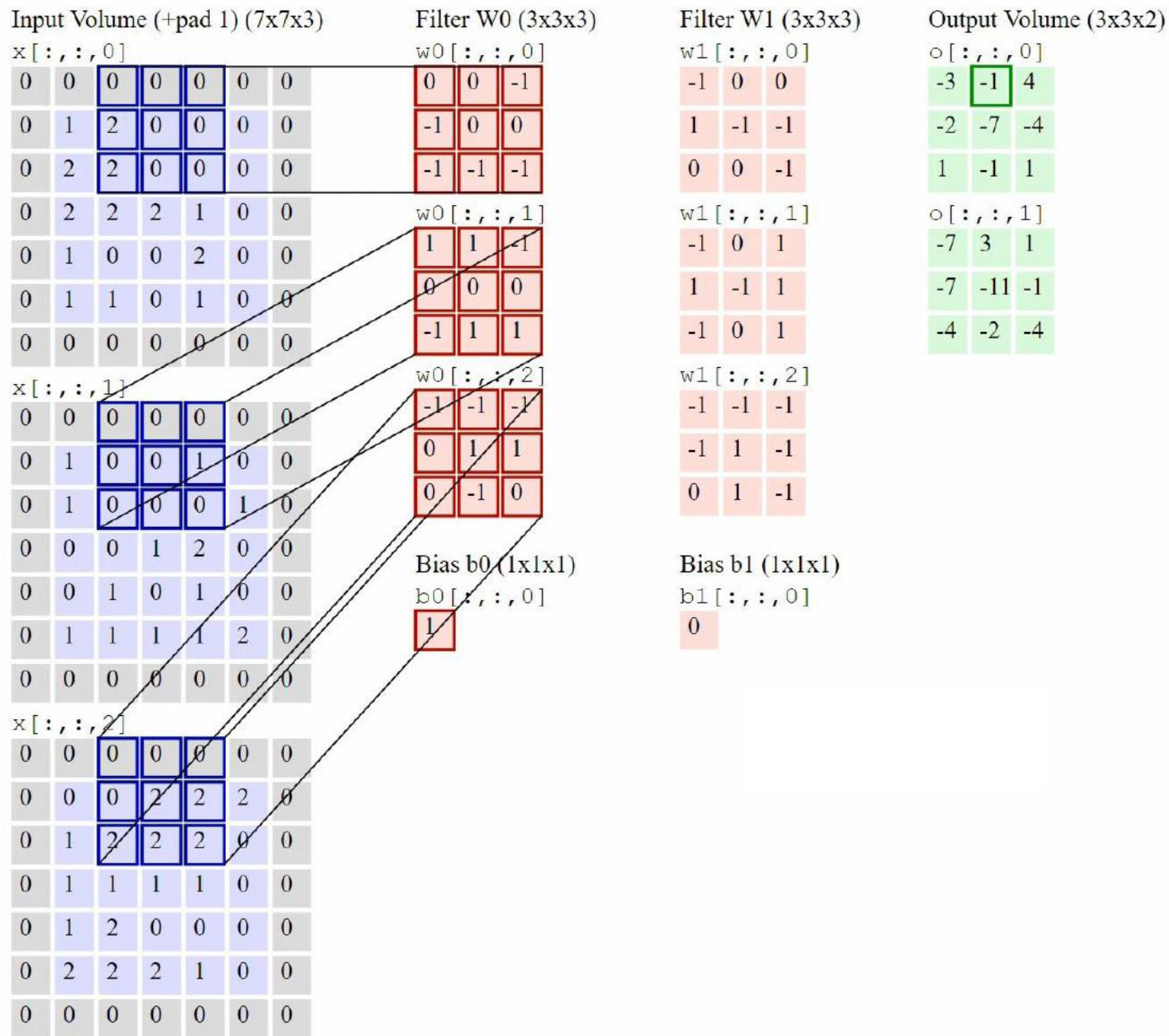
Filter W1 (3x3x3)

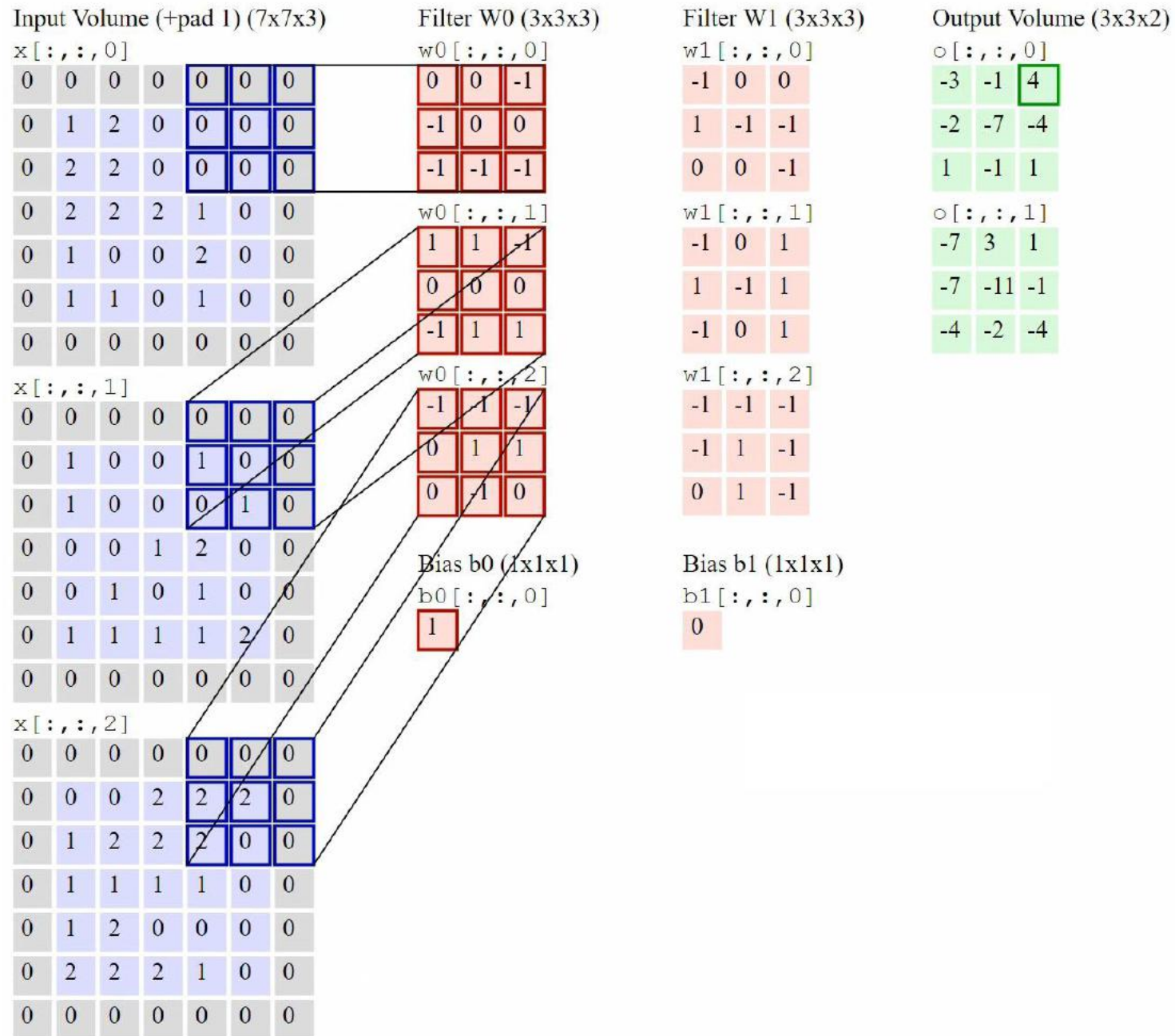
w1[:, :, 0]		
-1	0	0
1	-1	-1
0	0	-1
w1[:, :, 1]		
-1	0	1
1	-1	1
-1	0	1
w1[:, :, 2]		
-1	-1	-1
-1	1	-1
0	1	-1
Bias b1 (1x1x1)		
b1[:, :, 0]		
0		

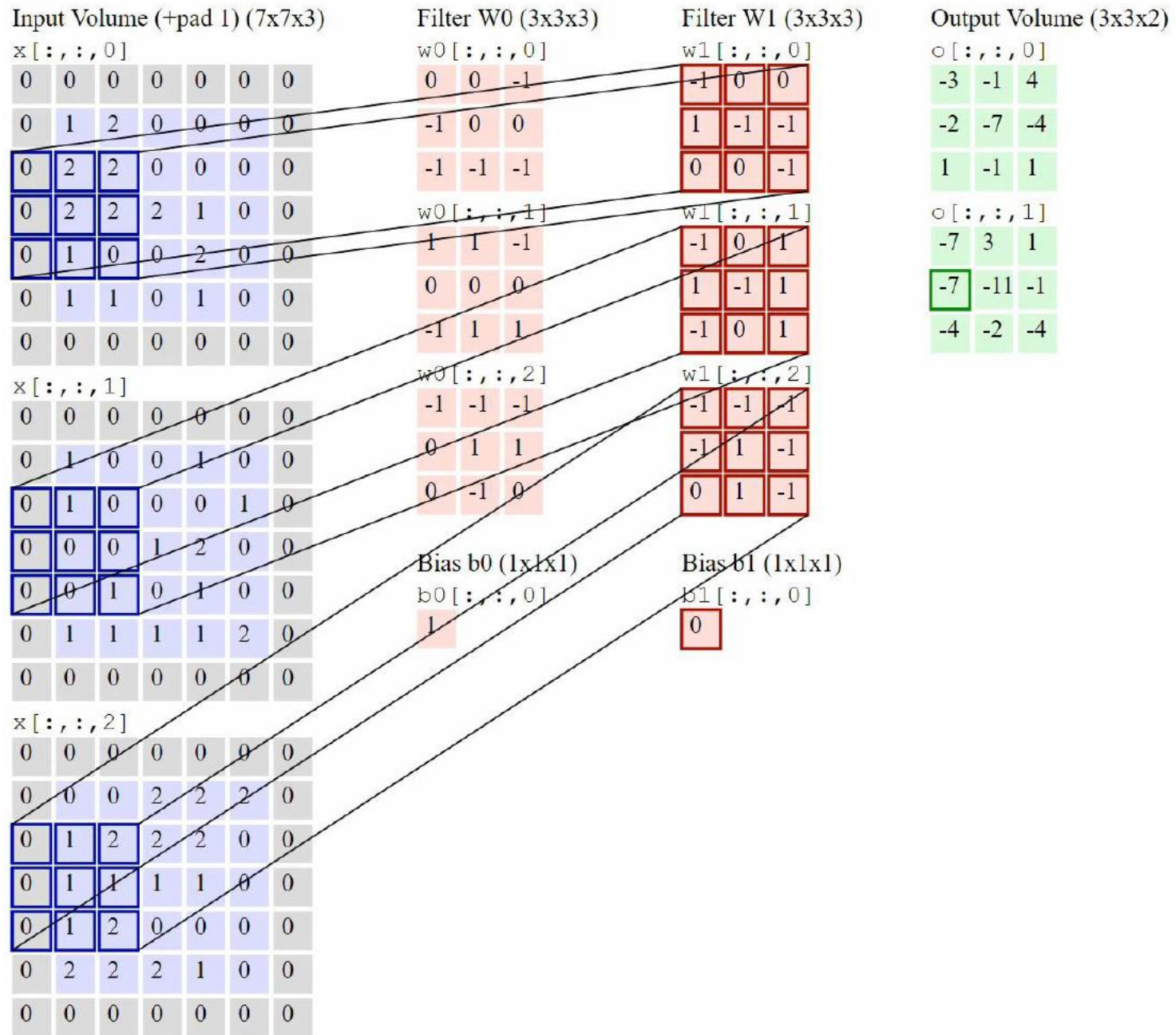
Output Volume (3x3x2)

o[:, :, 0]		
-3	-1	4
-2	-7	-4
1	-1	1
o[:, :, 1]		
-7	3	1
-7	-11	-1
-4	-2	-4

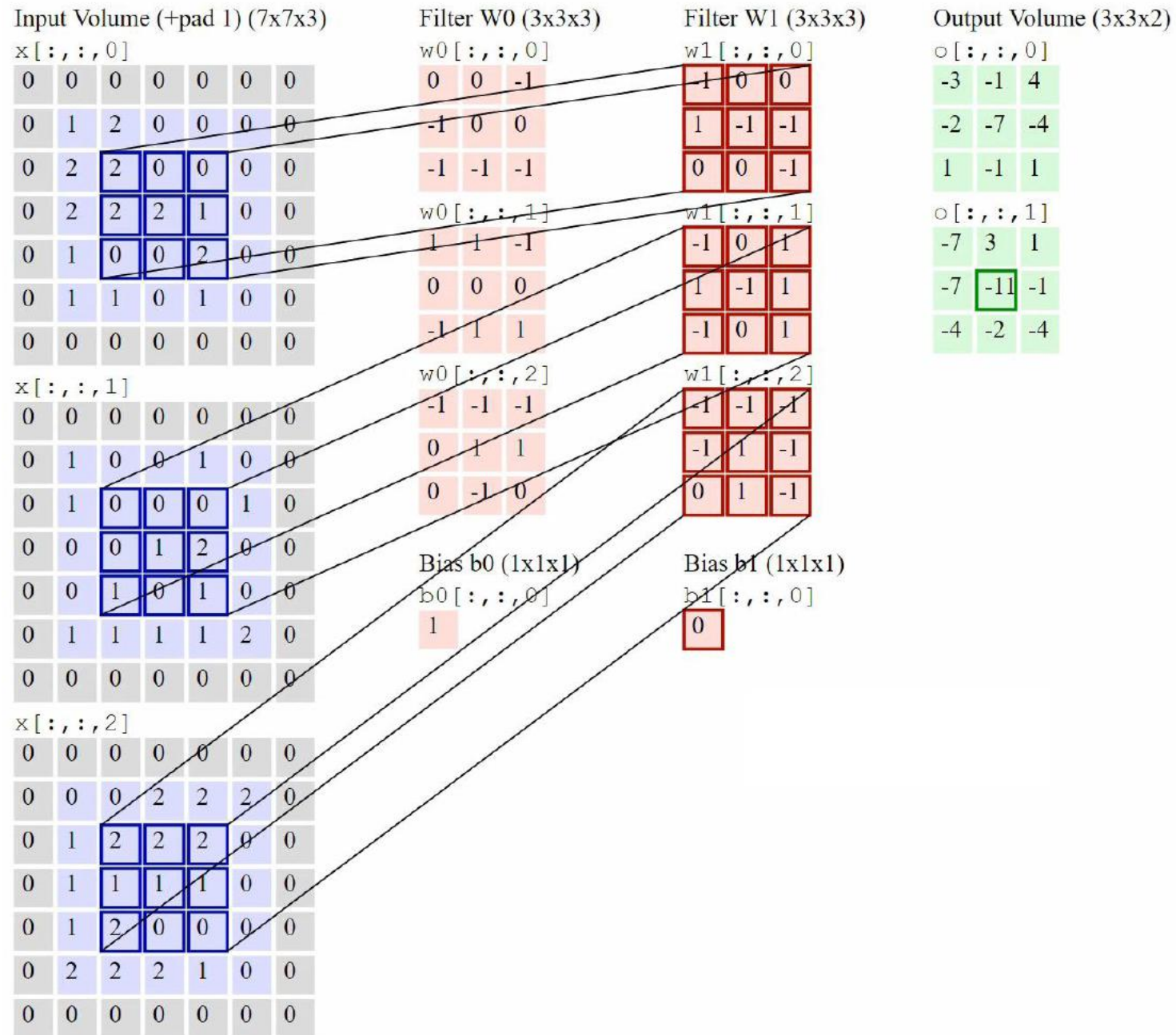


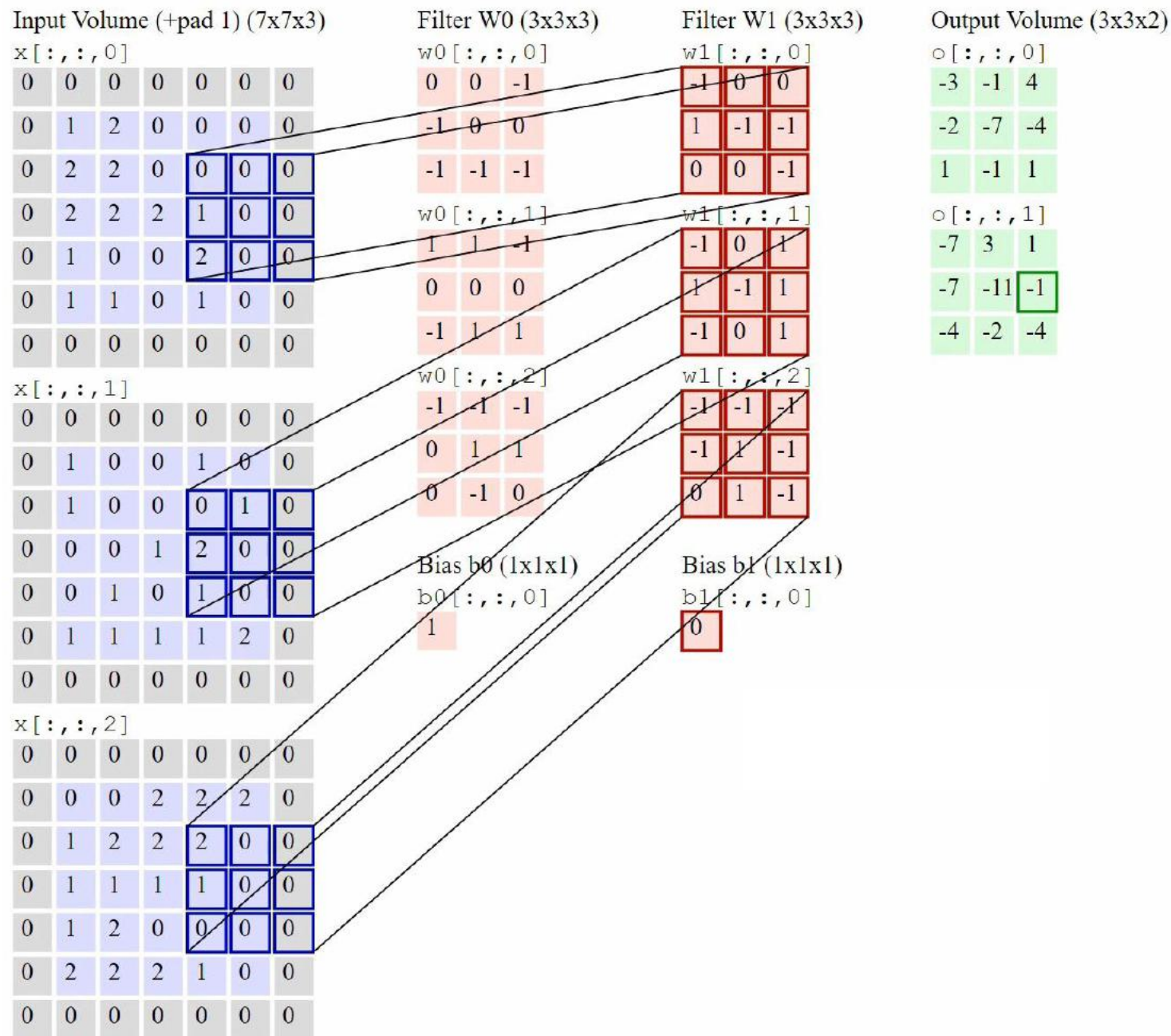




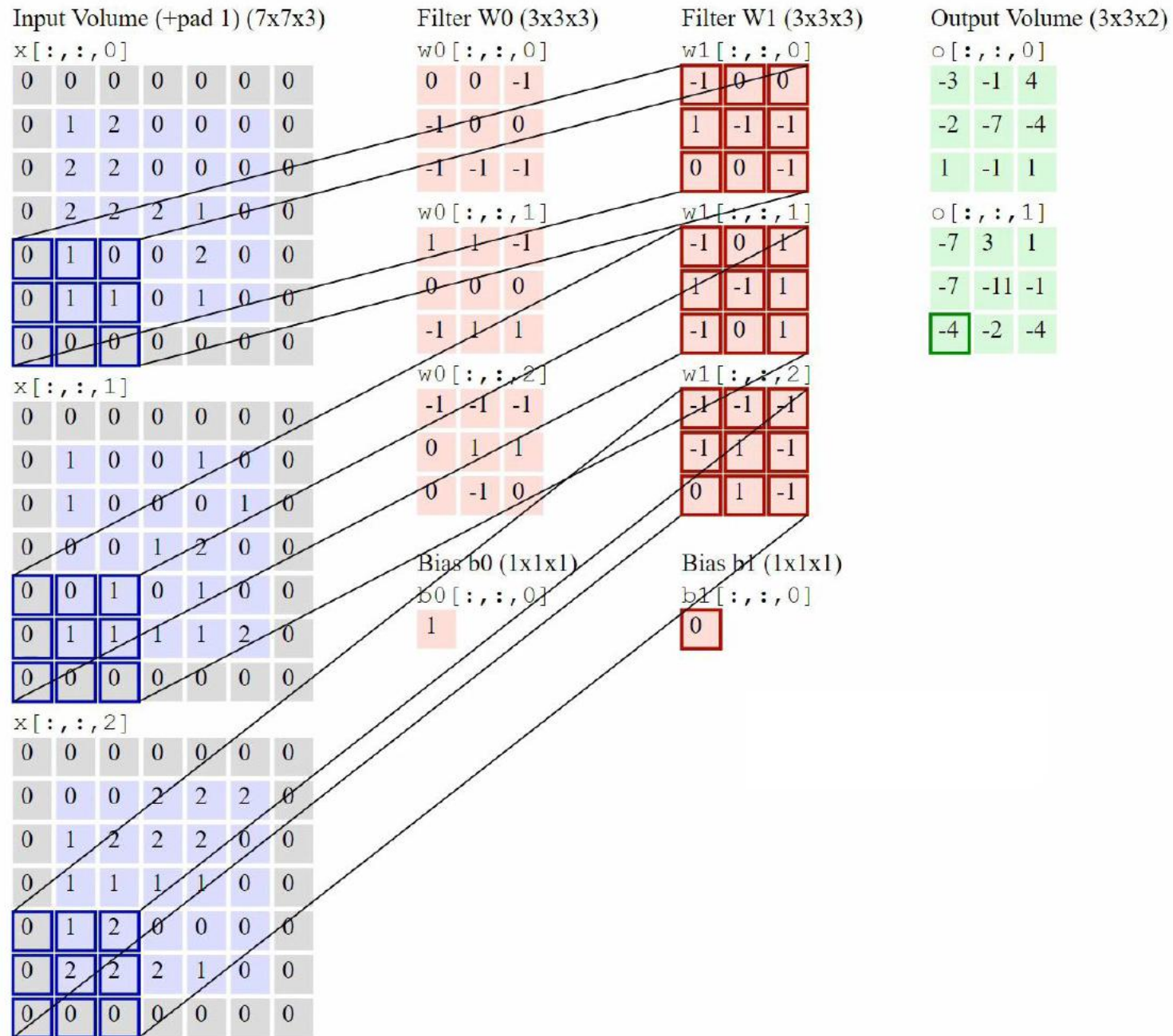


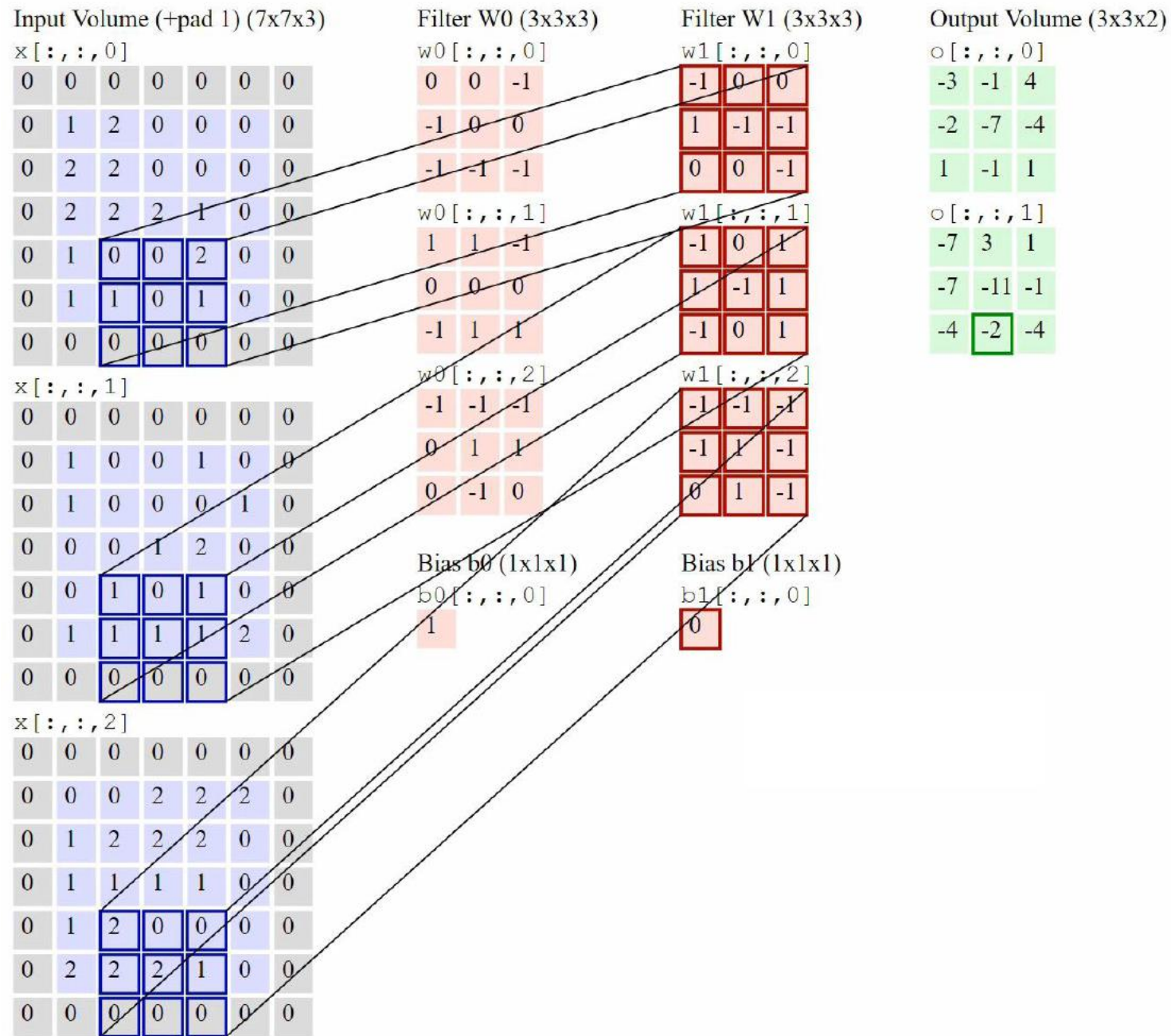


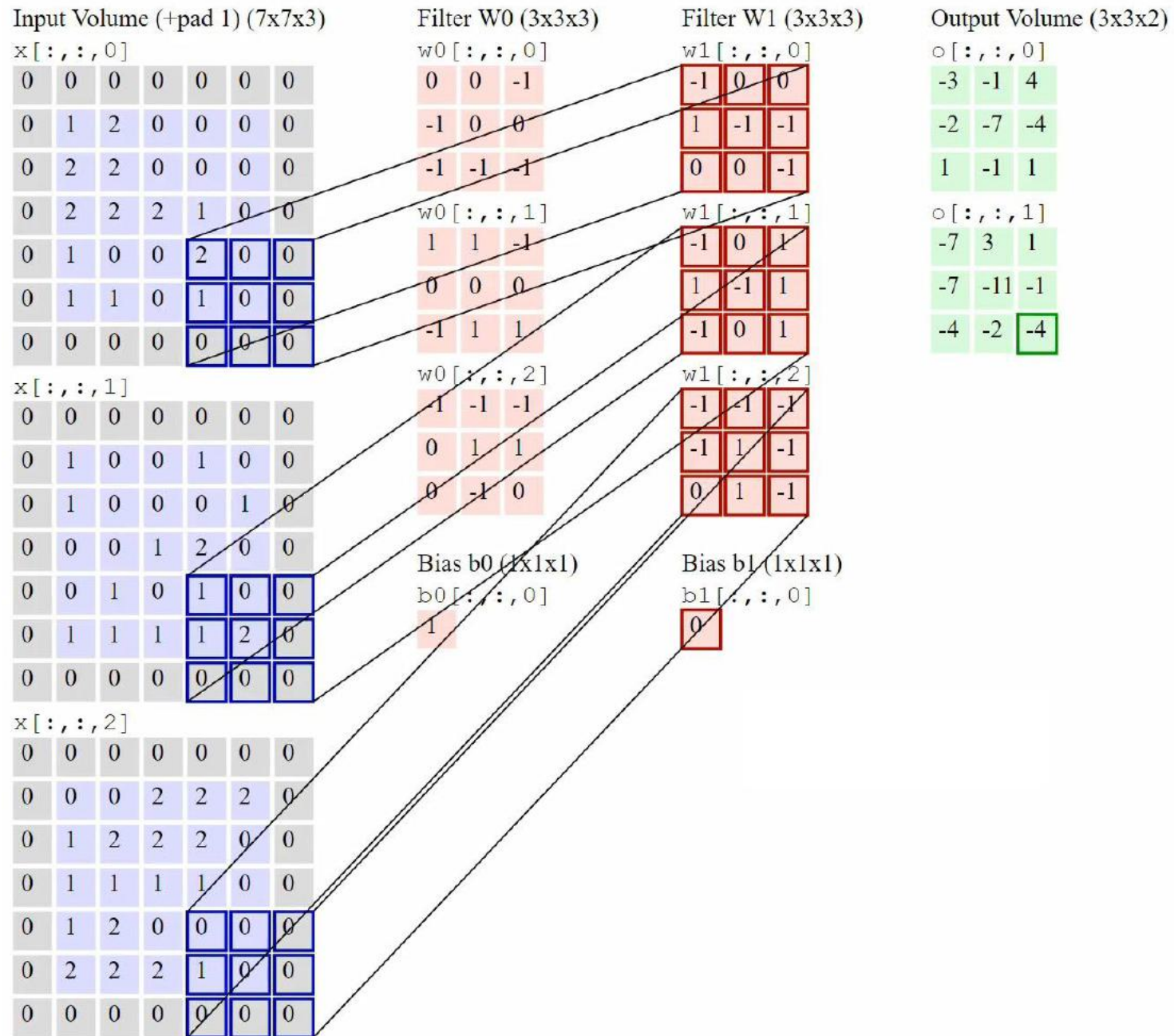






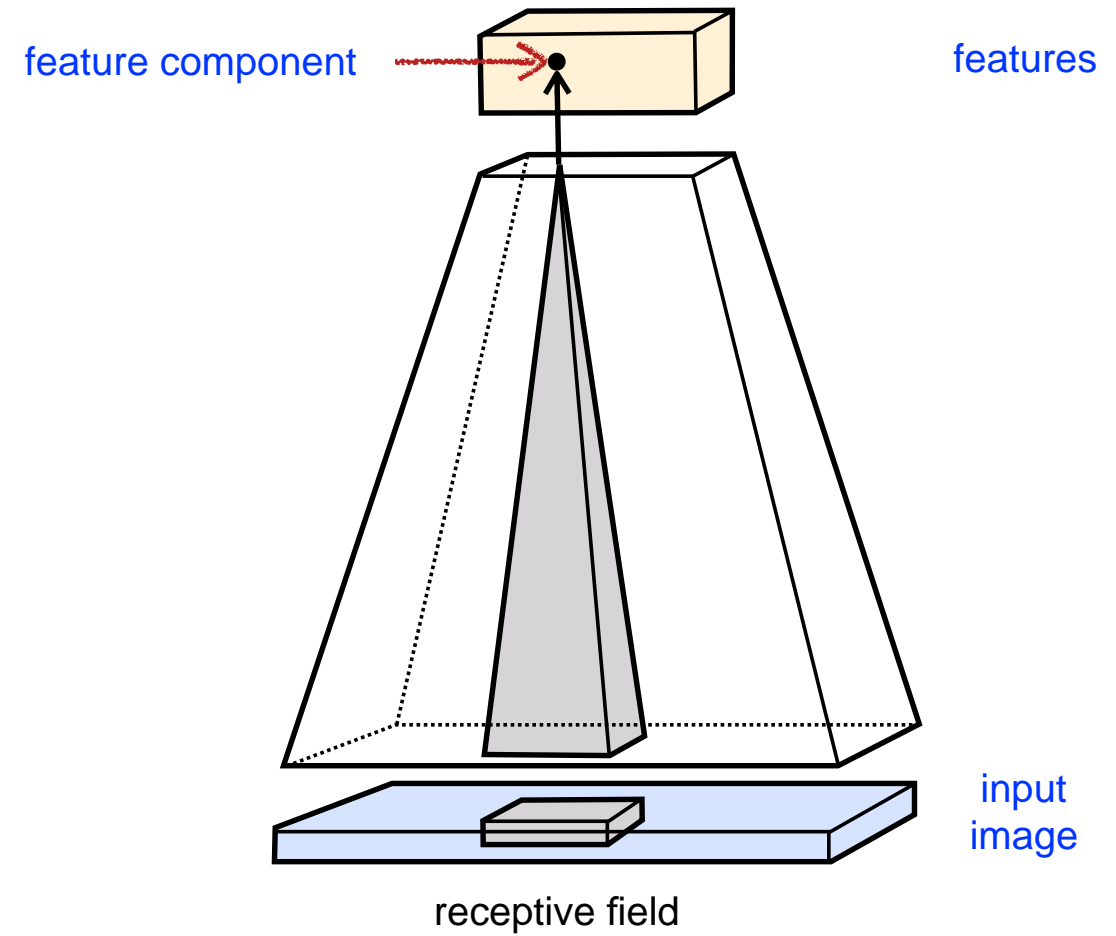






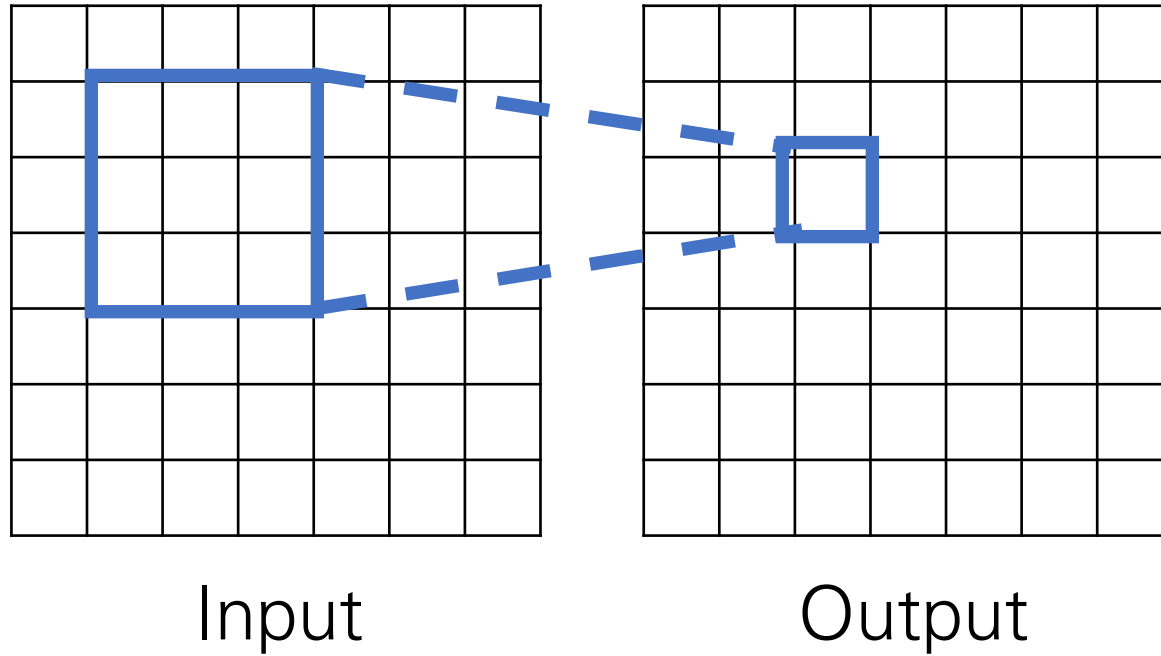
# Convolutional layers

- Local receptive field
- Each column of hidden units looks at a different input patch



# Receptive Fields

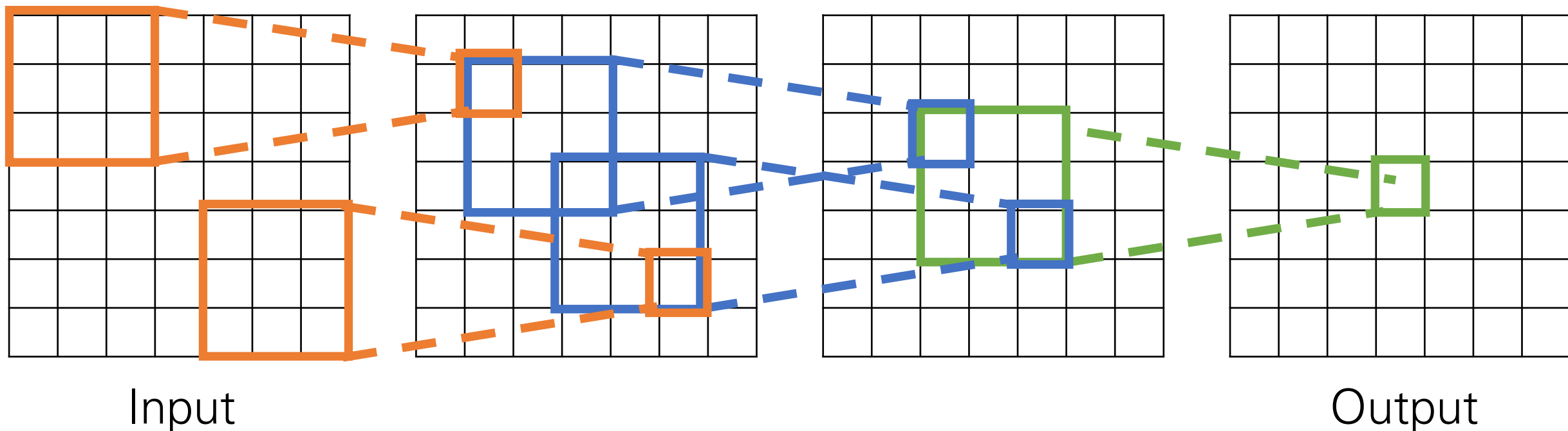
For convolution with kernel size  $K$ , each element in the output depends on a  $K \times K$  **receptive field** in the input





# Receptive Fields

Each successive convolution adds  $K - 1$  to the receptive field size  
With  $L$  layers the receptive field size is  $1 + L * (K - 1)$

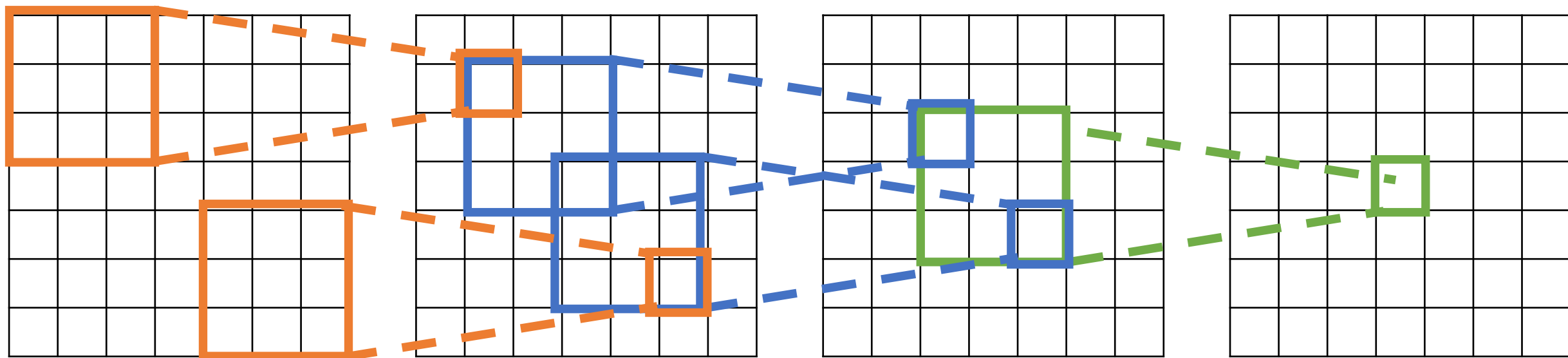


Be careful – “receptive field in the input” vs “receptive field in the previous layer”  
Hopefully clear from context!



# Receptive Fields

Each successive convolution adds  $K - 1$  to the receptive field size  
With  $L$  layers the receptive field size is  $1 + L * (K - 1)$



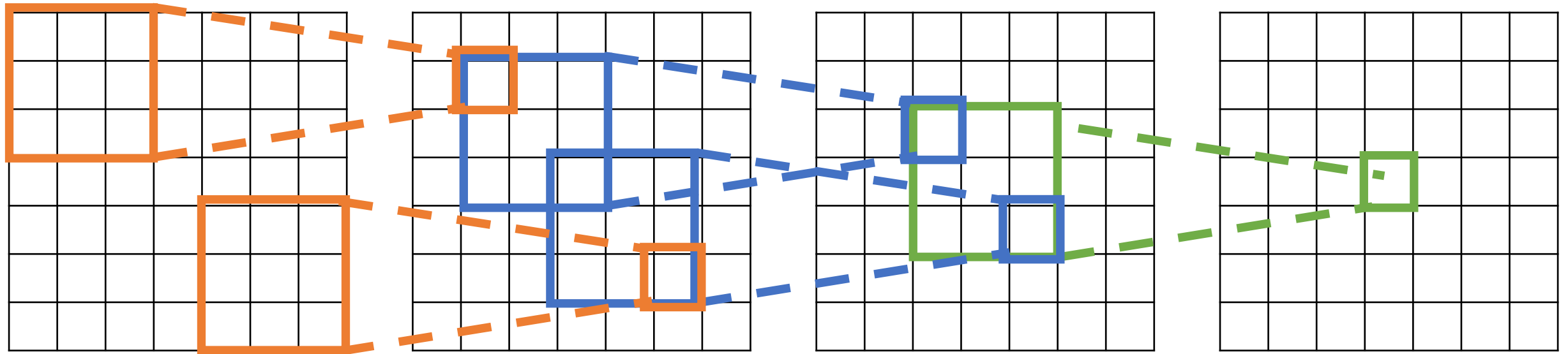
Input

**Problem:** For large images we need many layers for each output to "see" the whole image

Output

# Receptive Fields

Each successive convolution adds  $K - 1$  to the receptive field size  
With  $L$  layers the receptive field size is  $1 + L * (K - 1)$



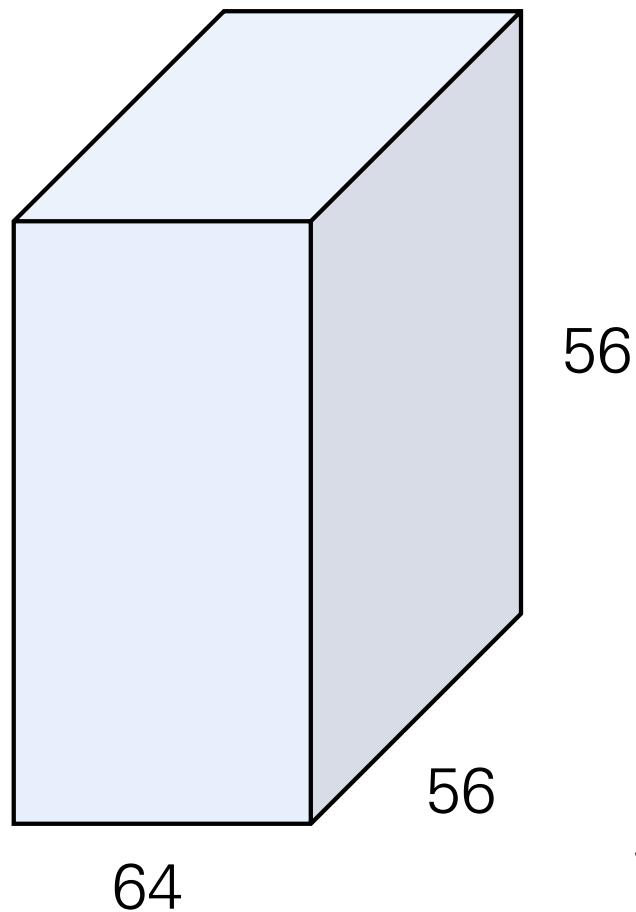
Input

**Problem:** For large images we need many layers for each output to “see” the whole image

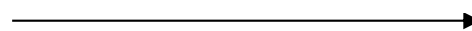
**Solution:** Downsample inside the network

Output

# 1x1 Convolution

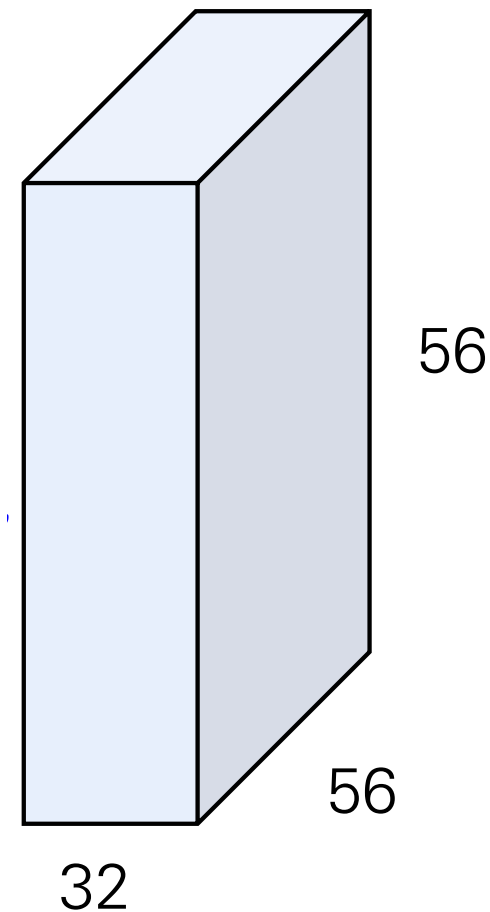


1x1 CONV  
with 32 filters



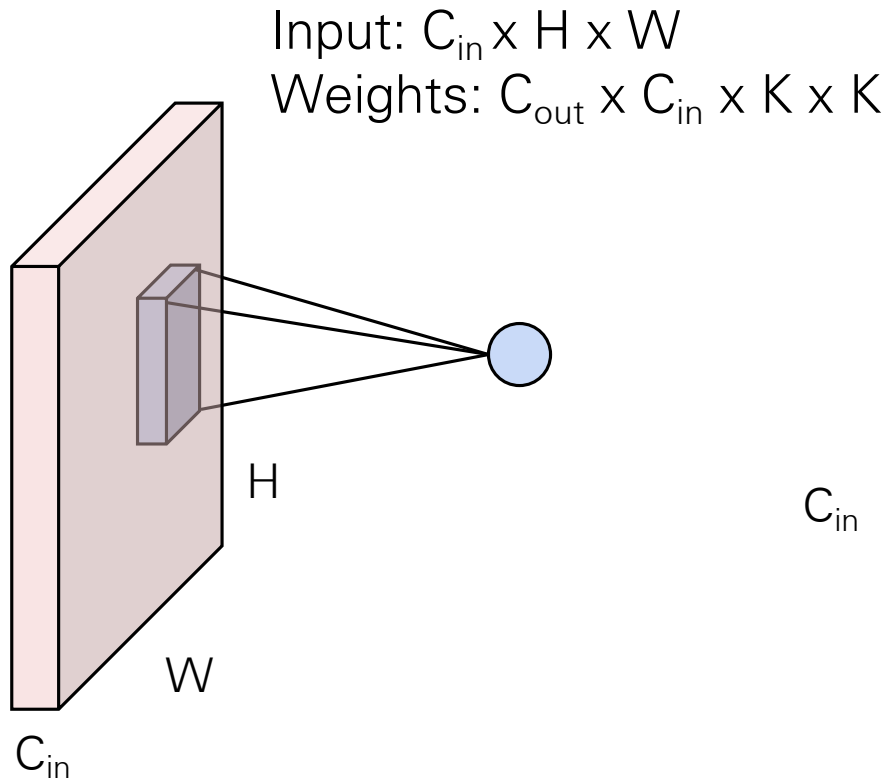
(each filter has size 64x1x1,  
and performs a 64-dimensional  
dot product)

Stacking 1x1 conv layers  
gives MLP operating on  
each input position



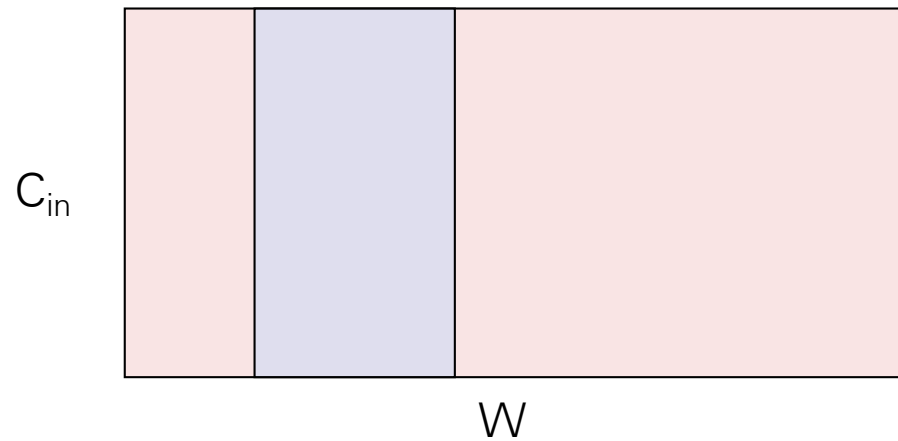
# Other types of convolution

## So far: 2D Convolution



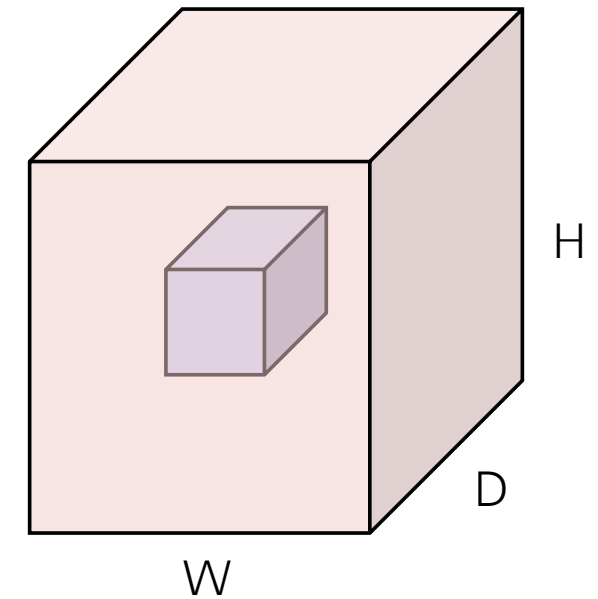
## 1D Convolution

Input:  $C_{in} \times W$   
Weights:  $C_{out} \times C_{in} \times K$



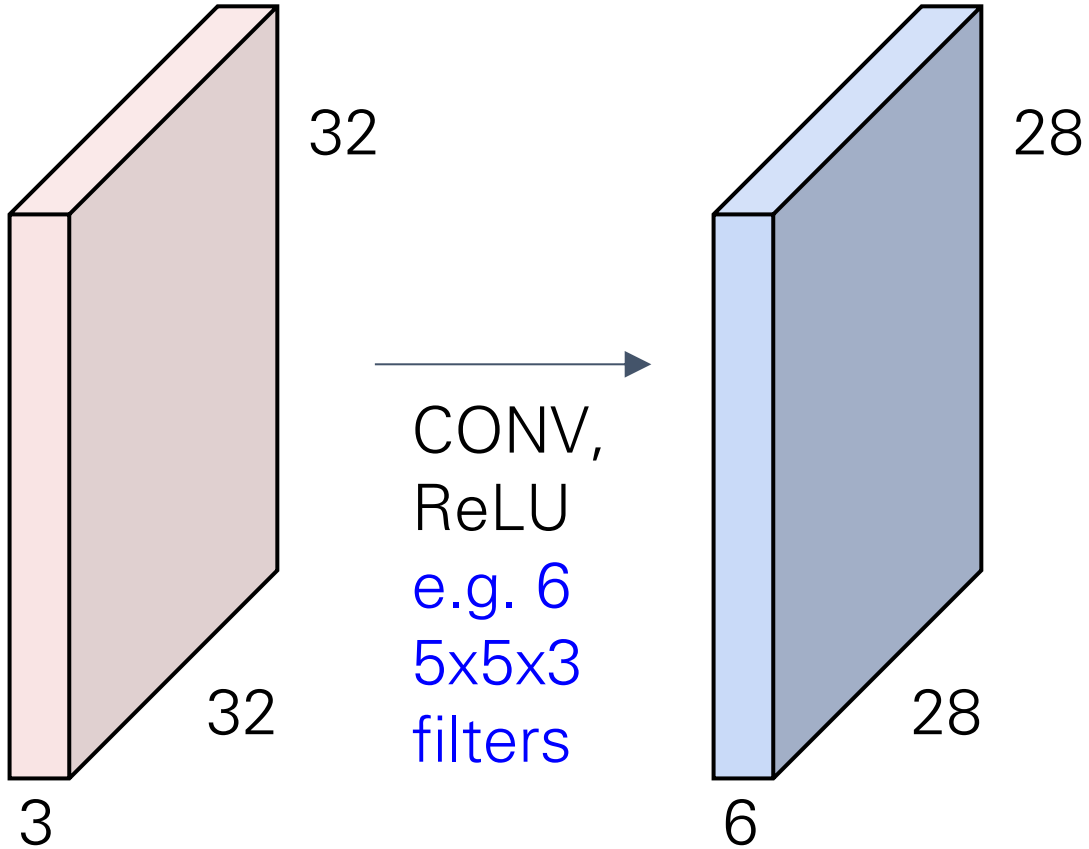
## 3D Convolution

Input:  $C_{in} \times H \times W \times D$   
Weights:  $C_{out} \times C_{in} \times K \times K \times K$

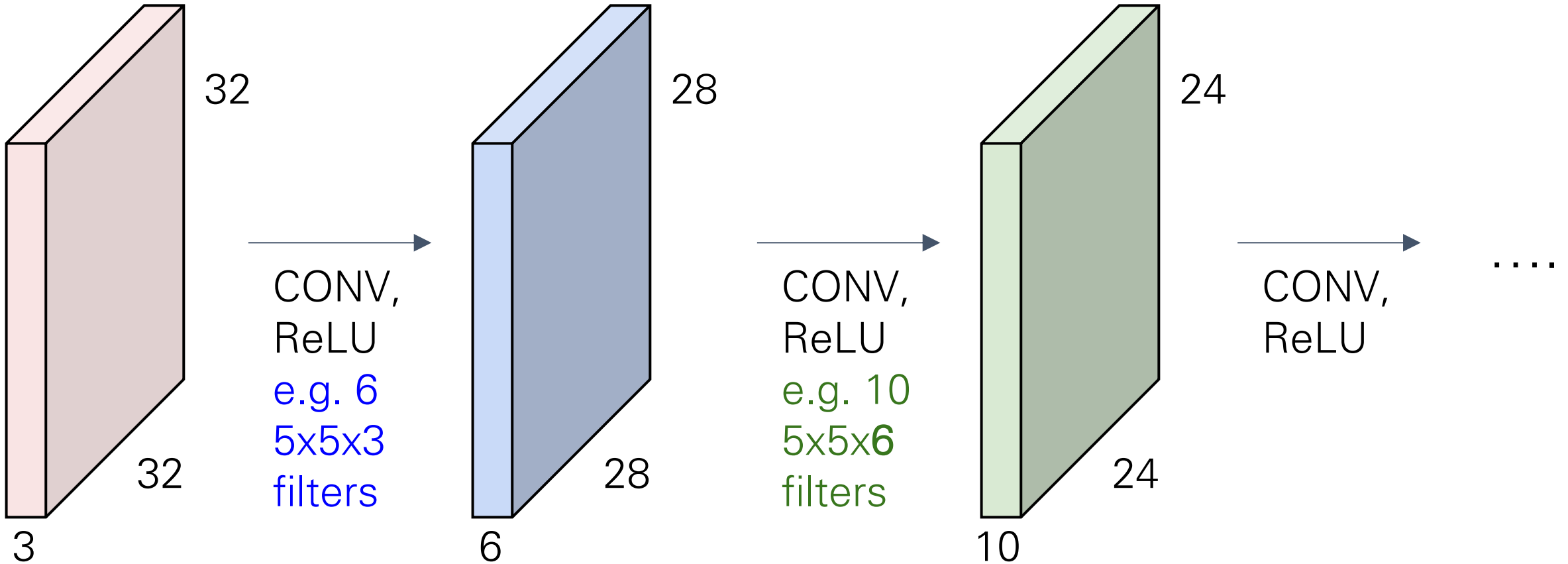


$C_{in}$ -dim vector at each point in the volume

# Convolutional layers



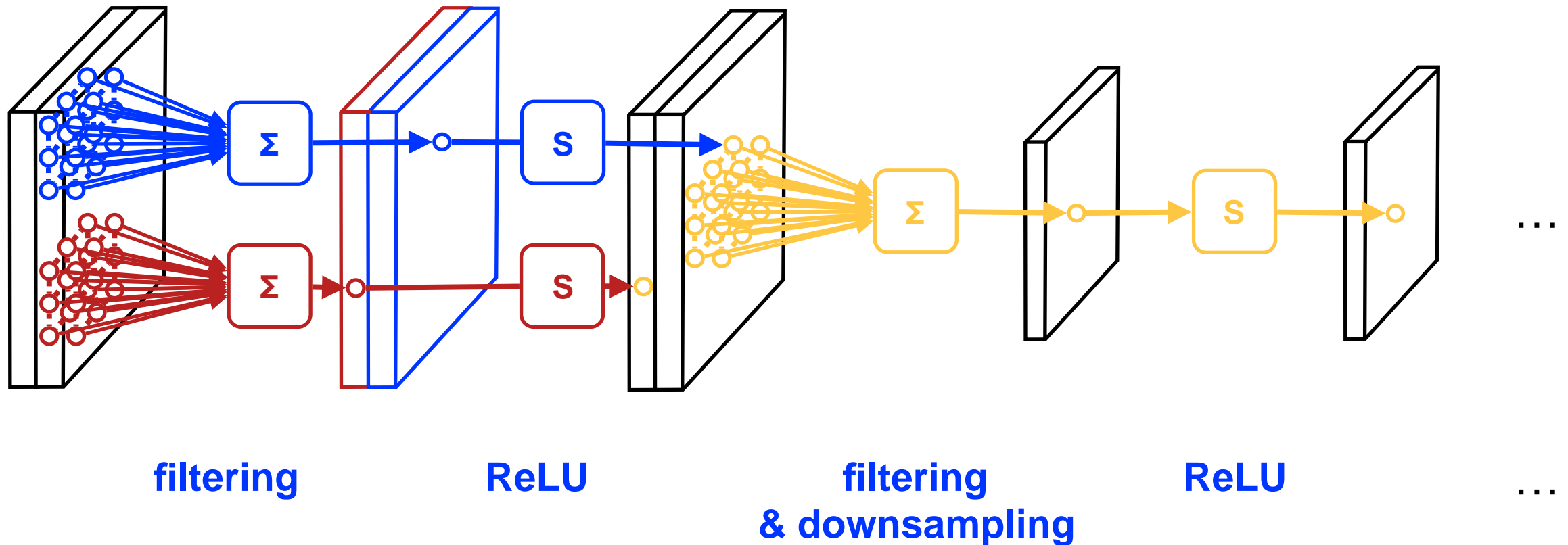
# Stacking Convolutions





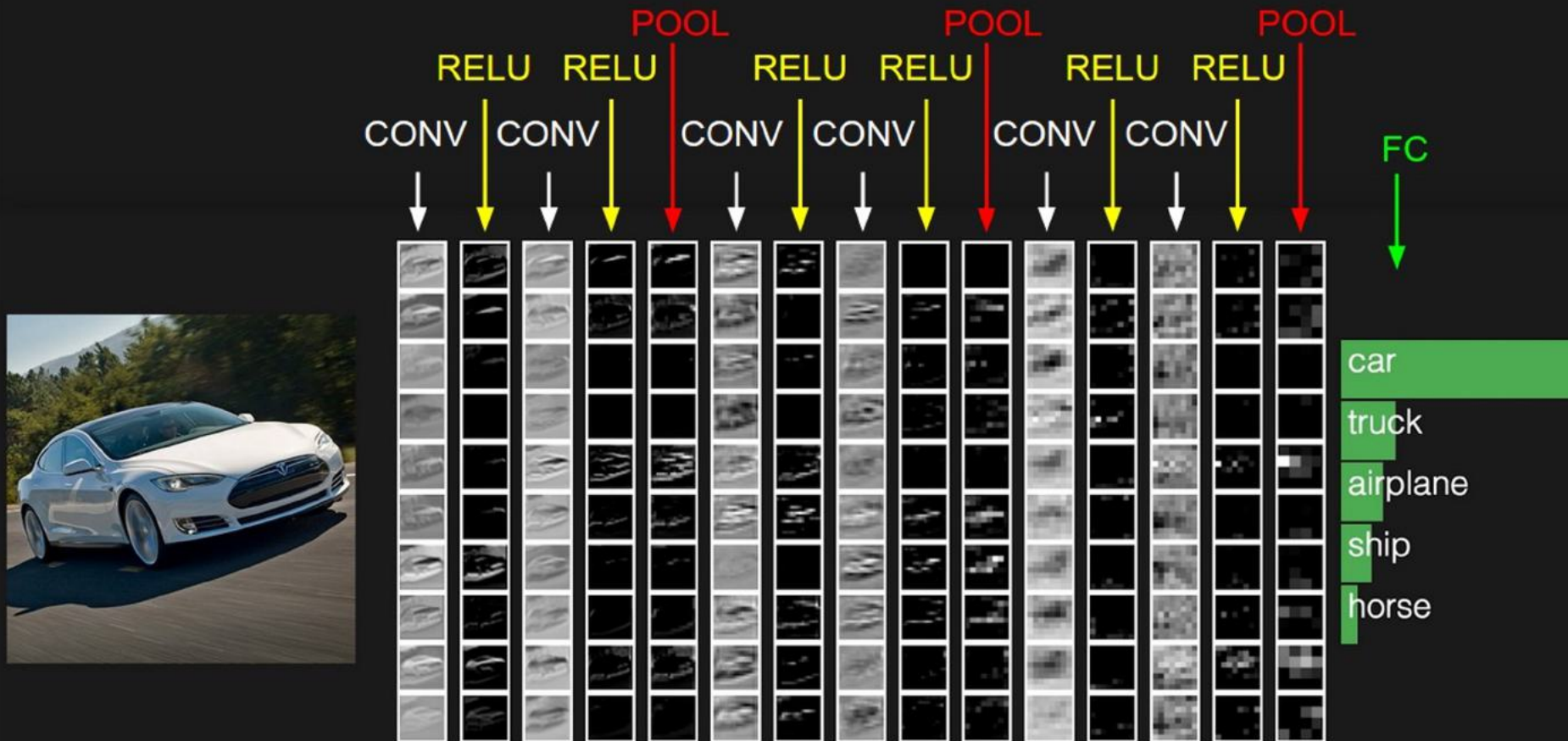
# Linear/Non-linear Chains

- The basic blueprint of most architectures
- Stack multiple layers of convolutions



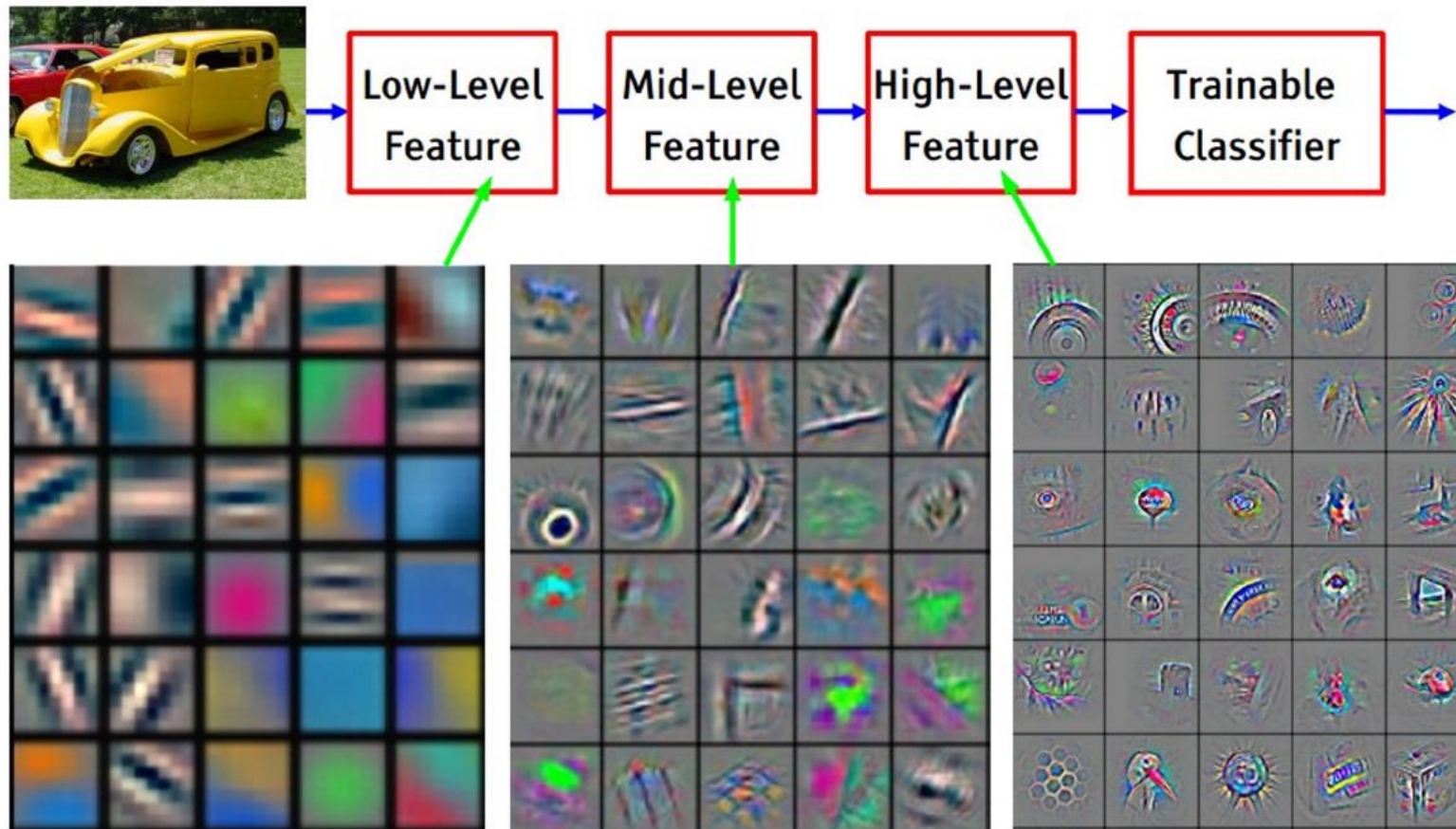
# Feature Learning

- Hierarchical layer structure allows to learn hierarchical filters (features).



# Feature Learning

- Hierarchical layer structure allows to learn hierarchical filters (features).



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

# Pooling layer

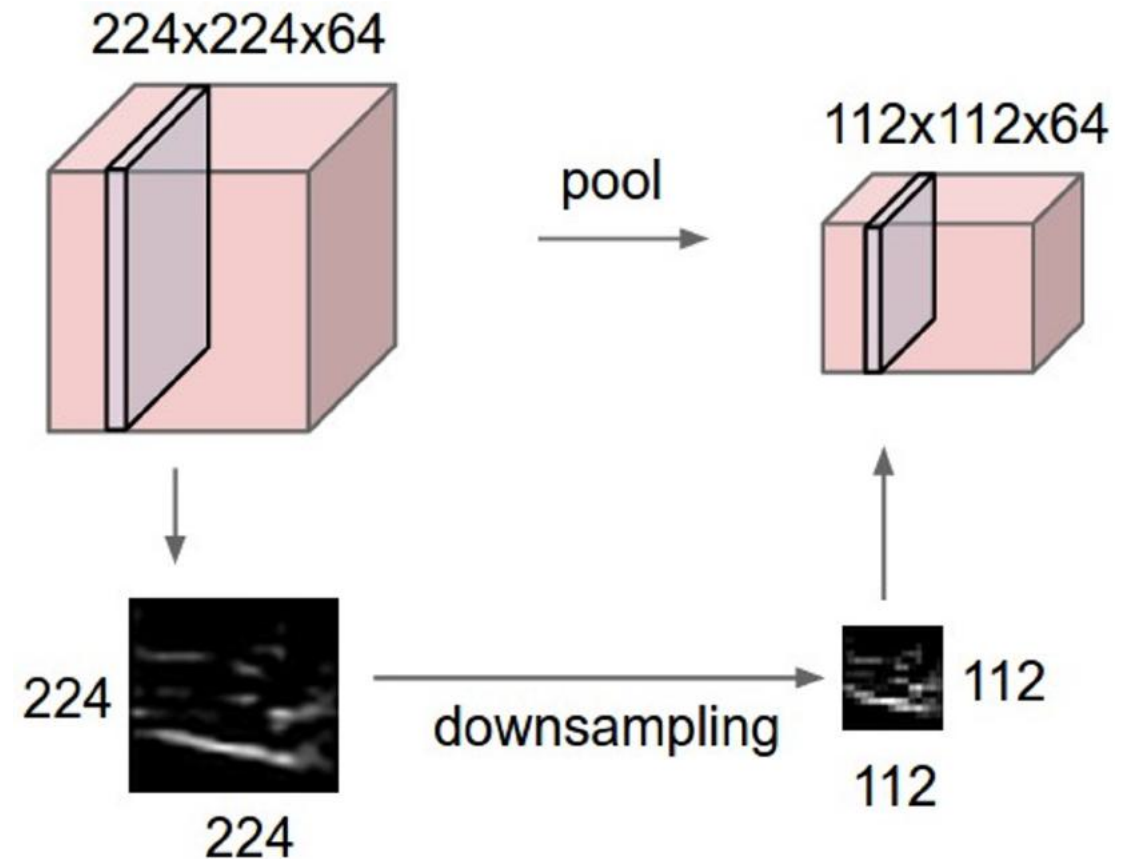
- makes the representations smaller and more manageable
- operates over each activation map independently:
- Max pooling, average pooling, etc.

Single depth slice

1	1	2	4
5	6	7	8
3	2	1	0
1	2	3	4

max pool with 2x2 filters and stride 2

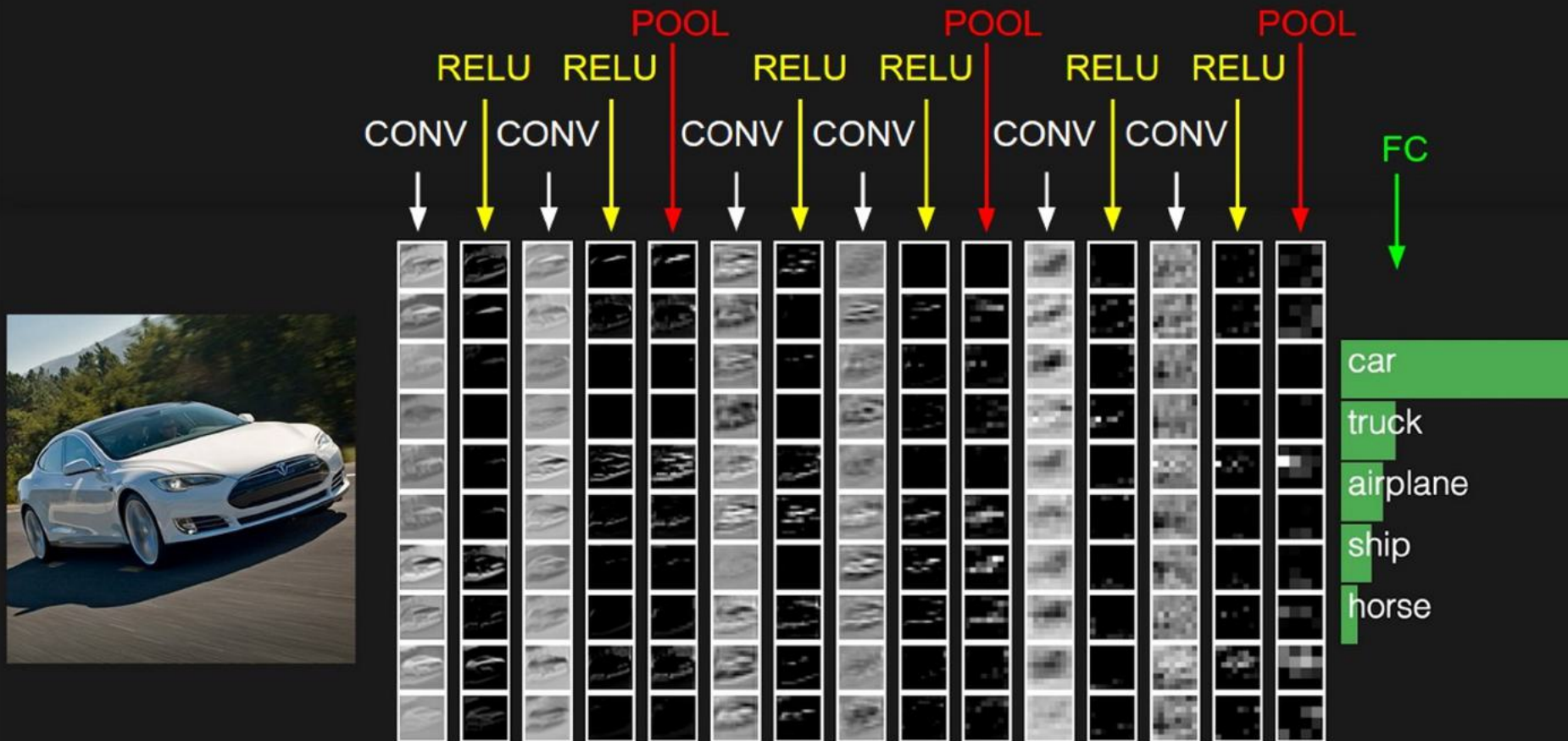
6	8
3	4





# Fully connected layer

- contains neurons that connect to the entire input volume, as in ordinary Neural Networks



# Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture:

[227x227x3] INPUT

[55x55x96] **CONV1**: 96 11x11 filters at stride 4, pad 0

[27x27x96] **MAX POOL1**: 3x3 filters at stride 2

[27x27x96] **NORM1**: Normalization layer

[27x27x256] **CONV2**: 256 5x5 filters at stride 1, pad 2

[13x13x256] **MAX POOL2**: 3x3 filters at stride 2

[13x13x256] **NORM2**: Normalization layer

[13x13x384] **CONV3**: 384 3x3 filters at stride 1, pad 1

[13x13x384] **CONV4**: 384 3x3 filters at stride 1, pad 1

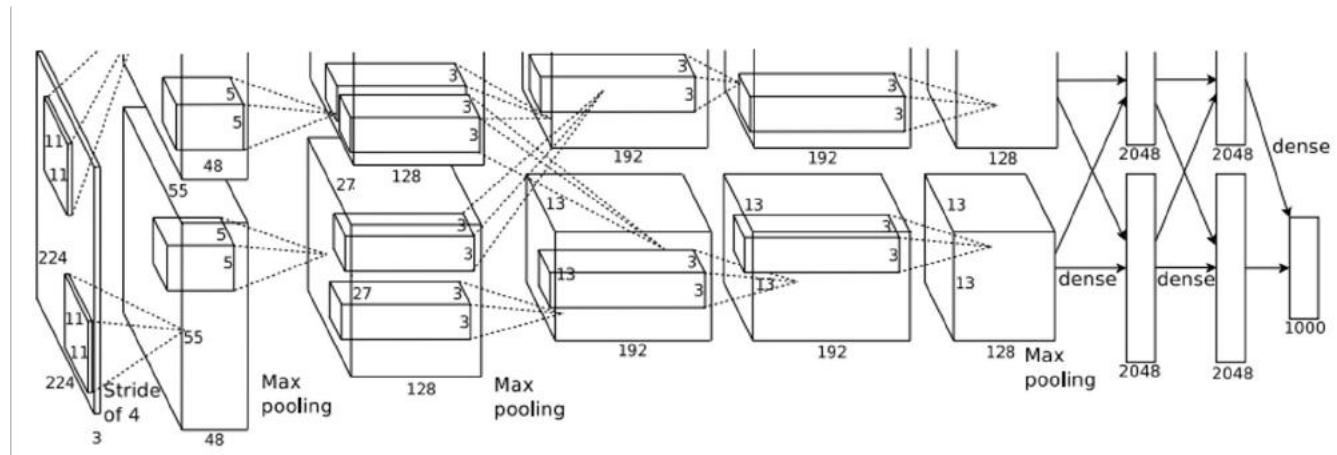
[13x13x256] **CONV5**: 256 3x3 filters at stride 1, pad 1

[6x6x256] **MAX POOL3**: 3x3 filters at stride 2

[4096] **FC6**: 4096 neurons

[4096] **FC7**: 4096 neurons

[1000] **FC8**: 1000 neurons (class scores)



## Details/Retrospectives:

- first use of ReLU
- used Norm layers (not common anymore)
- heavy data augmentation
- dropout 0.5
- batch size 128
- SGD Momentum 0.9
- Learning rate 1e-2, reduced by 10 manually when val accuracy plateaus
- L2 weight decay 5e-4
- 7 CNN ensemble: 18.2% -> 15.4%

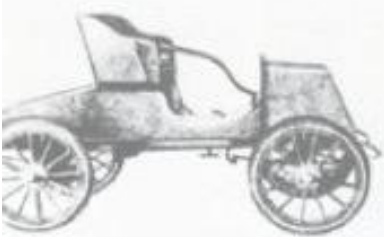


# Convolutional Neural Network Demo

- ConvNetJS demo: training on CIFAR-10
- <https://cs.stanford.edu/people/karpathy/convnetjs/demo/cifar10.html>

# Three Years of Progress

## From AlexNet (2012) to ResNet (2015)



1903



1904



1906



1907



1909



1913



1915



1918



1920



1924



1926



1927



1929

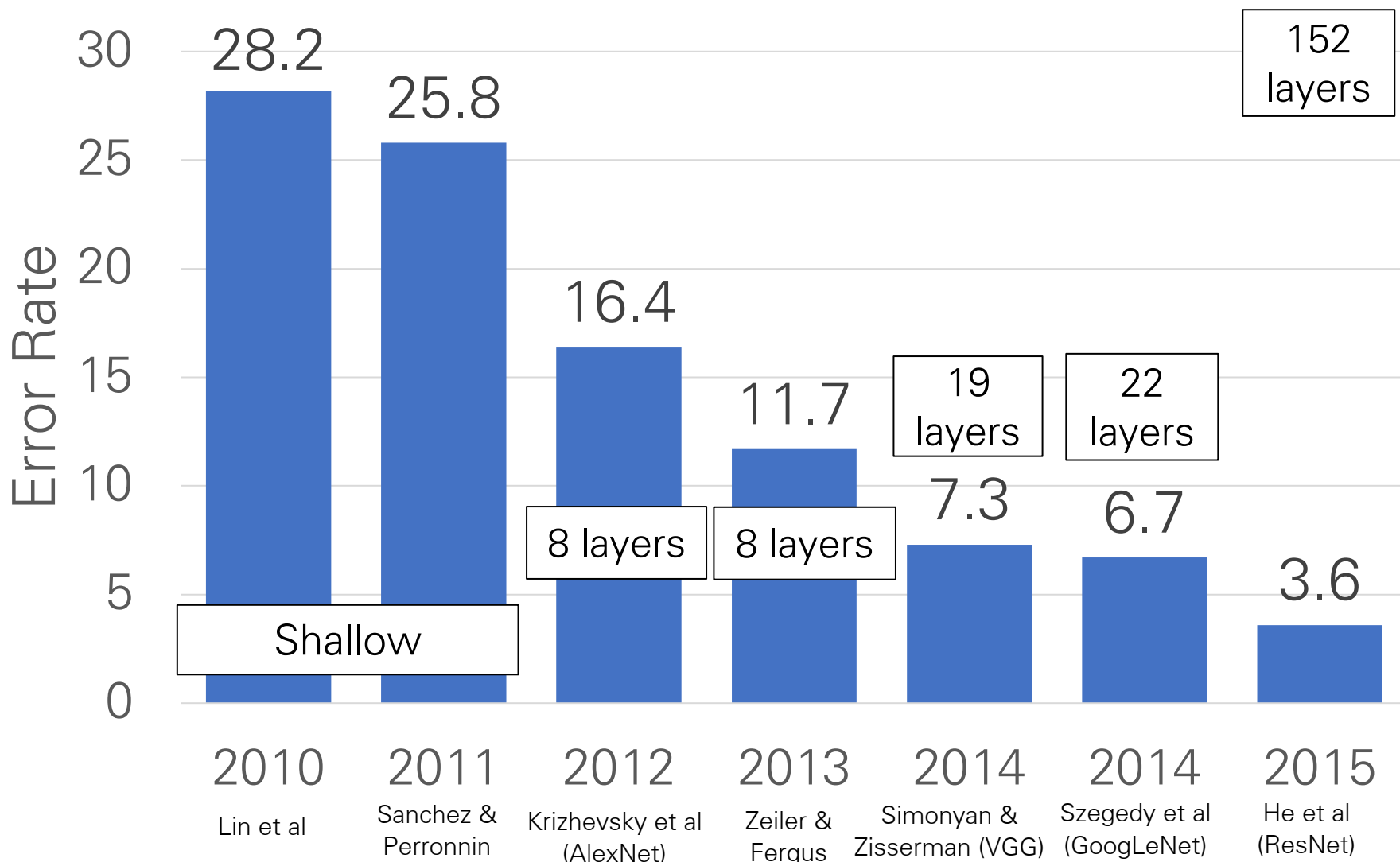


1932



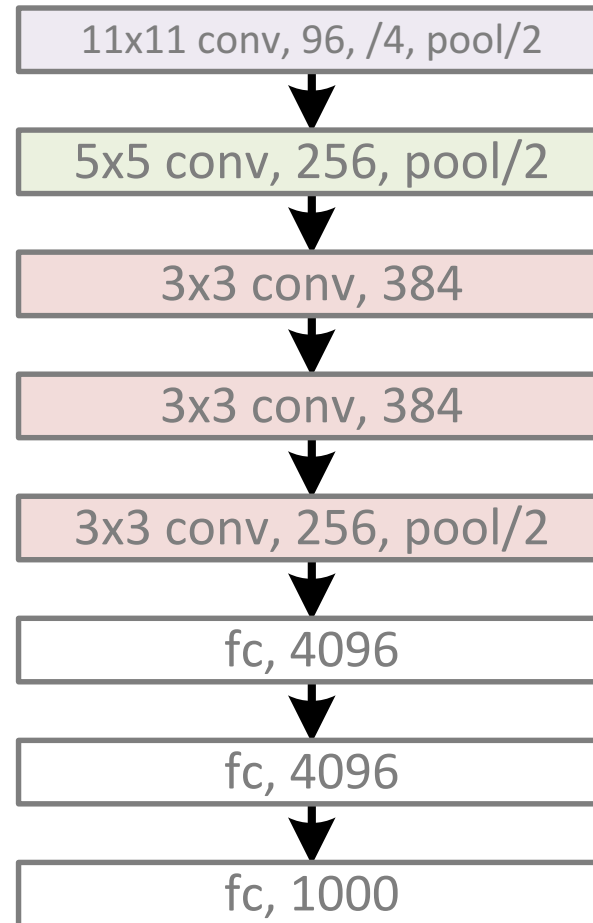
1933

# ImageNet Classification Challenge



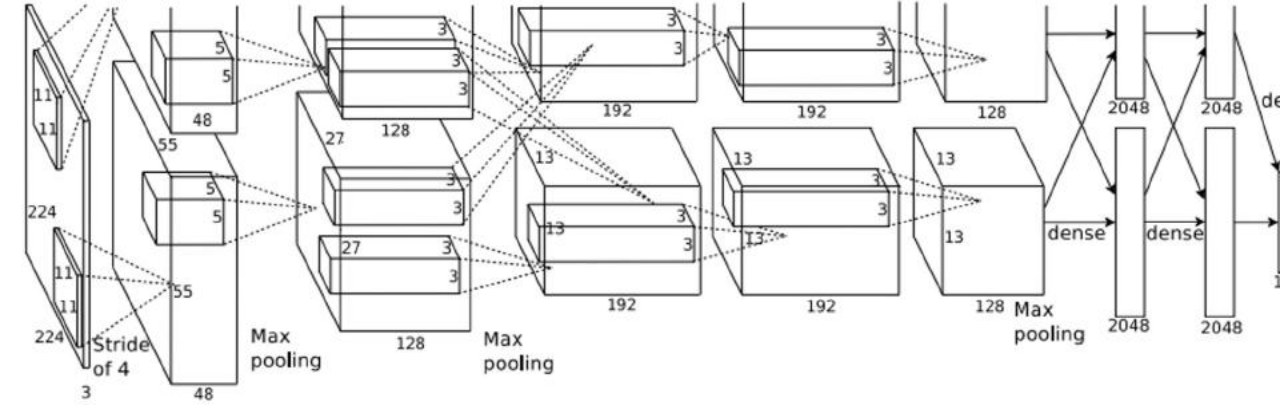
# Revolution of Depth

AlexNet, 8 layers  
(ILSVRC 2012)



- 5 convolutional layers
- 3 fully connected layers
- ReLU
- End-to-end (no pre-training)
- Data augmentation

# AlexNet

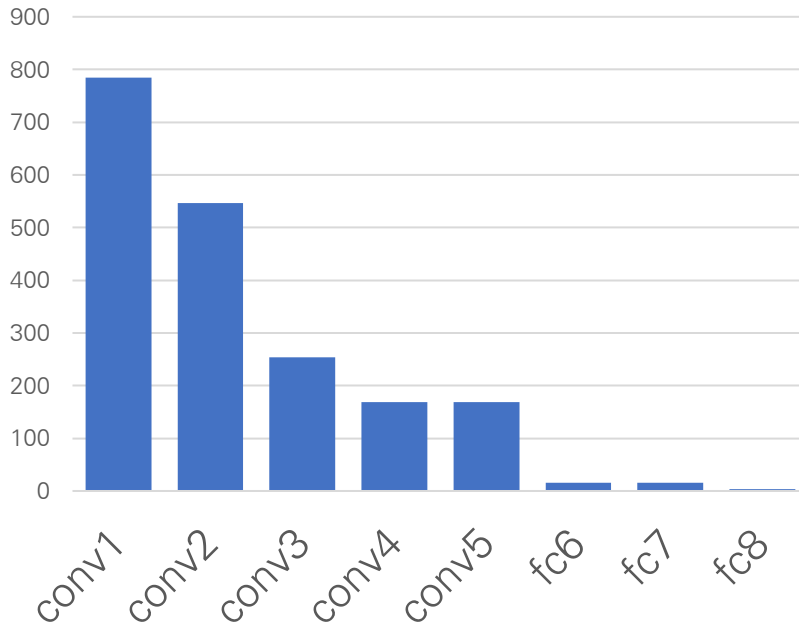


Most of the **memory usage** is in the early convolution layers

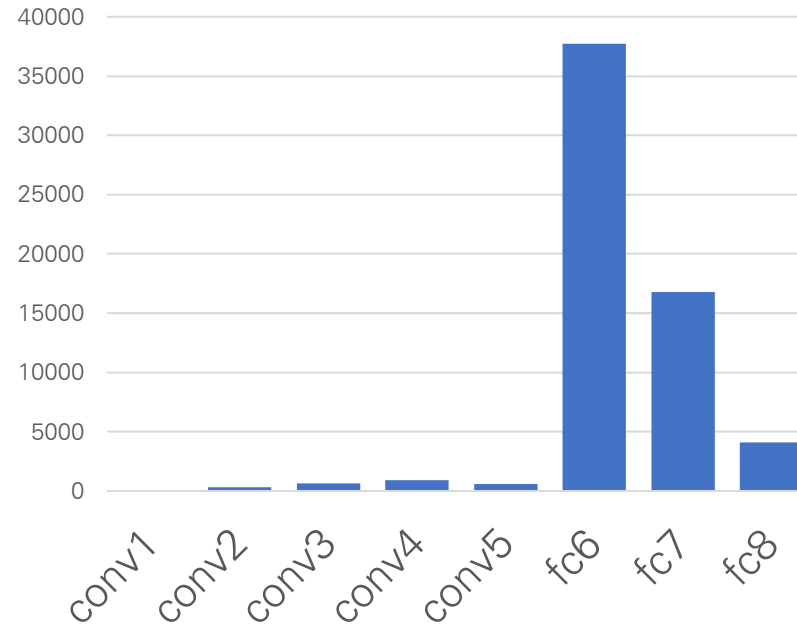
Nearly all **parameters** are in the fully-connected layers

Most **floating-point ops** occur in the convolution layers

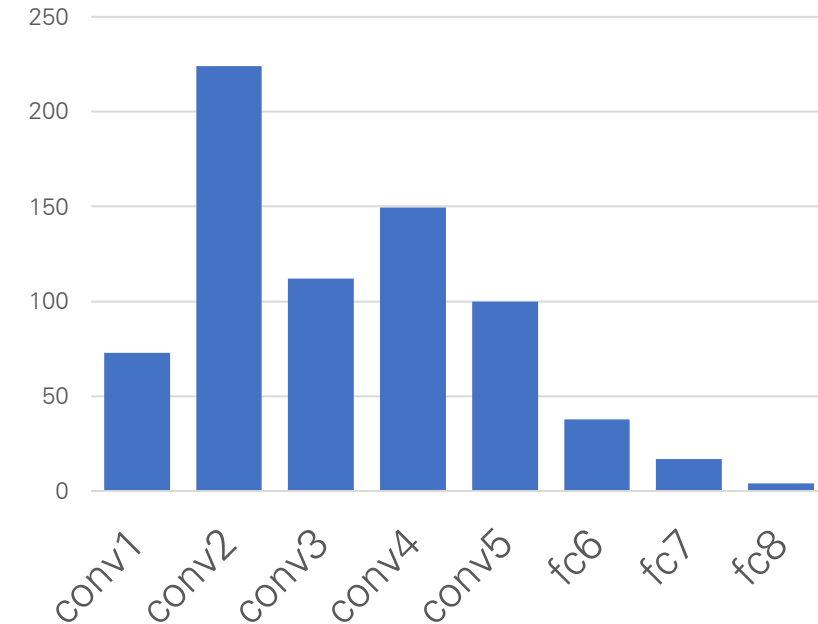
Memory (KB)



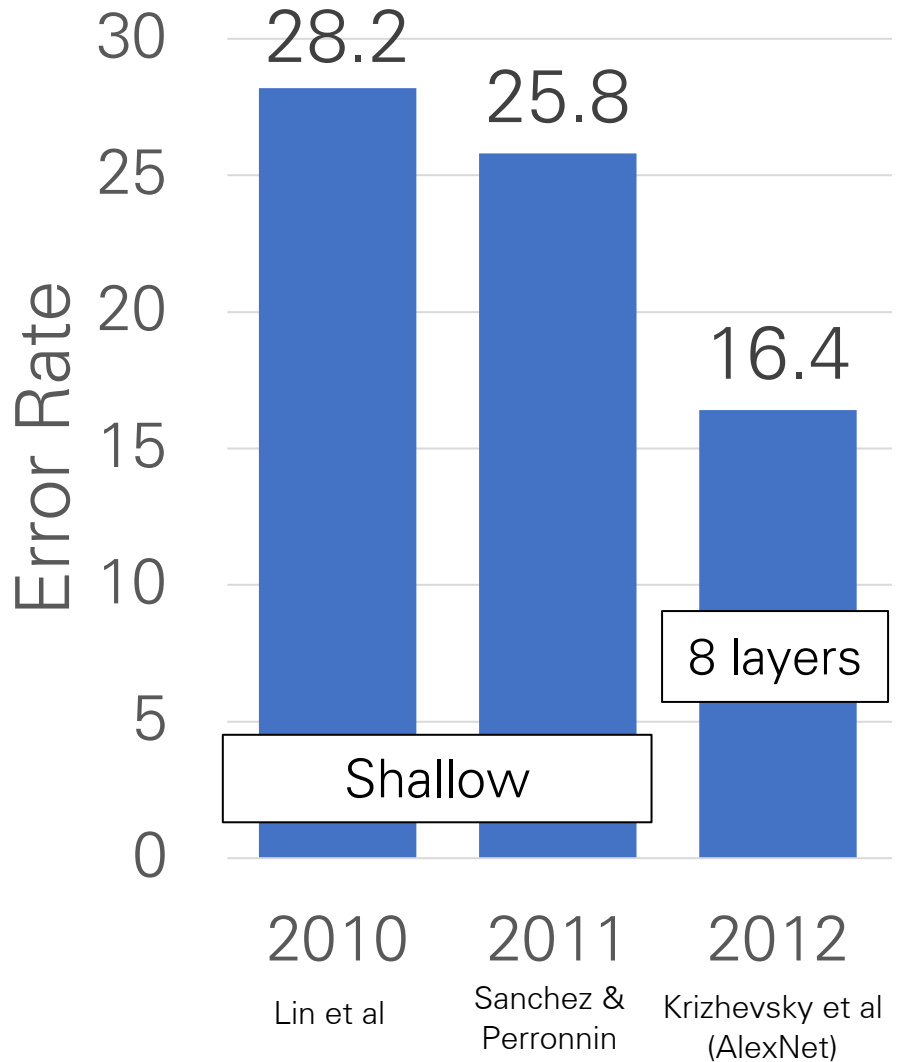
Params (K)



MFLOP

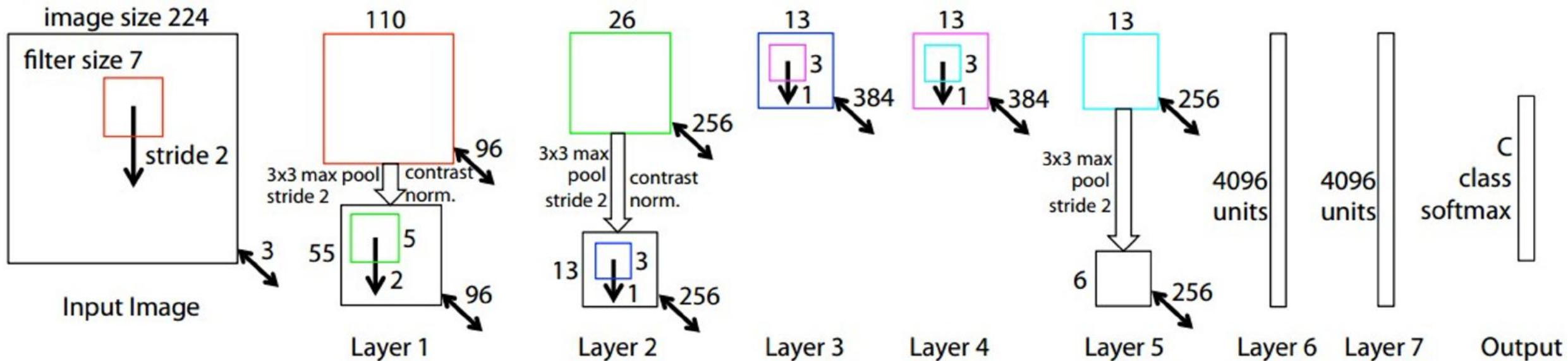


# ImageNet Classification Challenge





# ZFNet: A Bigger AlexNet



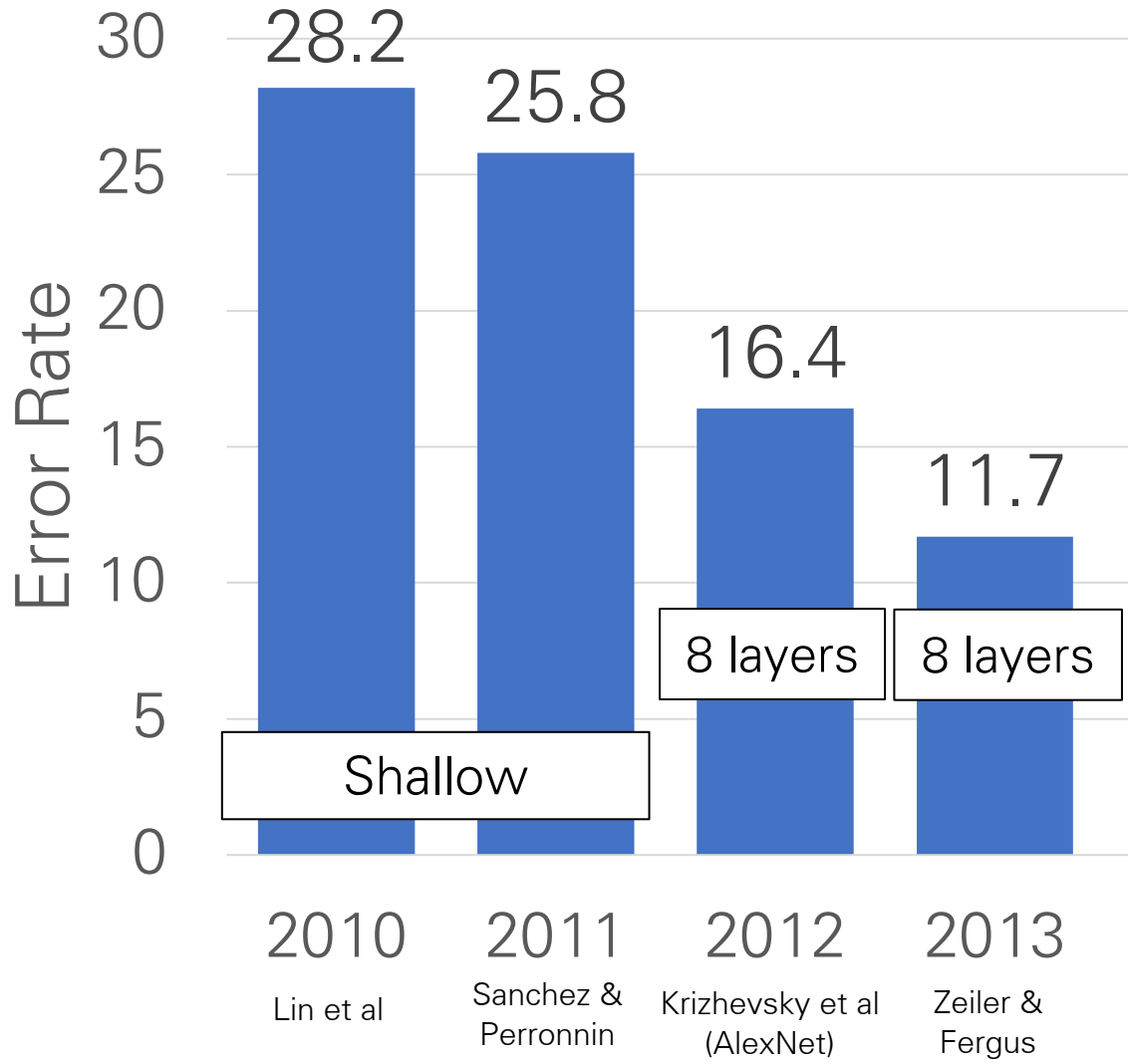
AlexNet but:

CONV1: change from (11x11 stride 4) to (7x7 stride 2)

CONV3,4,5: instead of 384, 384, 256 filters use 512, 1024, 512

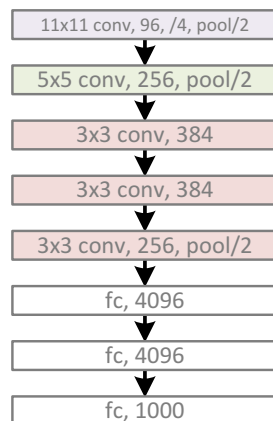
**More trial and error**

# ImageNet Classification Challenge

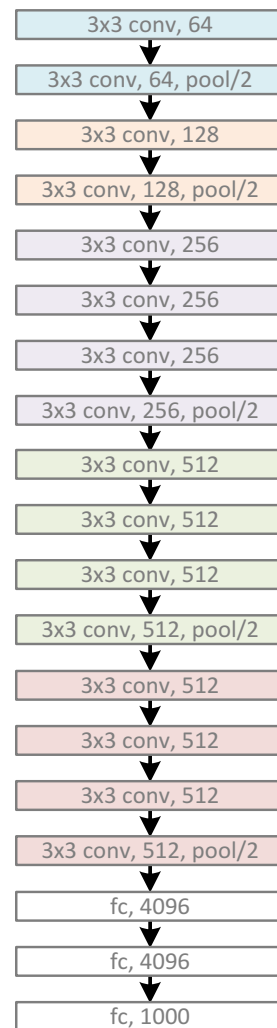


# Revolution of Depth

AlexNet, 8 layers  
(ILSVRC 2012)



VGG, 19 layers  
(ILSVRC 2014)



## VGG Design rules:

All conv are 3x3 stride 1 pad 1  
All max pool are 2x2 stride 2  
After pool, double #channels

Network has 5 convolutional **stages**:

Stage 1: conv-conv-pool

Stage 2: conv-conv-pool

Stage 3: conv-conv-pool

Stage 4: conv-conv-conv-[conv]-pool

Stage 5: conv-conv-conv-[conv]-pool

(VGG-19 has 4 conv in stages 4 and 5)

- Very deep
- Simply deep

# VGG: Deeper Networks, Regular Design

## VGG Design rules:

All conv are 3x3 stride 1 pad 1

All max pool are 2x2 stride 2

After pool, double #channels

## Option 1:

Conv(5x5, C -> C)

Params:  $25C^2$

FLOPs:  $25C^2HW$

## Option 2:

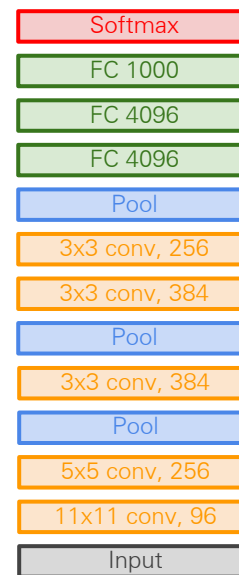
Conv(3x3, C -> C)

Conv(3x3, C -> C)

Params:  $18C^2$

FLOPs:  $18C^2HW$

Two 3x3 conv has same receptive field as a single 5x5 conv, but has fewer parameters and takes less computation!



AlexNet



VGG16

VGG19

# VGG: Deeper Networks, Regular Design

## VGG Design rules:

All conv are 3x3 stride 1 pad 1  
**All max pool are 2x2 stride 2**  
 After pool, double #channels

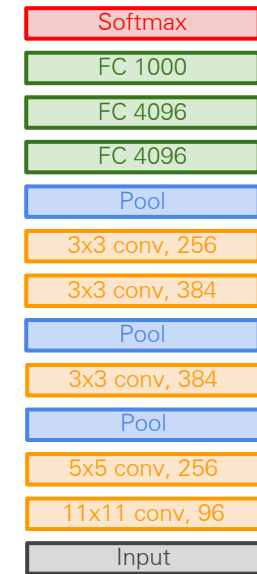
Input:  $C \times 2H \times 2W$   
 Layer: Conv(3x3,  $C \rightarrow C$ )

Memory:  $4HWC$   
 Params:  $9C^2$   
 FLOPs:  $36HWC^2$

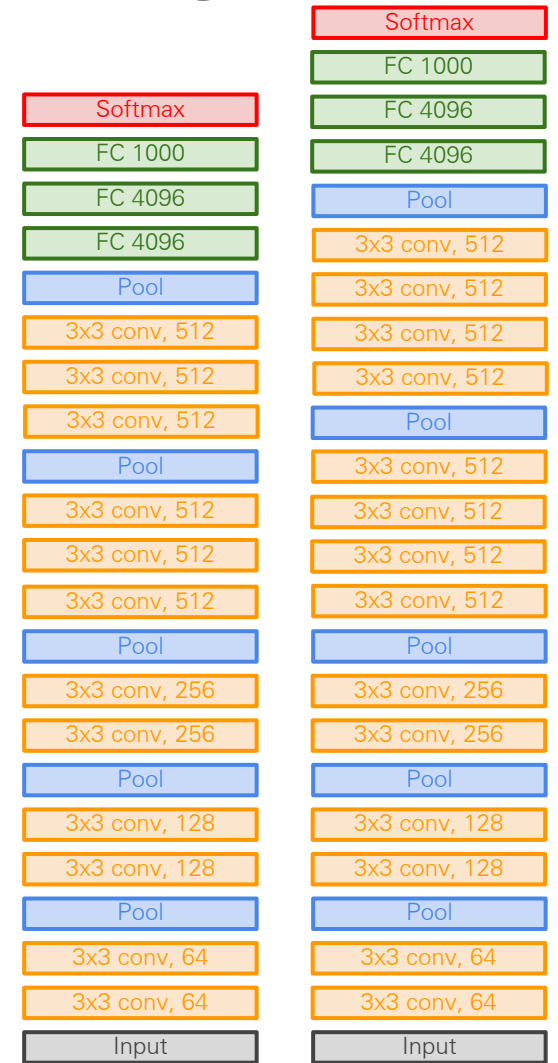
Input:  $2C \times H \times W$   
 Conv(3x3,  $2C \rightarrow 2C$ )

Memory:  $2HWC$   
 Params:  $36C^2$   
 FLOPs:  $36HWC^2$

Conv layers at each spatial resolution take the same amount of computation!



AlexNet

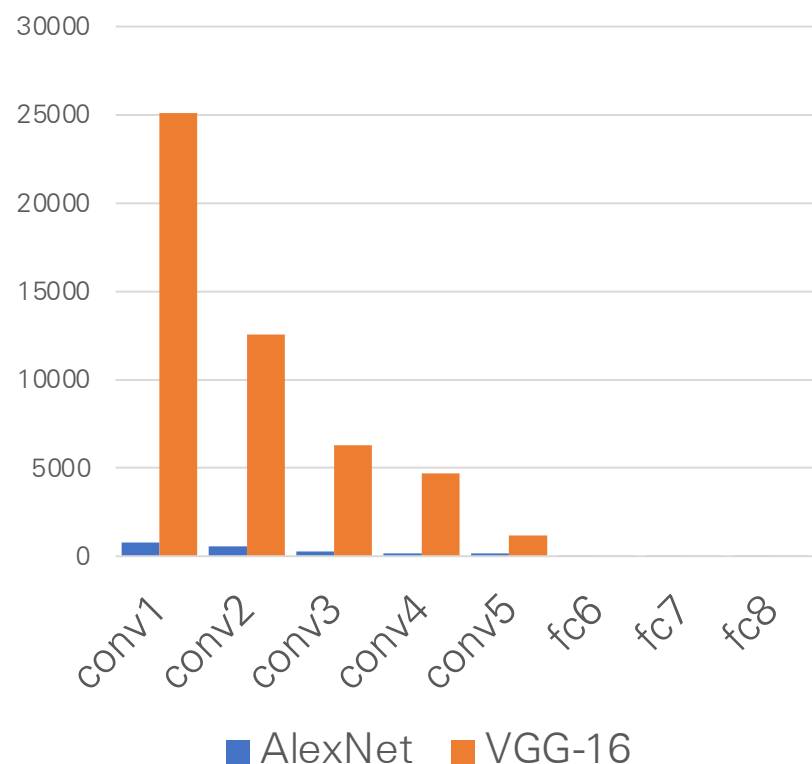


VGG16

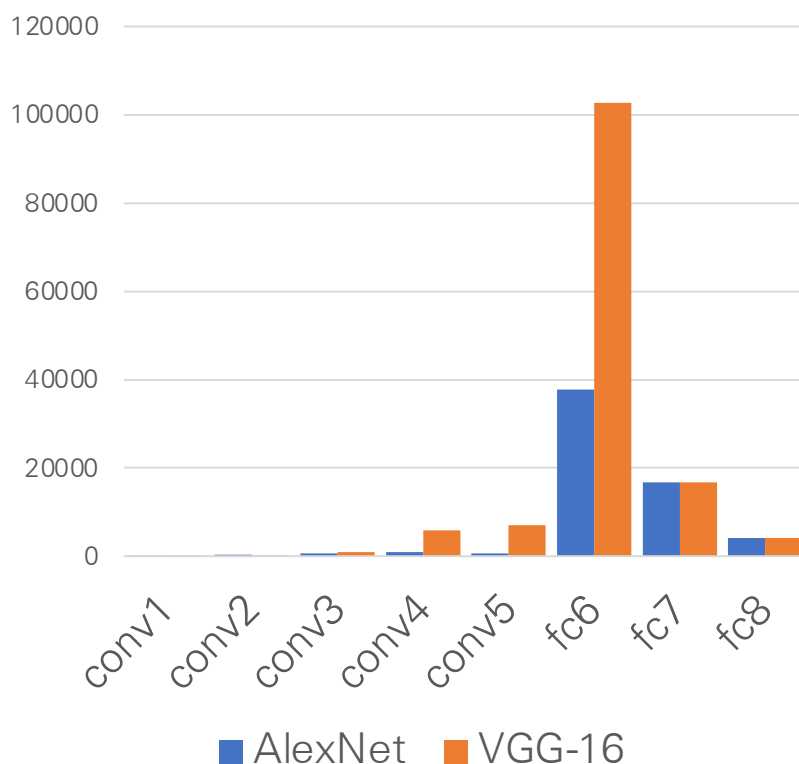
VGG19

# AlexNet vs VGG-16: Much bigger network!

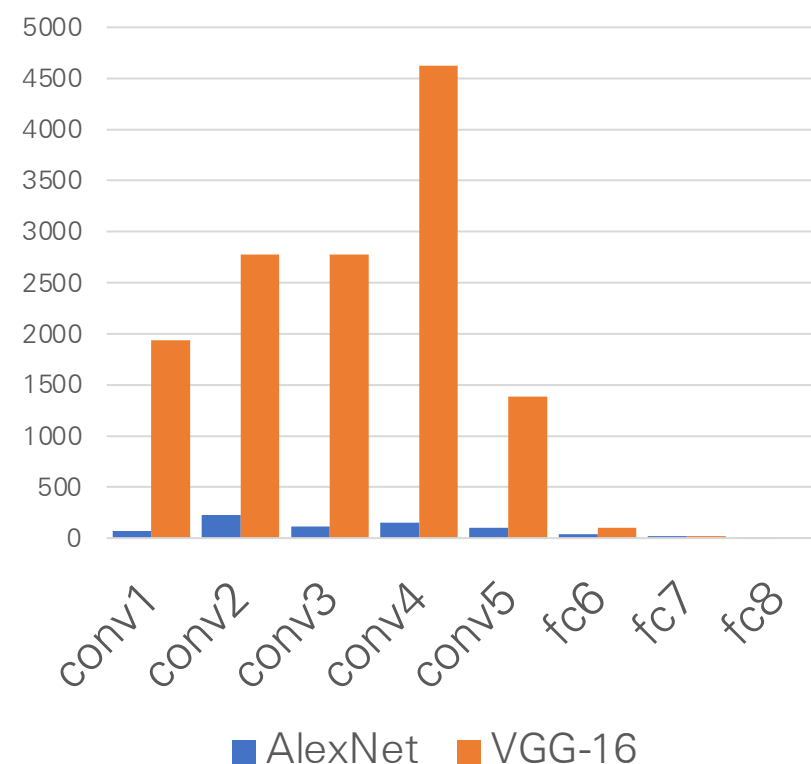
AlexNet vs VGG-16  
(Memory, KB)



AlexNet vs VGG-16  
(Params, M)



AlexNet vs VGG-16  
(MFLOPs)



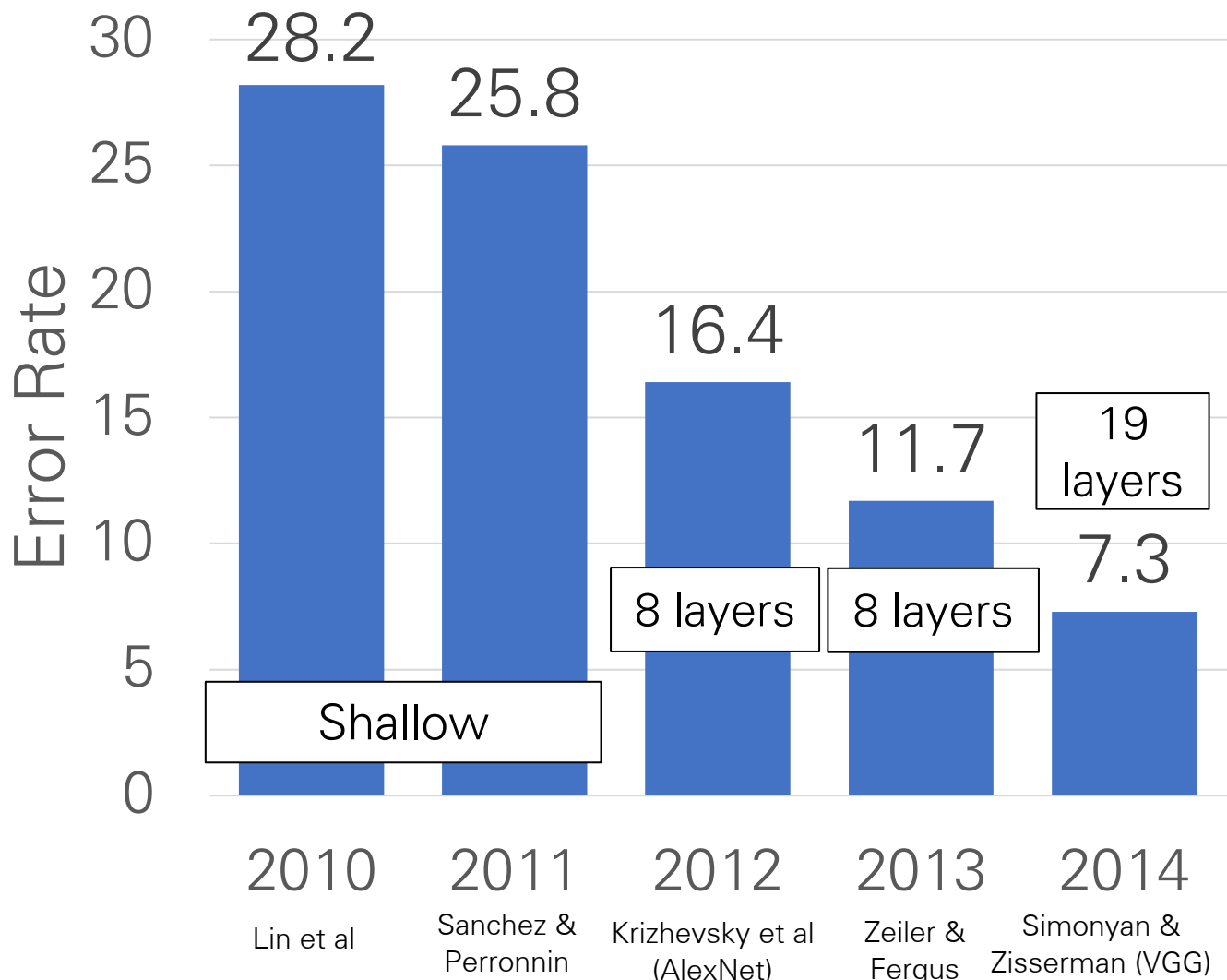
AlexNet total: 1.9 MB  
VGG-16 total: 48.6 MB (25x)

AlexNet total: 61M  
VGG-16 total: 138M (2.3x)

AlexNet total: 0.7 GFLOP  
VGG-16 total: 13.6 GFLOP (19.4x)

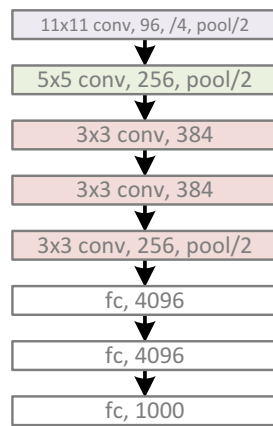


# ImageNet Classification Challenge

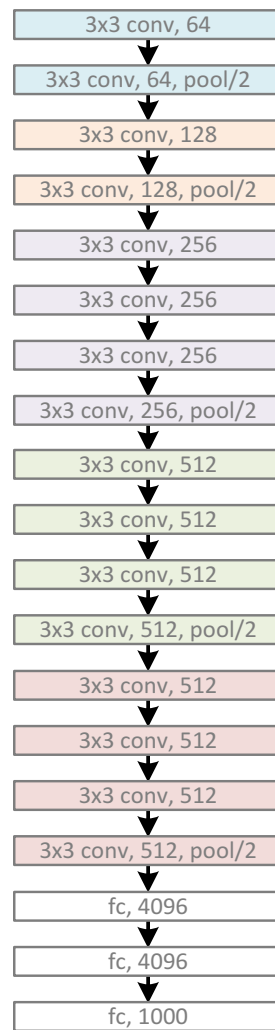


# Revolution of Depth

AlexNet, 8 layers  
(ILSVRC 2012)

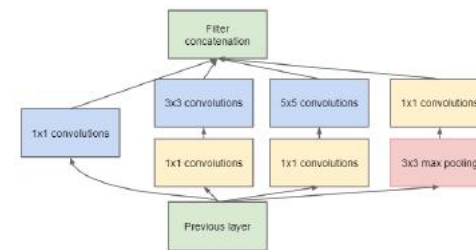


VGG, 19 layers  
(ILSVRC 2014)



- Very deep
- Simply deep

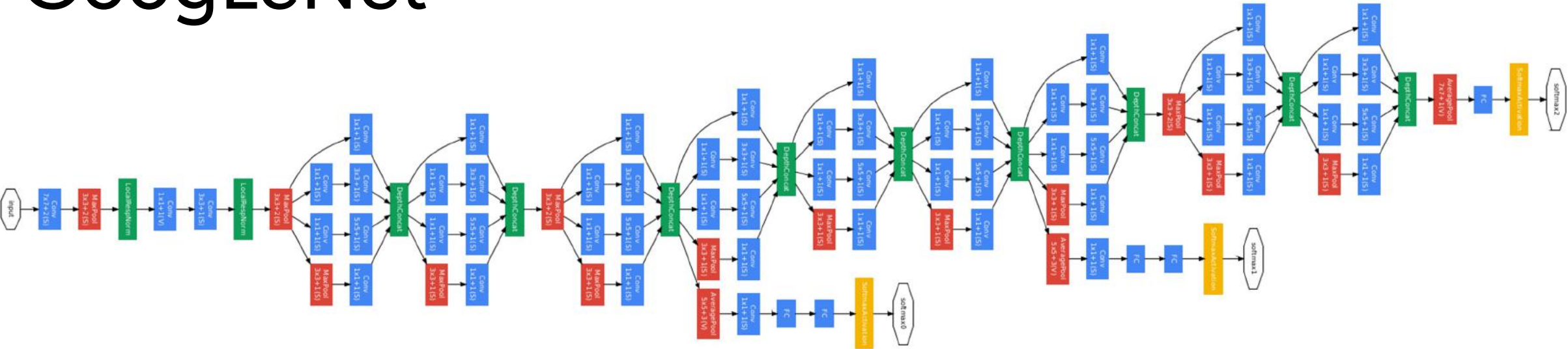
GoogLeNet,  
22 layers  
(ILSVRC 2014)



- Branching
- Bottleneck
- Skip connection

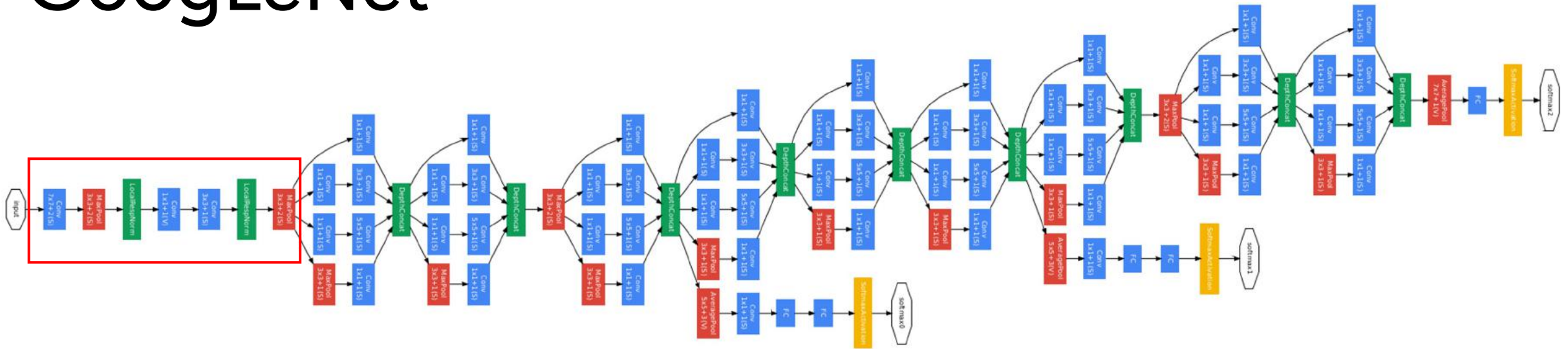


# GoogLeNet



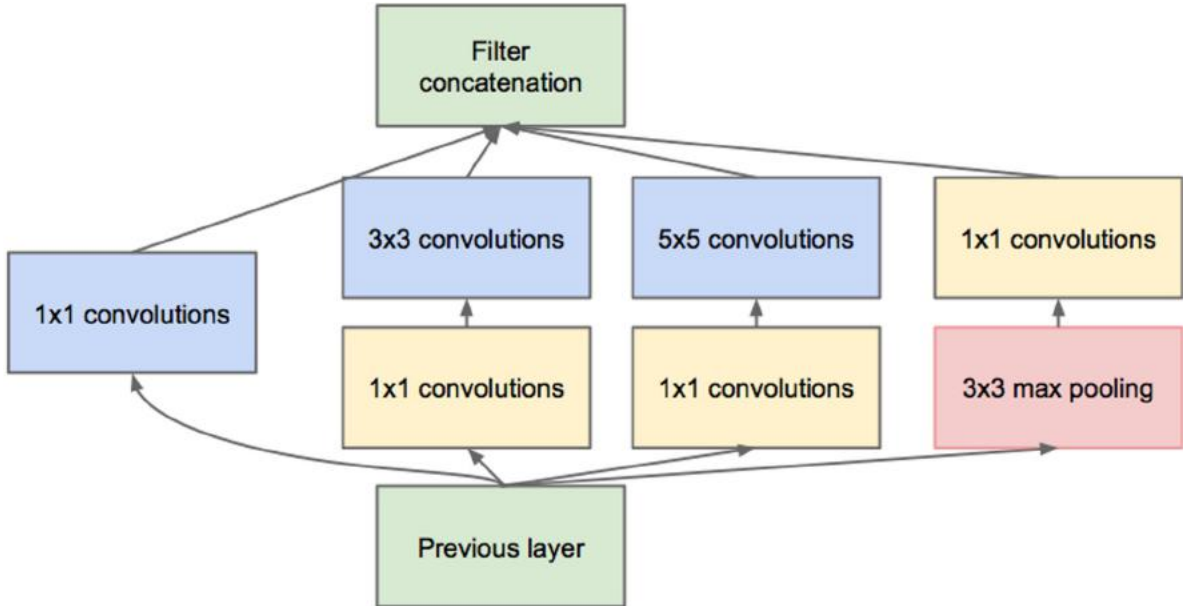
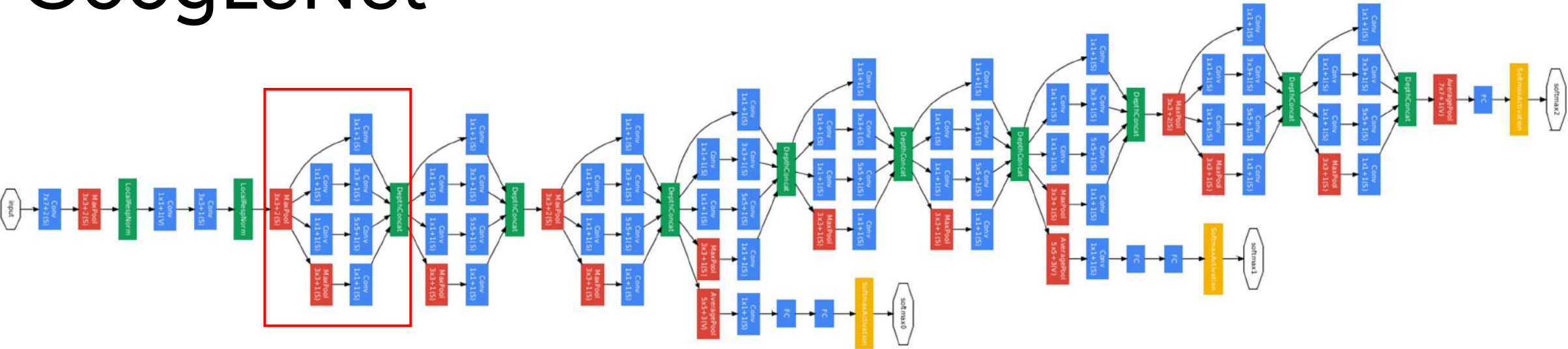
Many innovations for efficiency: reduce parameter count, memory usage, and computation

# GoogLeNet



**Stem network** at the start aggressively downsamples input (Recall in VGG-16: Most of the compute was at the start)

# GoogLeNet

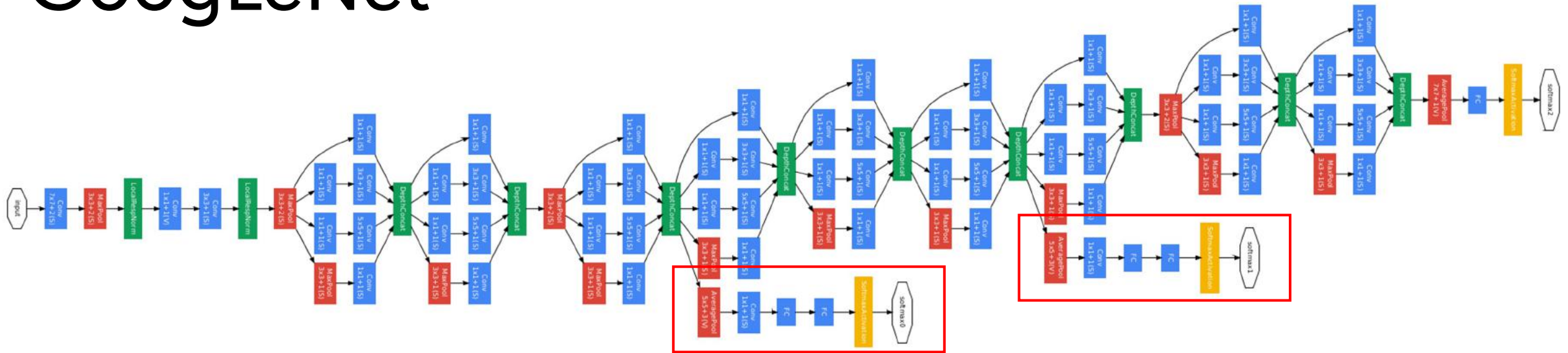


## Inception module

Local unit with parallel branches  
 Local structure repeated many times throughout the network  
 Uses 1x1 "Bottleneck" layers to reduce channel dimension before expensive conv



# GoogLeNet



## Auxiliary Classifiers

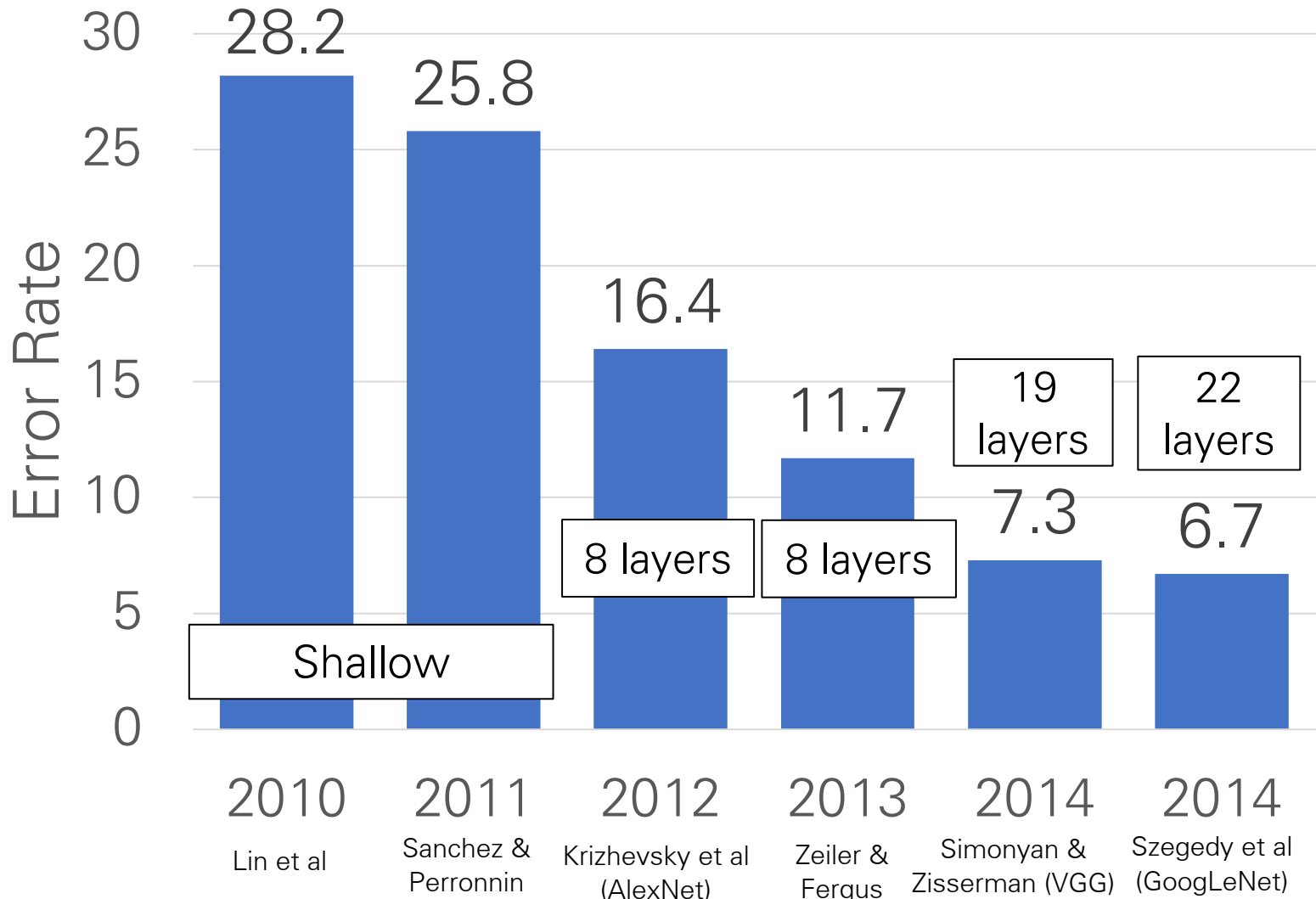
Training using loss at the end of the network didn't work well: Network is too deep, gradients don't propagate cleanly

As a hack, attach "auxiliary classifiers" at several intermediate points in the network that also try to classify the image and receive loss

GoogLeNet was before batch normalization! With BatchNorm no longer need to use this trick



# ImageNet Classification Challenge



# GoogLeNet

[Szegedy et al., 2014]

Fun features:

- Only 5 million params!  
(Removes FC layers completely)

**Compared to AlexNet:**

- 12X less params  
- 2x more compute  
- 6.67% (vs. 16.4%)

type	patch size/ stride	output size	depth	#1×1	#3×3 reduce	#3×3	#5×5 reduce	#5×5	pool proj	params	ops
convolution	7×7/2	112×112×64	1							2.7K	34M
max pool	3×3/2	56×56×64	0								
convolution	3×3/1	56×56×192	2		64	192				112K	360M
max pool	3×3/2	28×28×192	0								
inception (3a)		28×28×256	2	64	96	128	16	32	32	159K	128M
inception (3b)		28×28×480	2	128	128	192	32	96	64	380K	304M
max pool	3×3/2	14×14×480	0								
inception (4a)		14×14×512	2	192	96	208	16	48	64	364K	73M
inception (4b)		14×14×512	2	160	112	224	24	64	64	437K	88M
inception (4c)		14×14×512	2	128	128	256	24	64	64	463K	100M
inception (4d)		14×14×528	2	112	144	288	32	64	64	580K	119M
inception (4e)		14×14×832	2	256	160	320	32	128	128	840K	170M
max pool	3×3/2	7×7×832	0								
inception (5a)		7×7×832	2	256	160	320	32	128	128	1072K	54M
inception (5b)		7×7×1024	2	384	192	384	48	128	128	1388K	71M
avg pool	7×7/1	1×1×1024	0								
dropout (40%)		1×1×1024	0								
linear		1×1×1000	1							1000K	1M
softmax		1×1×1000	0								

# Revolution of Depth

AlexNet, 8 layers  
(ILSVRC 2012)



VGG, 19 layers  
(ILSVRC 2014)

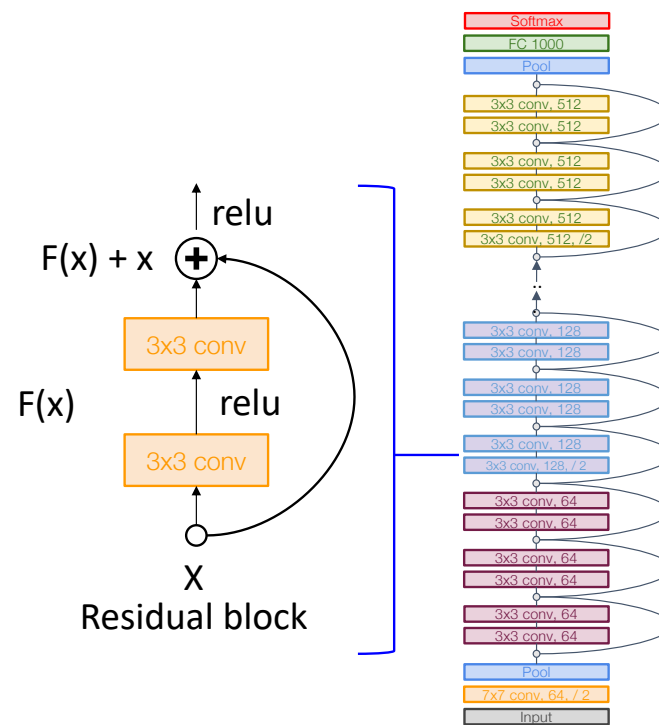


ResNet,  
152 layers  
(ILSVRC 2015)

A residual network is a stack of many residual blocks

Regular design, like VGG: each residual block has two 3x3 conv

Network is divided into **stages**: the first block of each stage halves the resolution (with stride-2 conv) and doubles the number of channels



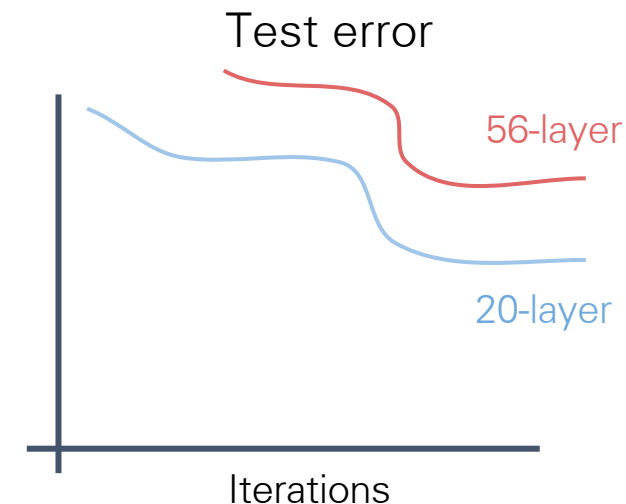
# Residual Networks (ResNet)

[He et al., 2015]

Once we have Batch Normalization, we can train networks with 10+ layers. What happens as we go deeper?

Deeper model does worse than shallow model!

Initial guess: Deep model is **overfitting** since it is much bigger than the other model



# Residual Networks (ResNet)

[He et al., 2015]

Once we have Batch Normalization, we can train networks with 10+ layers. What happens as we go deeper?



In fact, the deep model seems to be **underfitting** since it also performs worse than the shallow model on the training set! It is actually **underfitting**

# Residual Networks (ResNet)

[He et al., 2015]

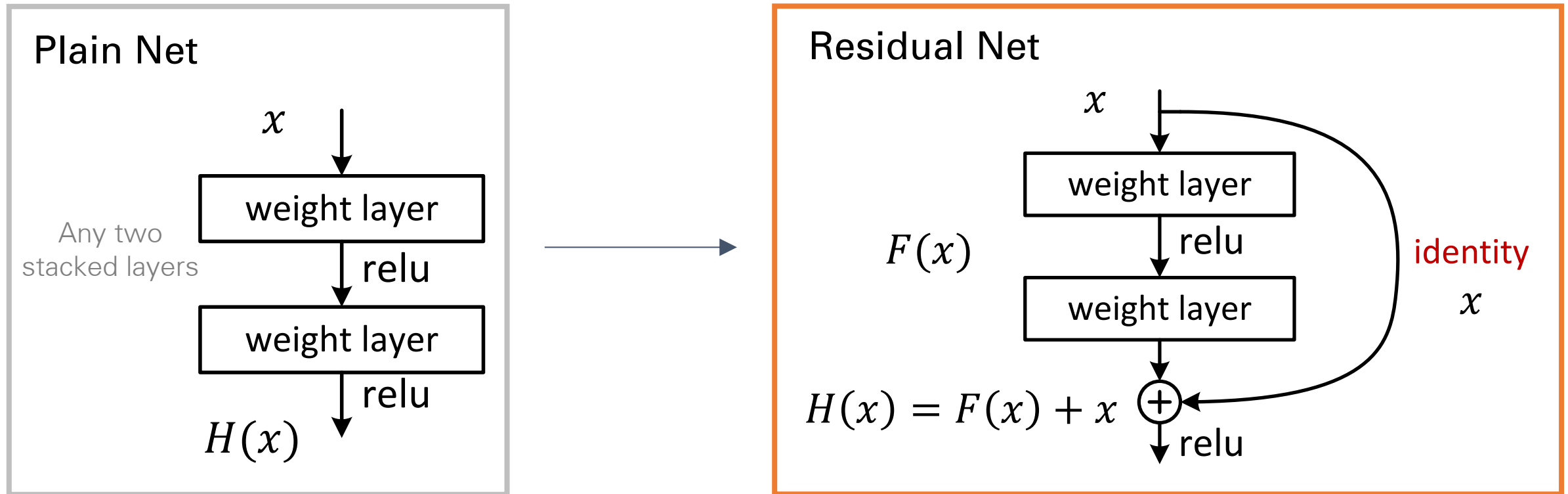
- A deeper model can emulate a shallower model: copy layers from shallower model, set extra layers to identity
- Thus deeper models should do at least as good as shallow models
- **Hypothesis:** This is an optimization problem. Deeper models are harder to optimize, and in particular don't learn identity functions to emulate shallow models

**Solution:** Change the network so learning identity functions with extra layers is easy!



# Residual Networks (ResNet)

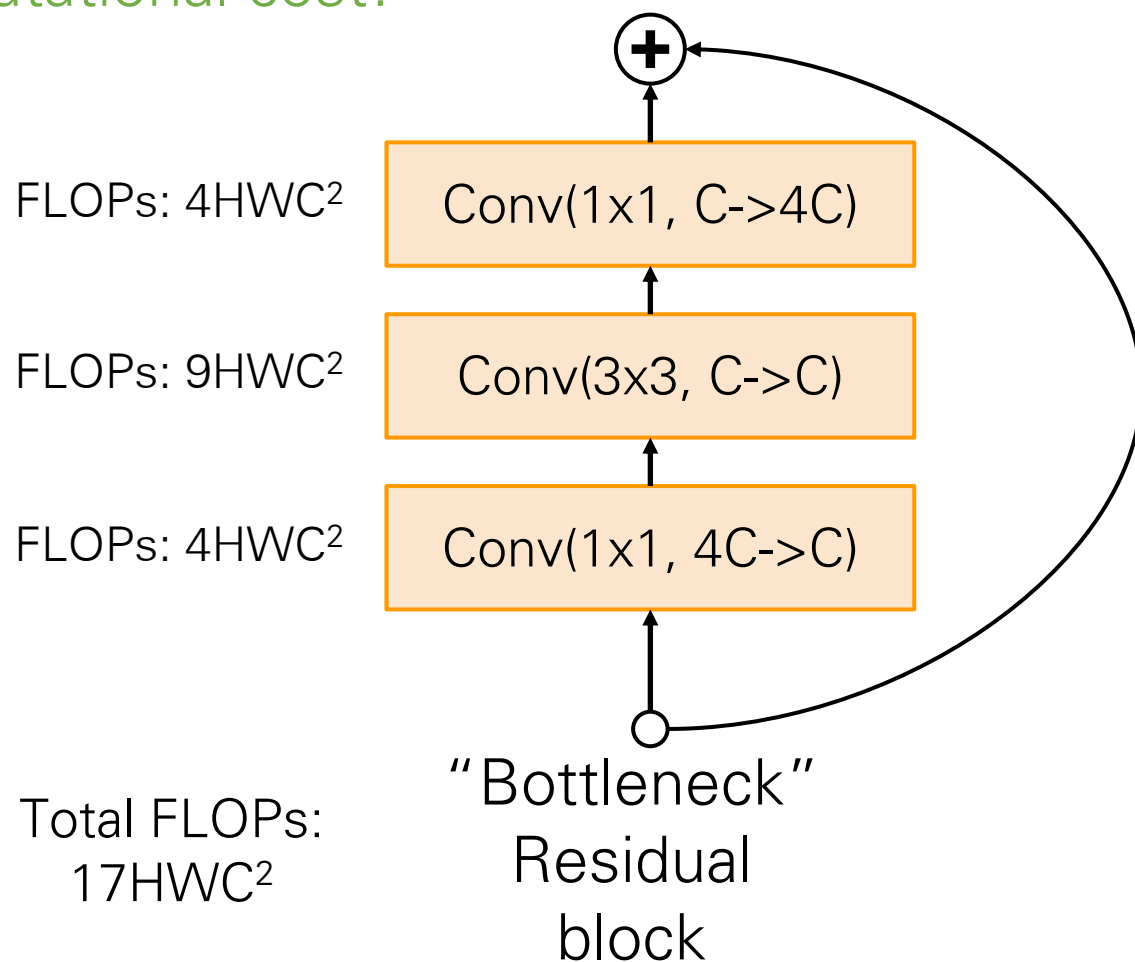
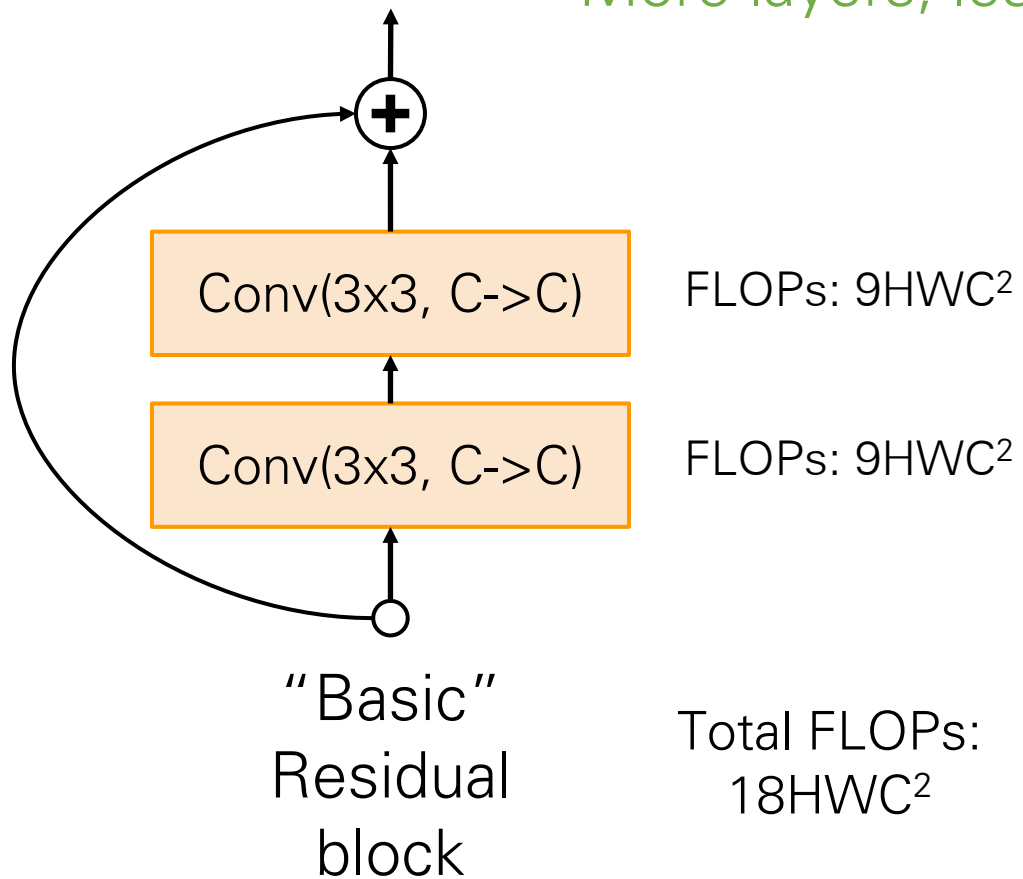
[He et al., 2015]



# Residual Networks (ResNet)

[He et al., 2015]

More layers, less computational cost!



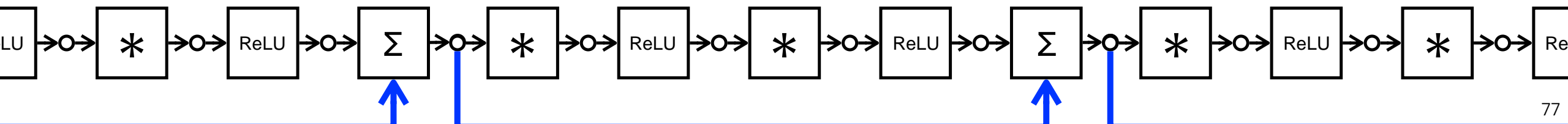
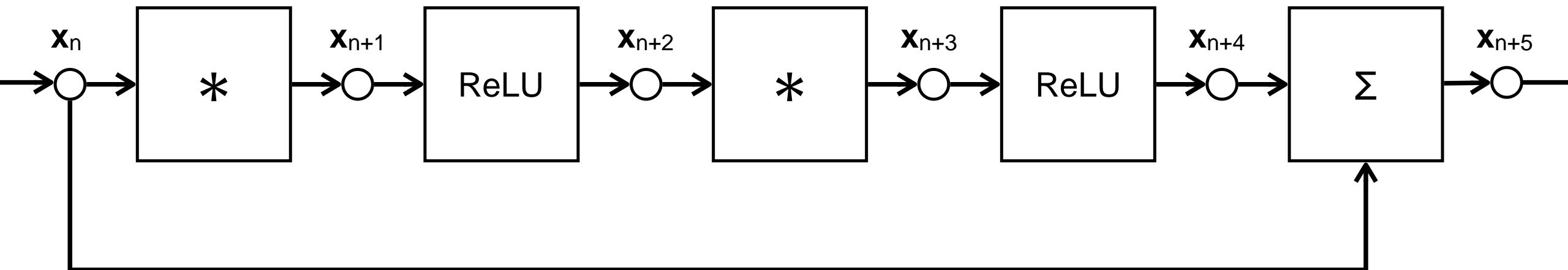
# Residual Learning

Fixed identity  
// learned residual

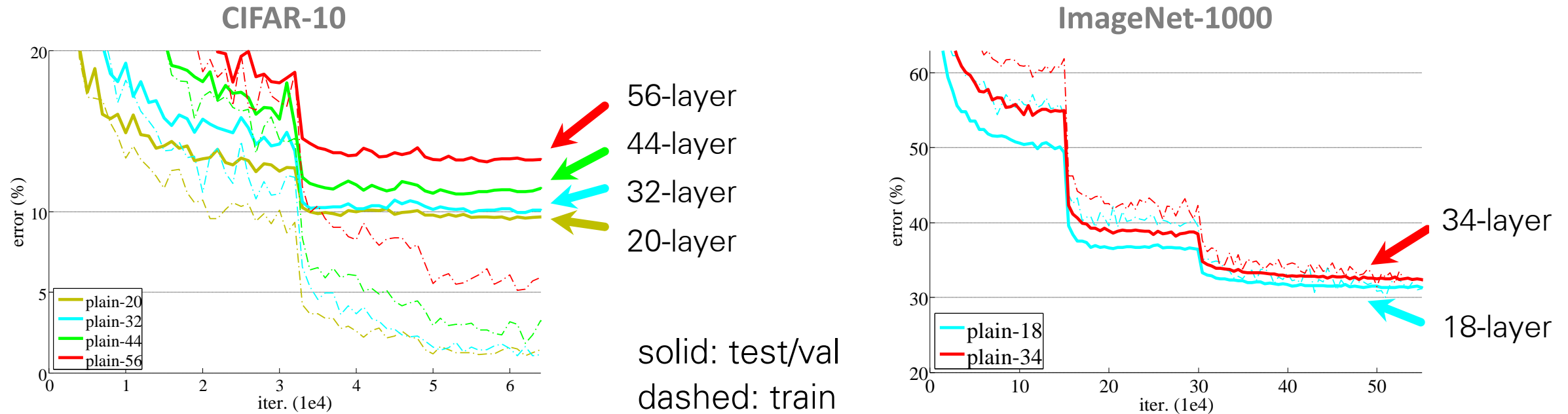
$$\mathbf{x}_{n+5} = \mathbf{x}_n + \underbrace{(\phi_{\text{ReLU}} \circ \phi_* \circ \phi_{\text{ReLU}} \circ \phi_*)}_{\text{residual}}(\mathbf{x}_n)$$

↑  
identity

K. He, X. Zhang, S. Ren, and J. Sun.  
**Deep residual learning for image recognition.** In CVPR 2016.



# Residual Learning

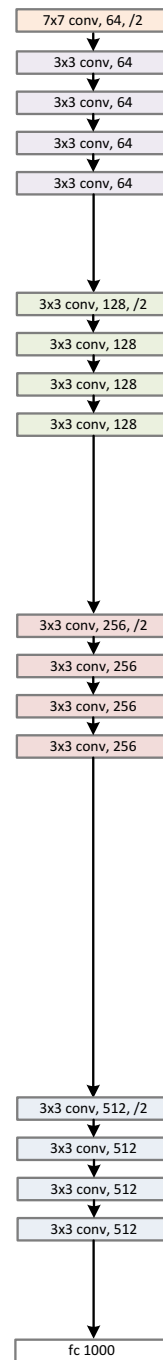


- “Overly deep” plain nets have **higher training error**
- A general phenomenon, observed in many datasets
- This is optimization issue, deeper models are harder to optimize

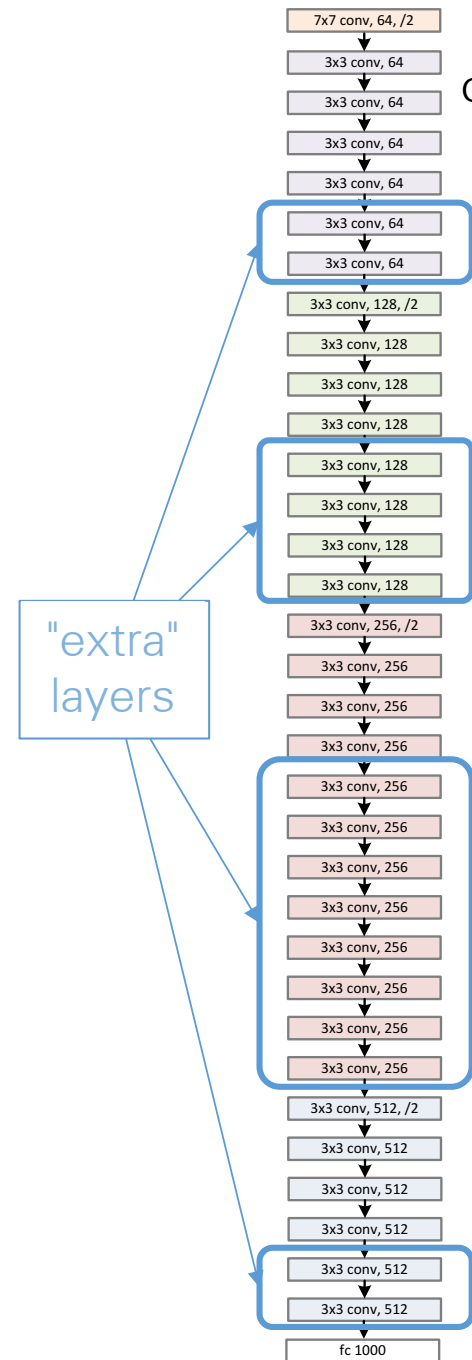
# Residual Learning

- Richer solution space
- A deeper model should not have **higher training error**
- A solution by construction:
  - original layers: copied from a learned shallower model
  - extra layers: set as identity
  - at least the same training error

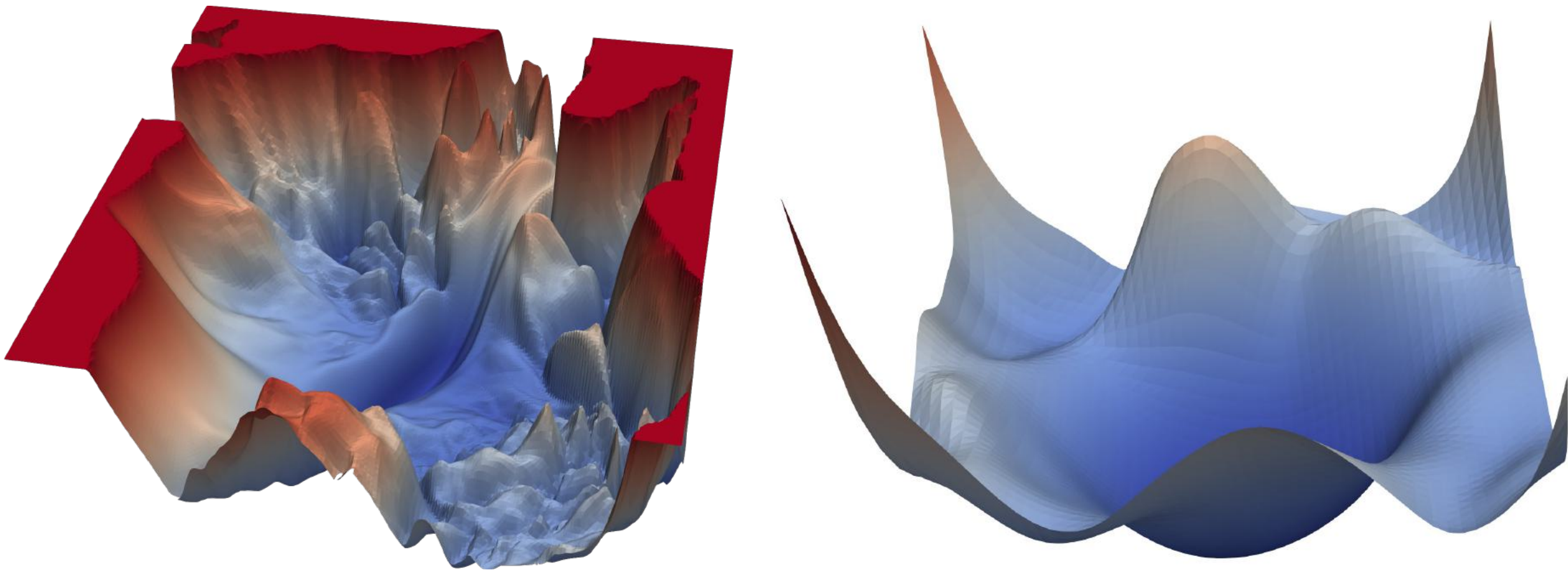
a shallower model  
(18 layers)



a deeper counterpart  
(34 layers)



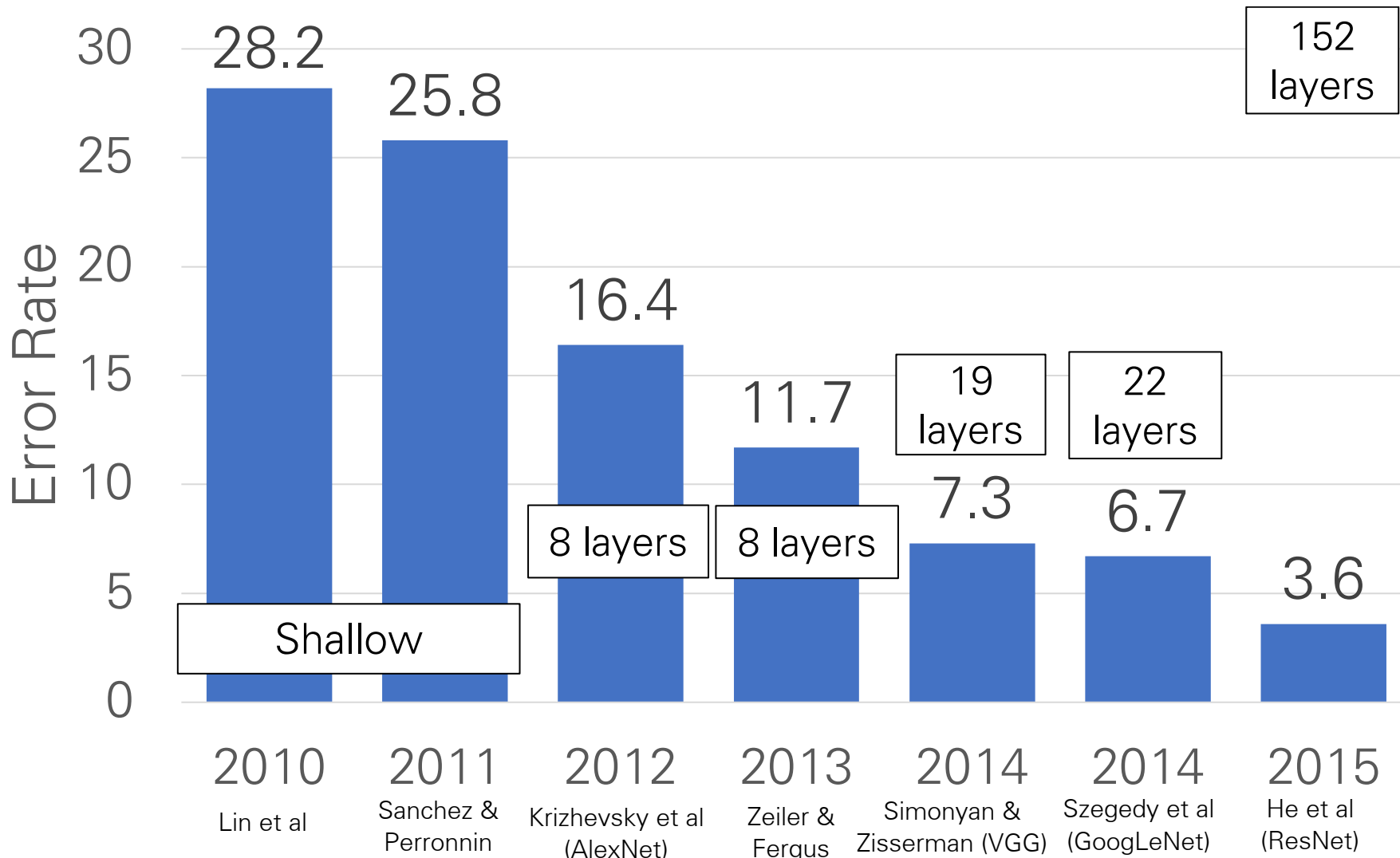
# Residual Learning



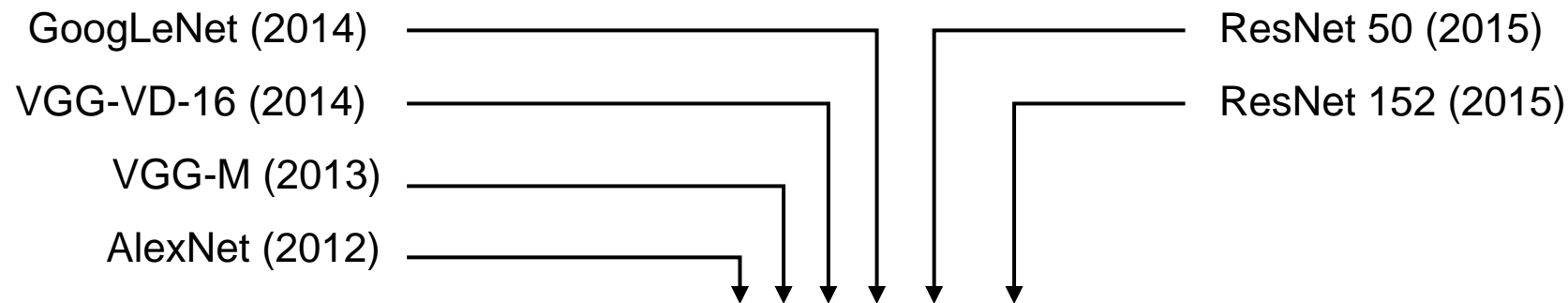
- The loss surface of a 56-layer net using the CIFAR-10 dataset, both without (left) and with (right) residual connections.



# ImageNet Classification Challenge



# How deep is enough?



16 convolutional layers



50 convolutional layers



152 convolutional layers



Krizhevsky, I. Sutskever, and G. E. Hinton. *ImageNet classification with deep convolutional neural networks*. In Proc. NIPS, 2012.

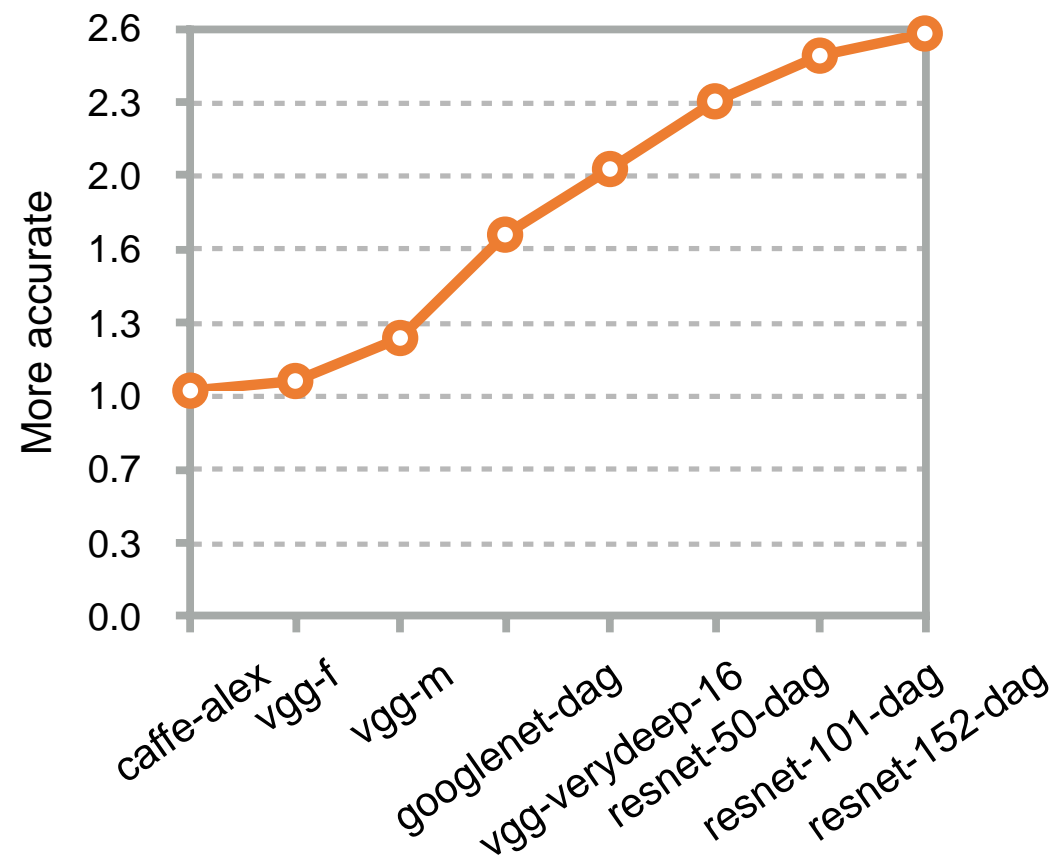
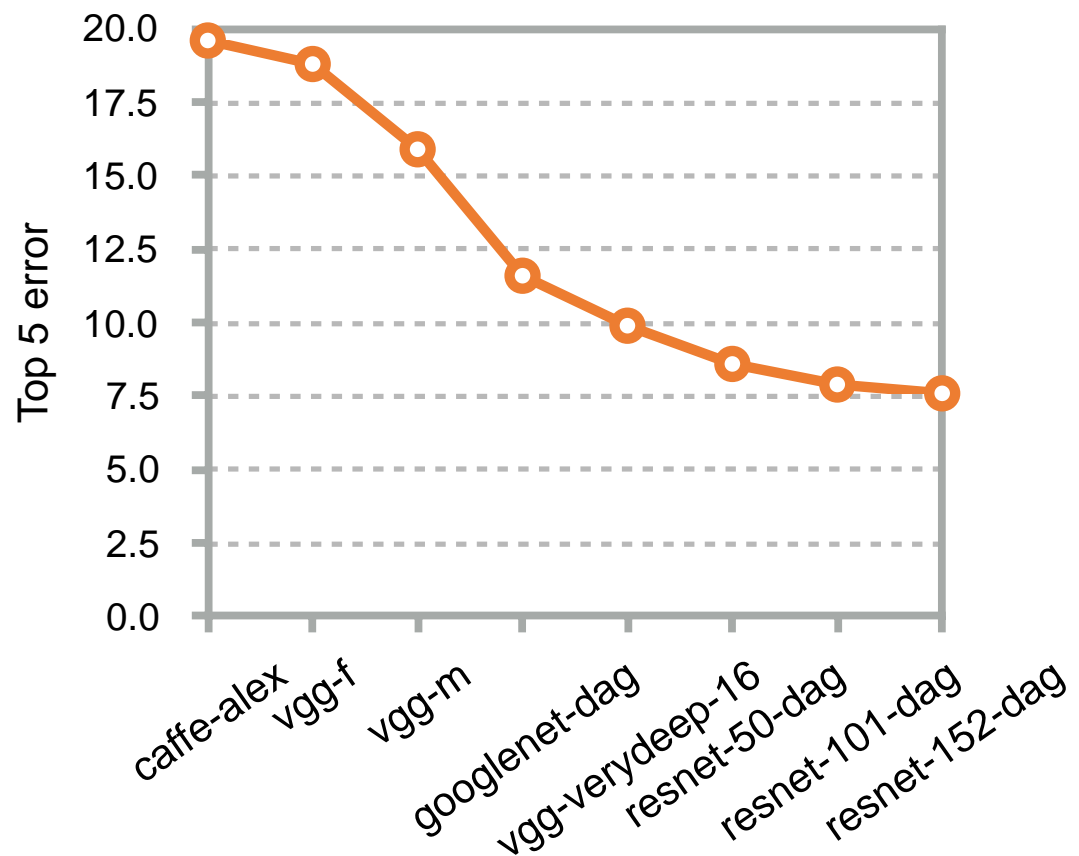
C. Szegedy, W. Liu, Y. Jia, P. Sermanet, S. Reed, D. Anguelov, D. Erhan, V. Vanhoucke, and A. Rabinovich. *Going deeper with convolutions*. In Proc. CVPR, 2015.

K. Simonyan and A. Zisserman. *Very deep convolutional networks for large-scale image recognition*. In Proc. ICLR, 2015.

K. He, X. Zhang, S. Ren, and J. Sun. *Deep residual learning for image recognition*. In Proc. CVPR, 2016.

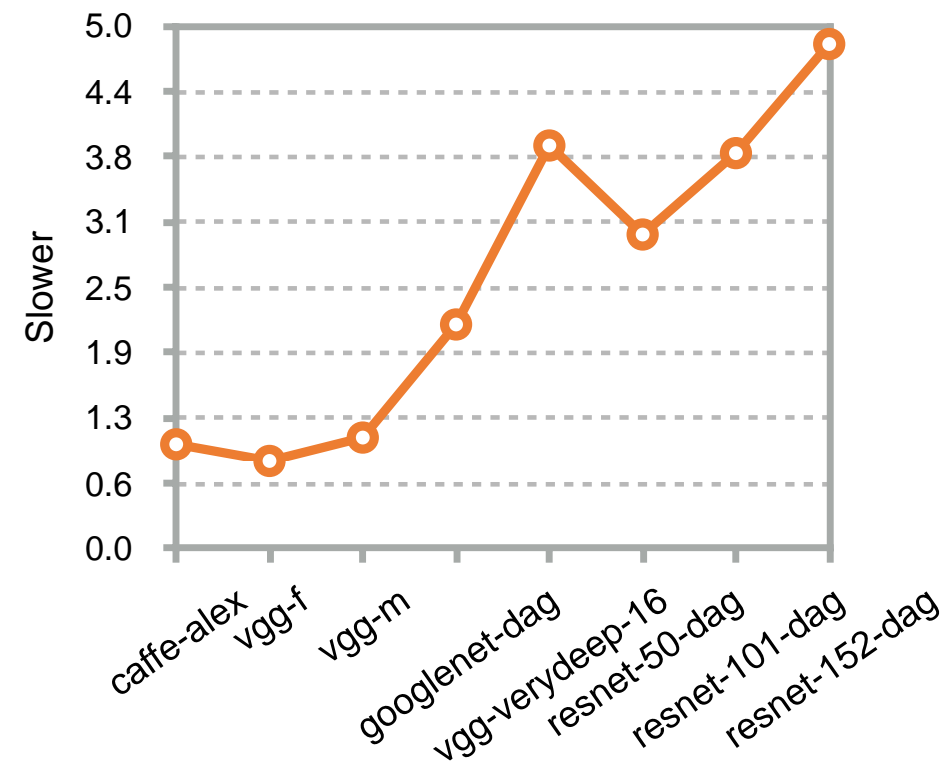
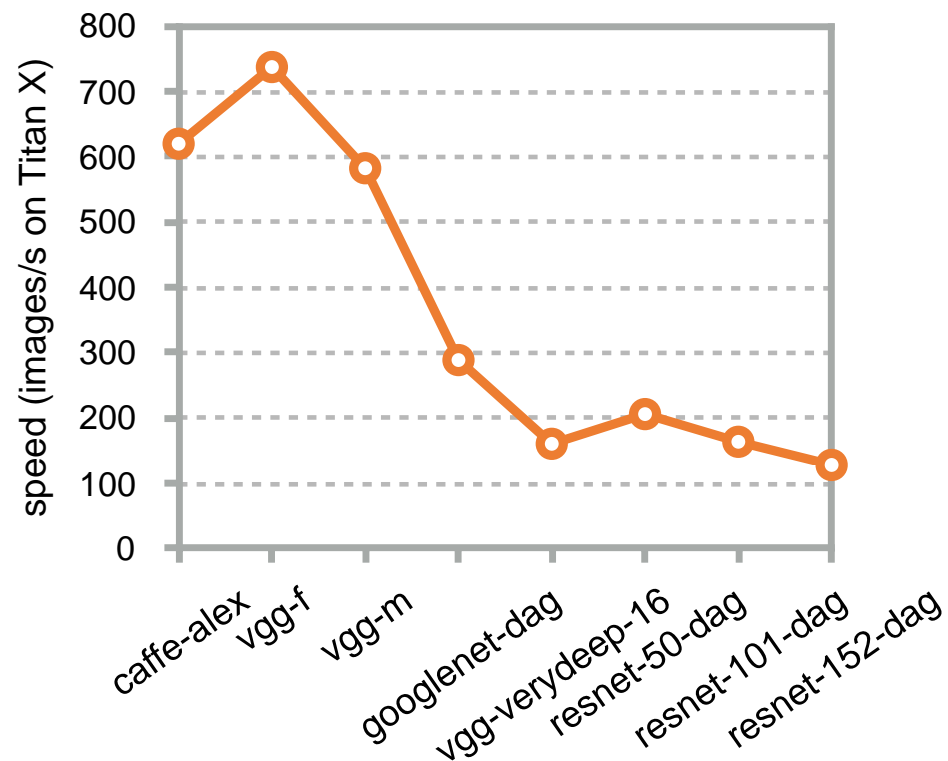
# How deep is enough?

- 3 × more accurate in 3 years



# Speed

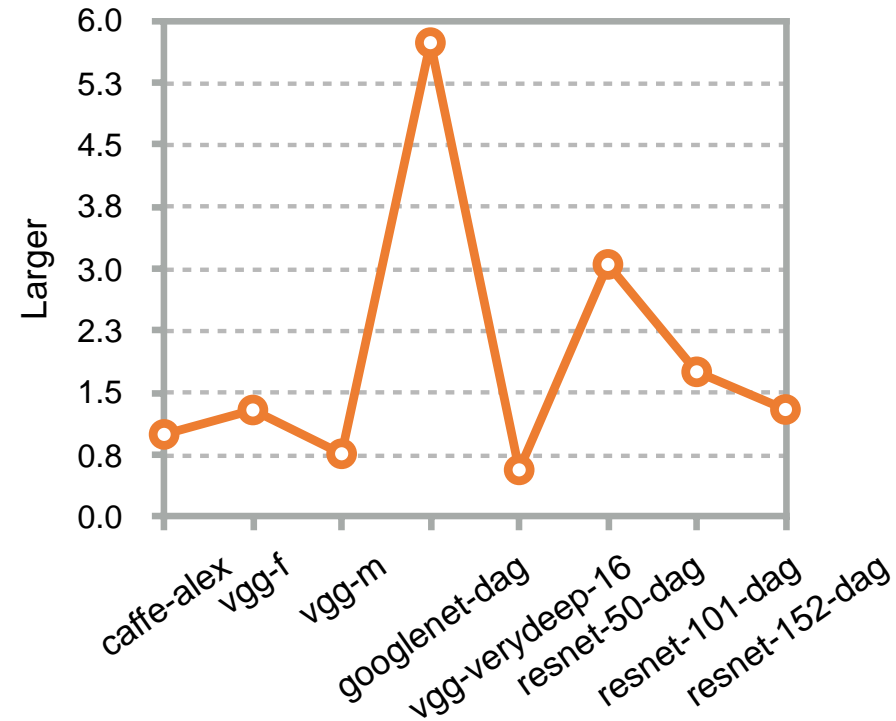
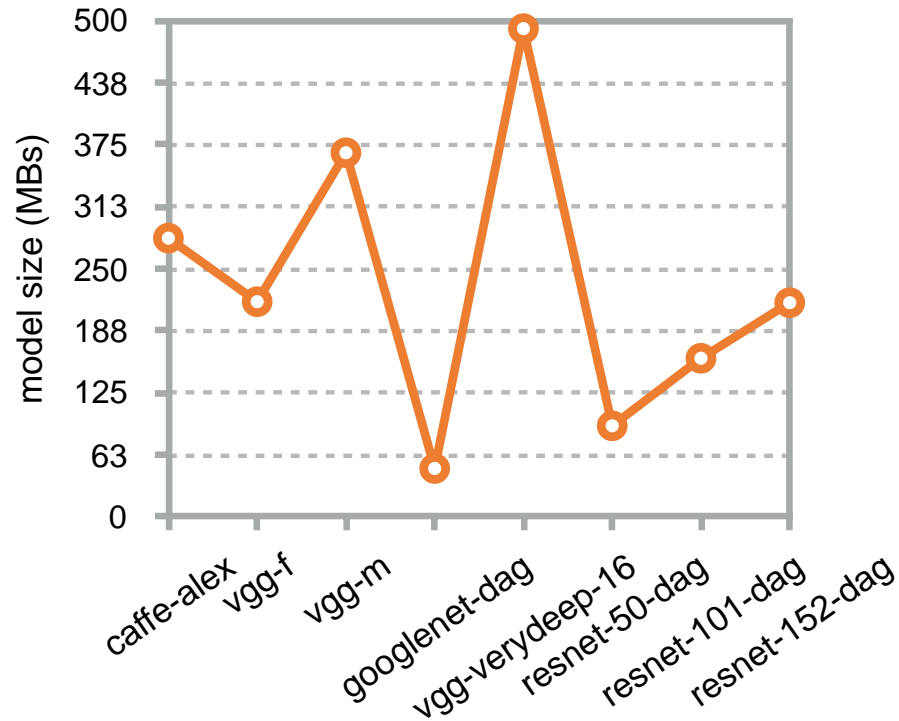
- 5 × slower



- **Remark:** 101 ResNet layers same size/speed as 16 VGG-VD layers
- **Reason:** Far fewer feature channels (quadratic speed/space gain)
- **Moral:** Optimize your architecture

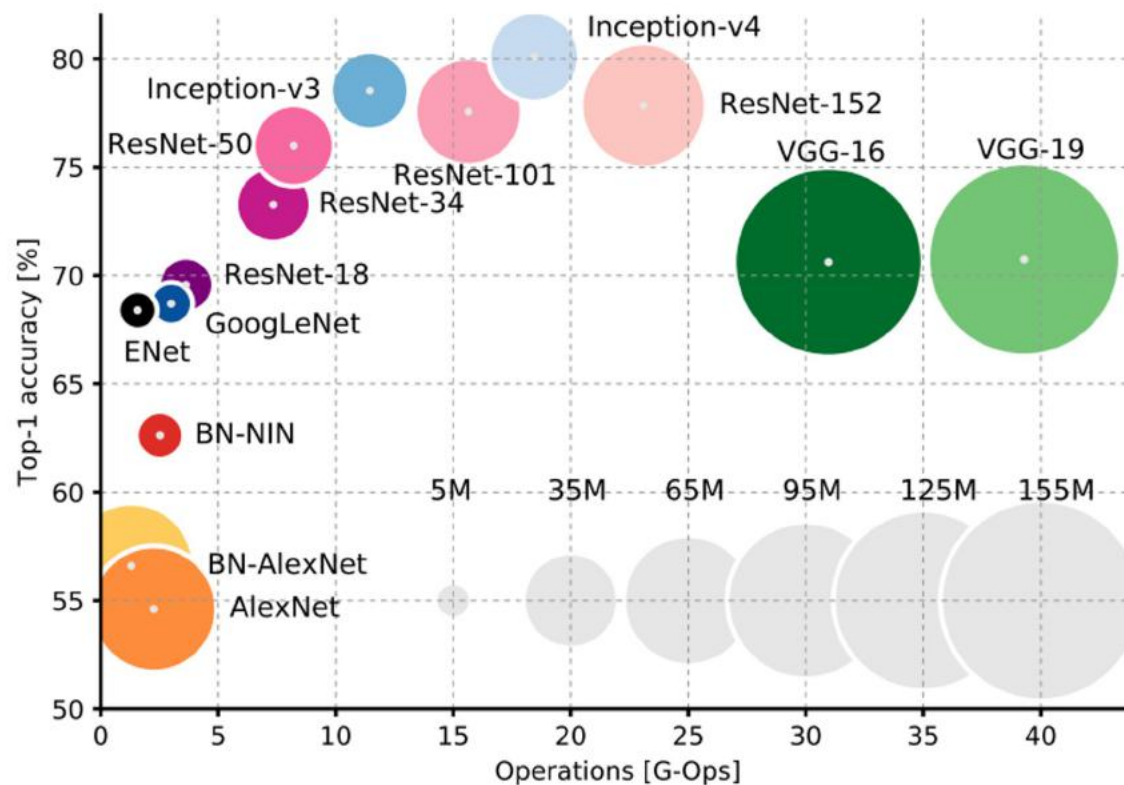
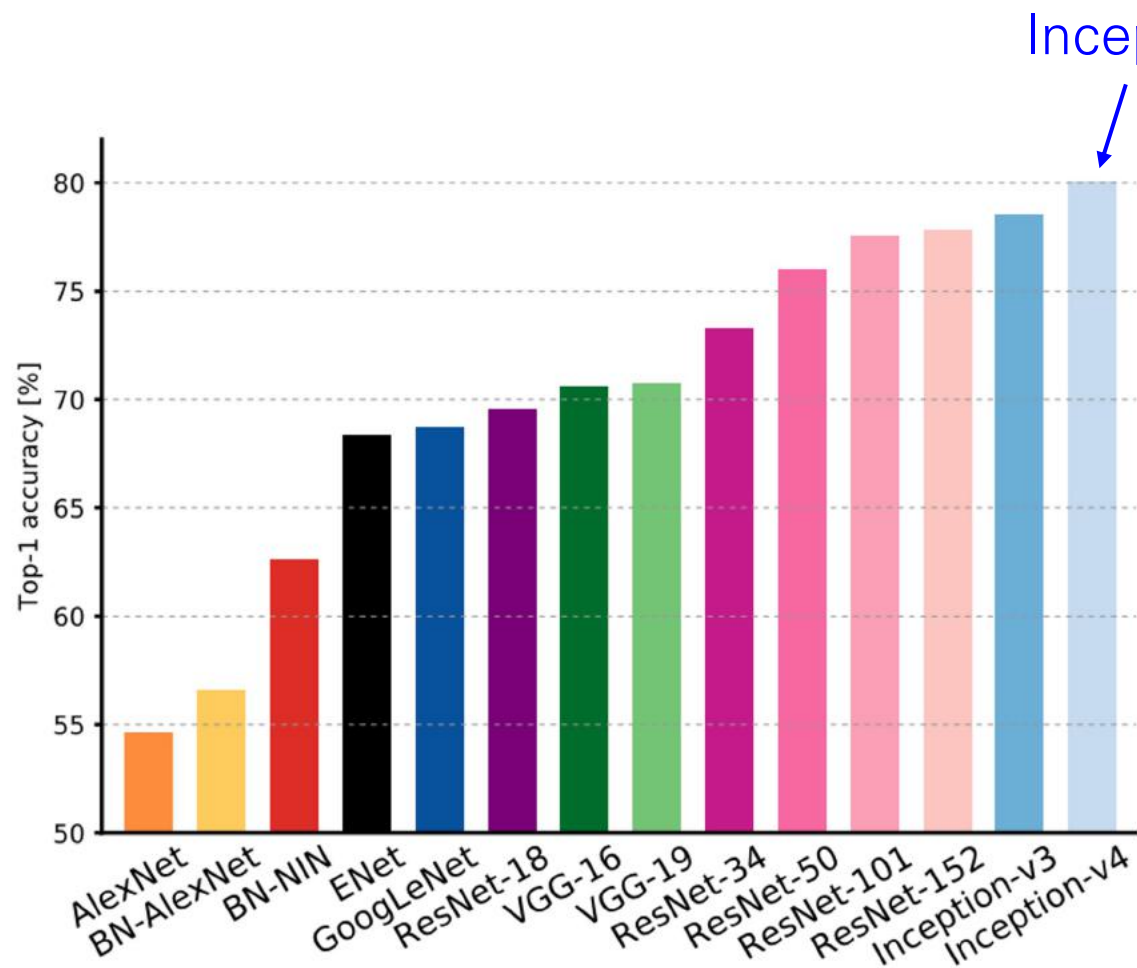
# Model Size

- Num. of parameters is about the same



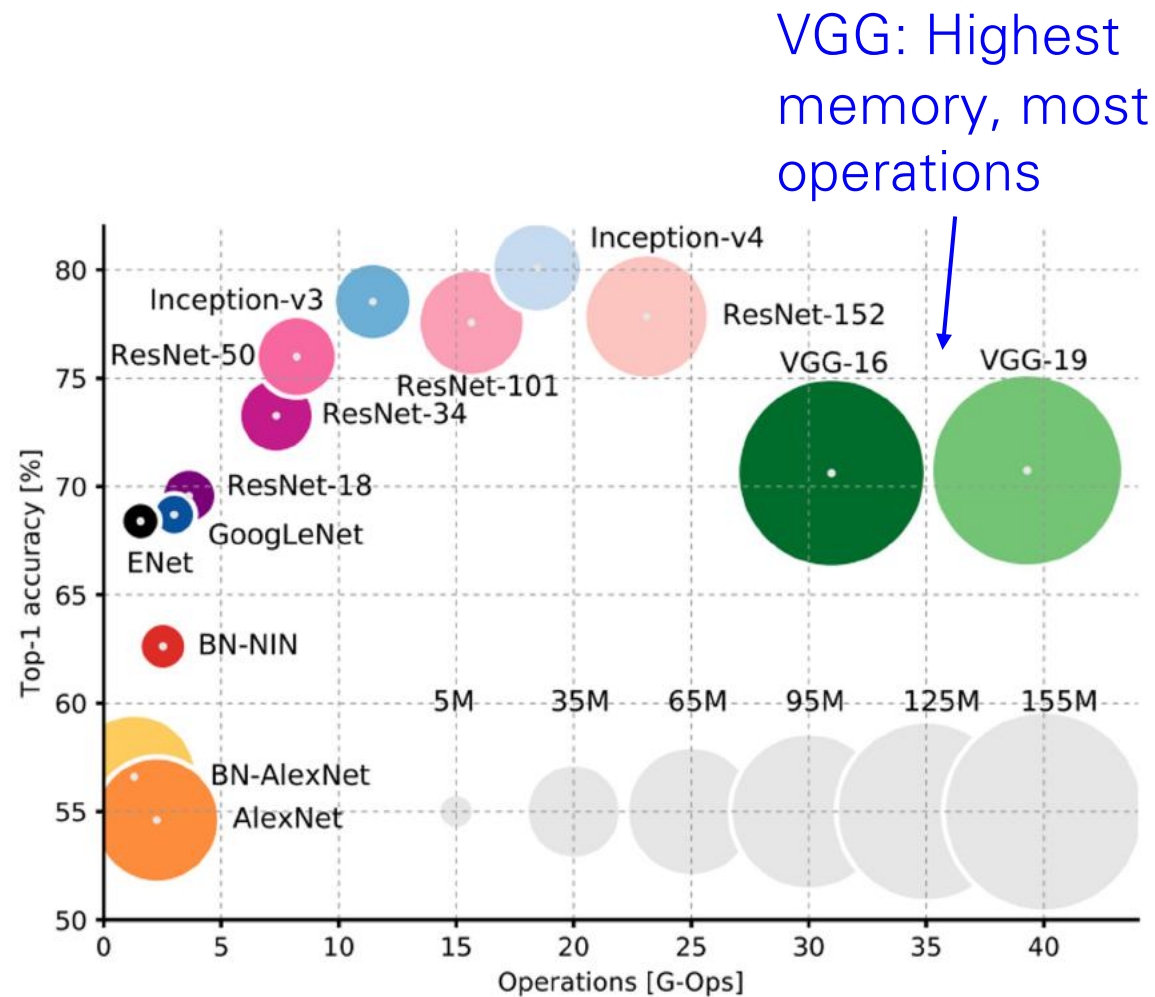
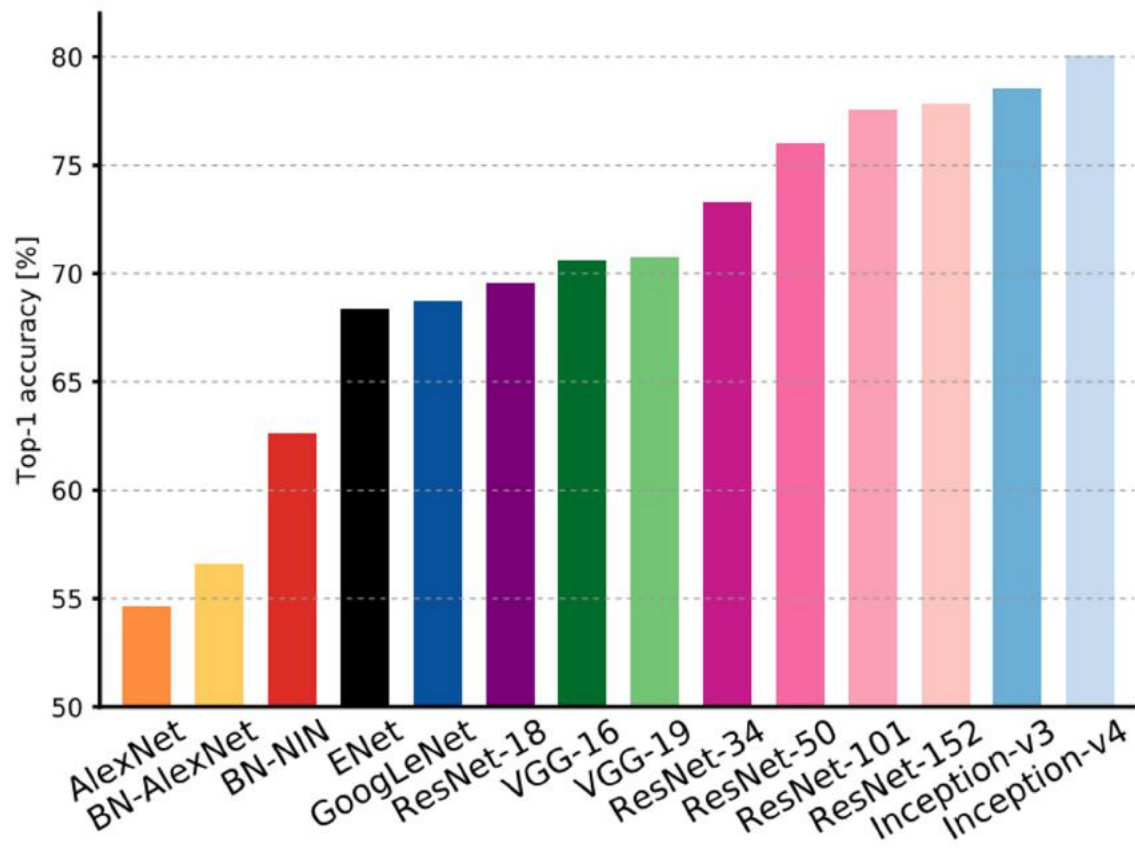
- **Remark:** 101 ResNet layers same size/speed as 16 VGG-VD layers
- **Reason:** Far fewer feature channels (quadratic speed/space gain)
- **Moral:** Optimize your architecture

# Comparing Complexity

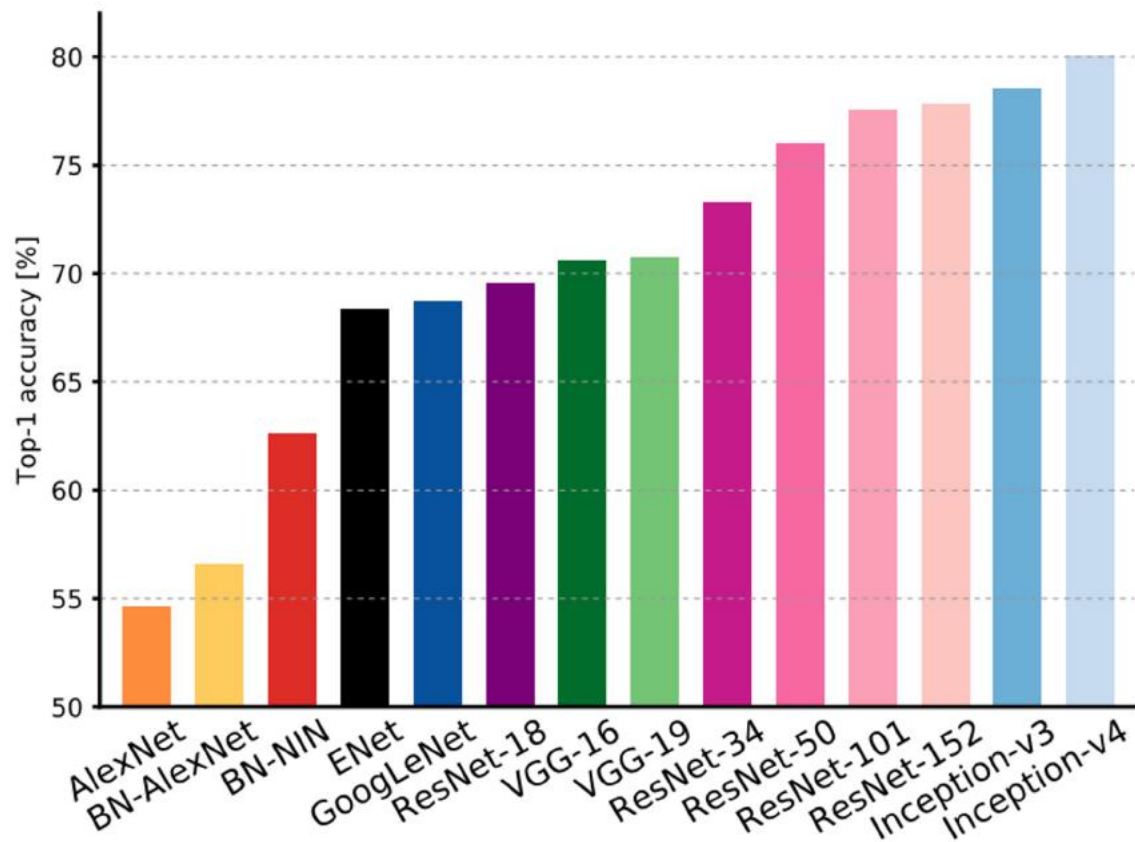




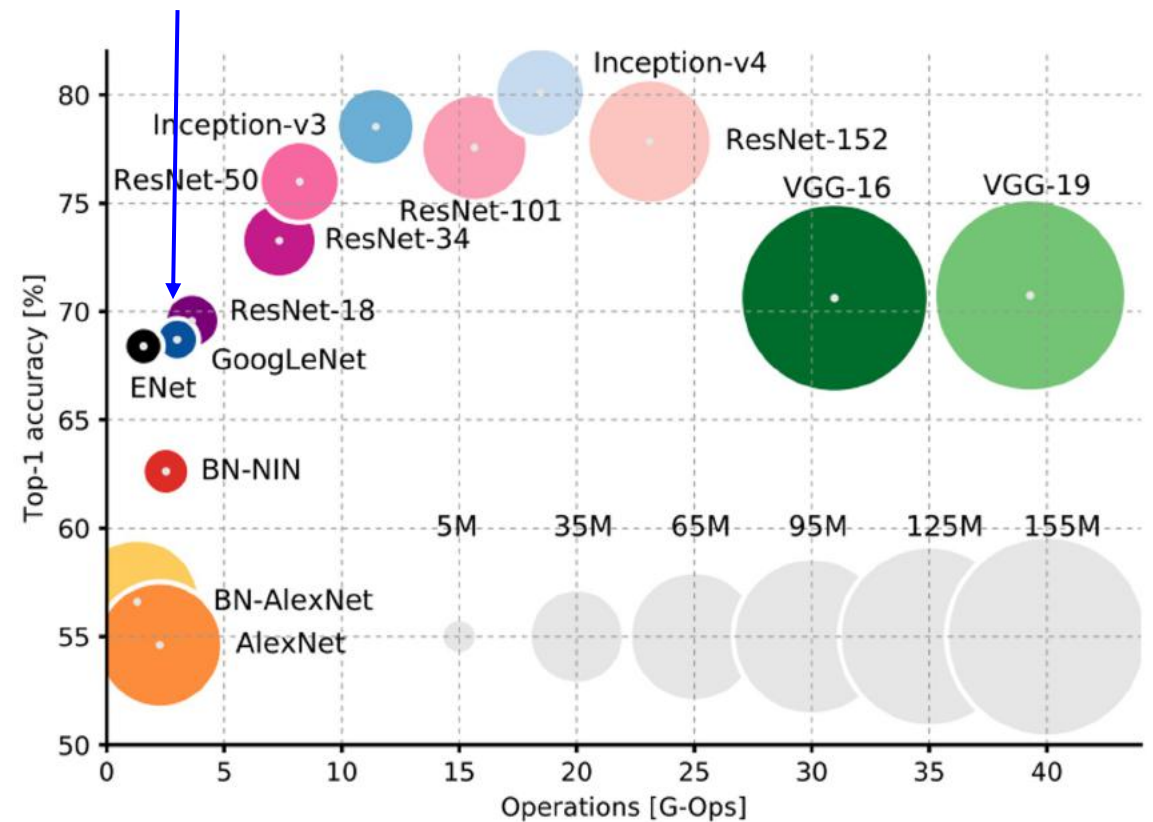
# Comparing Complexity



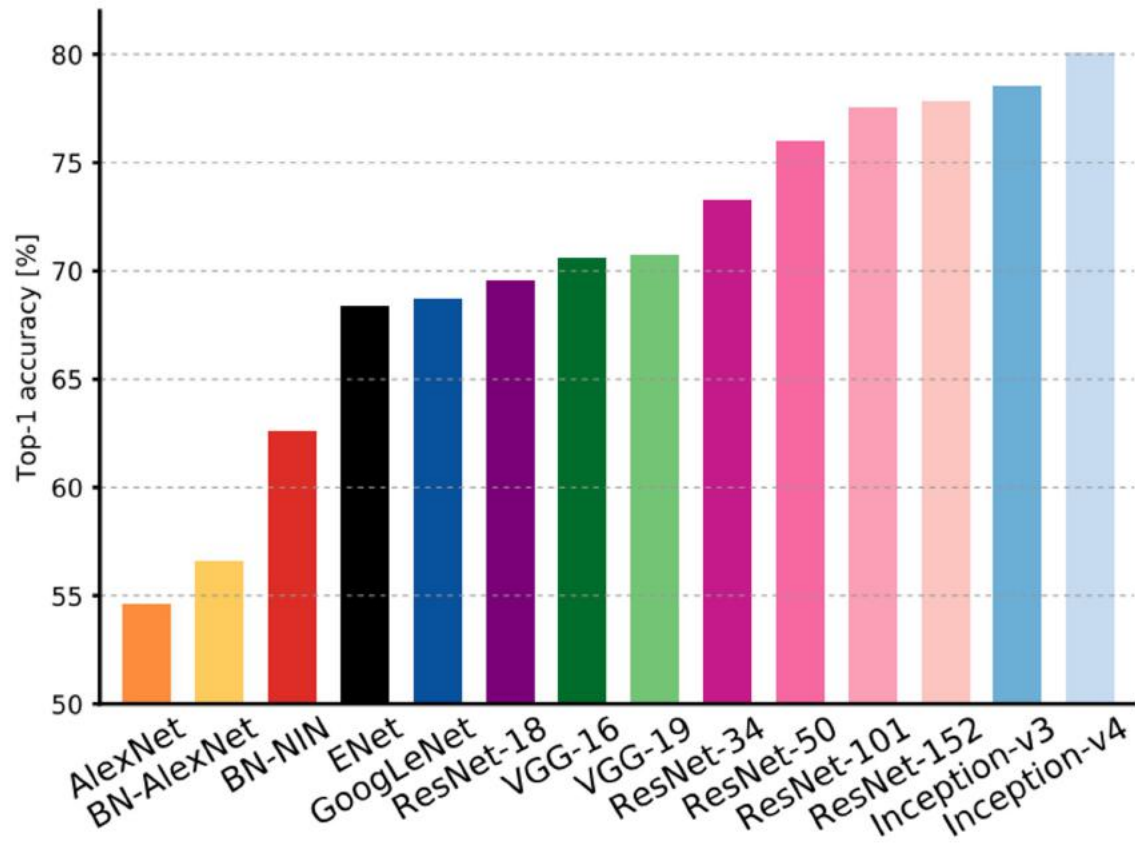
# Comparing Complexity



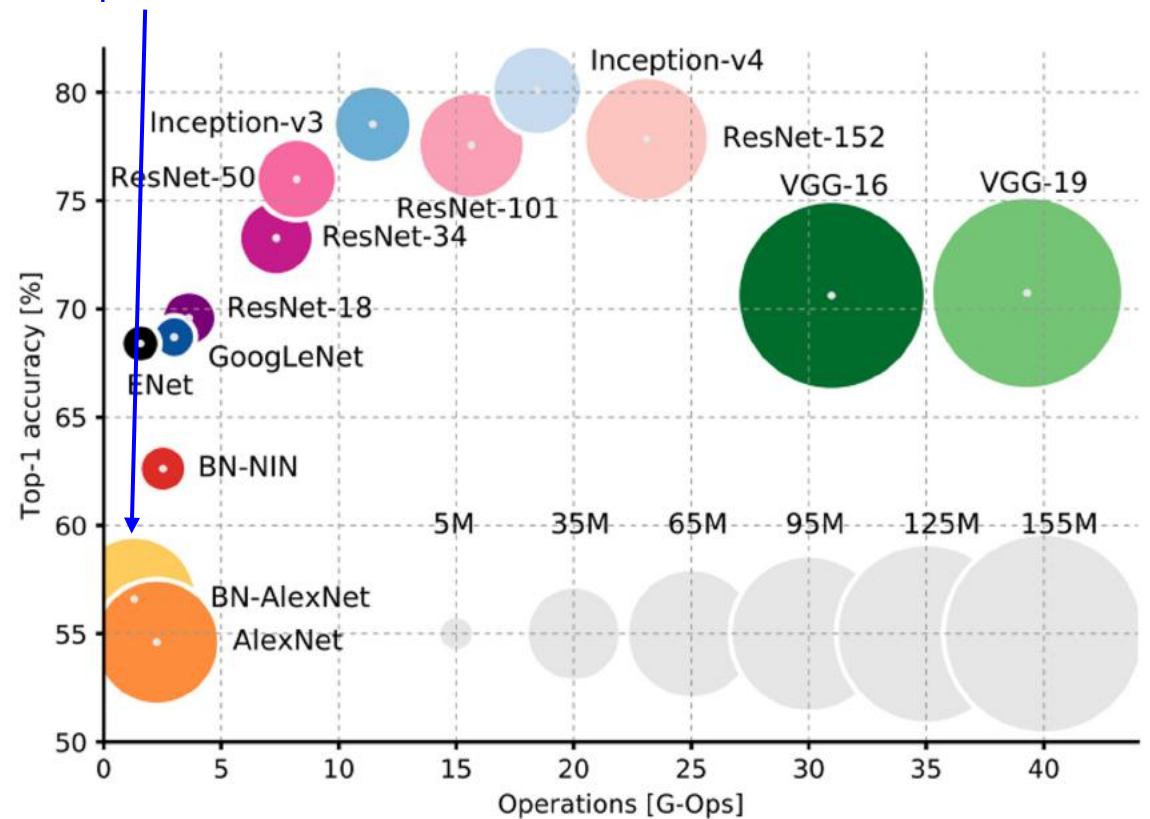
GoogLeNet:  
Very efficient!



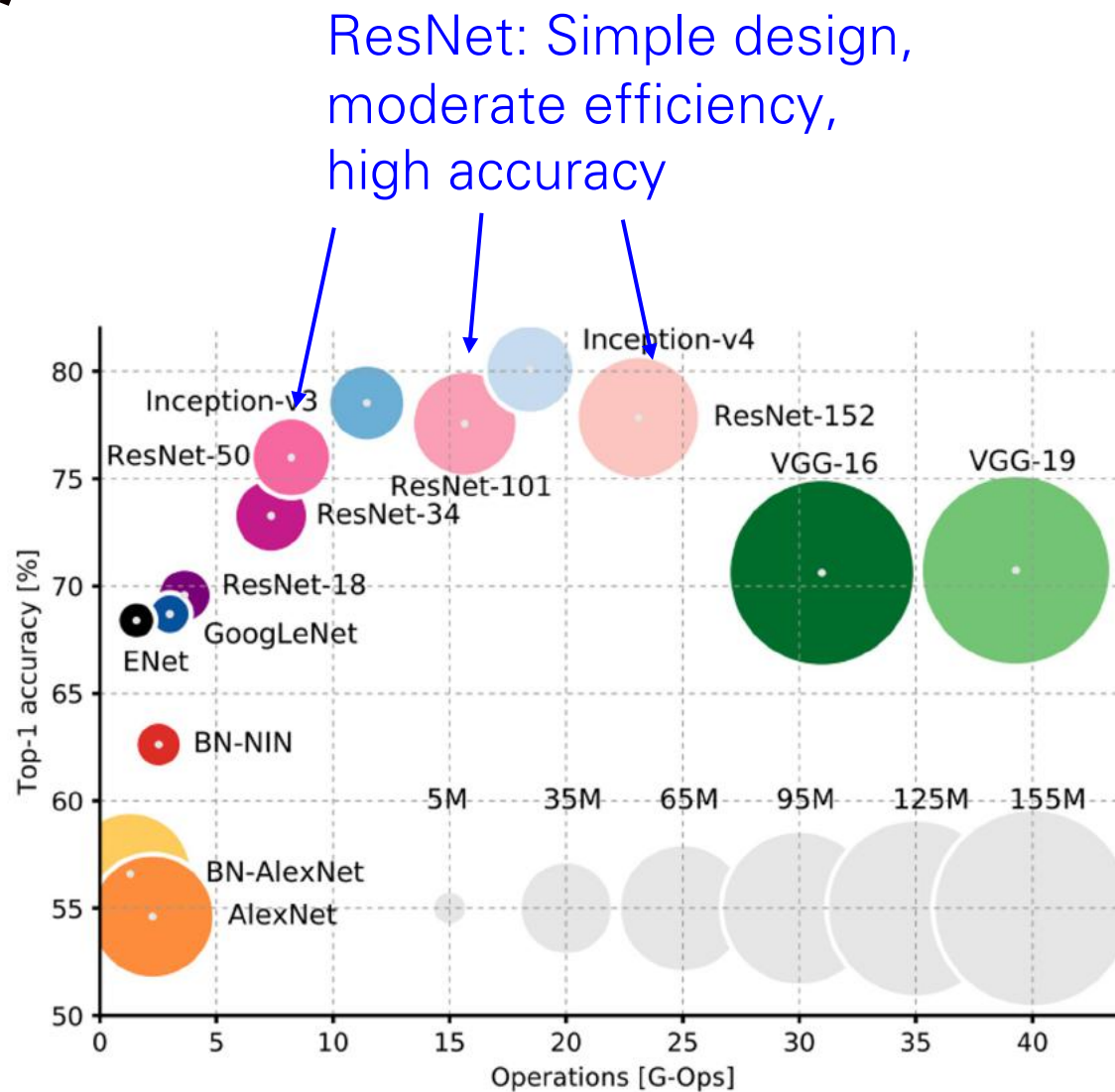
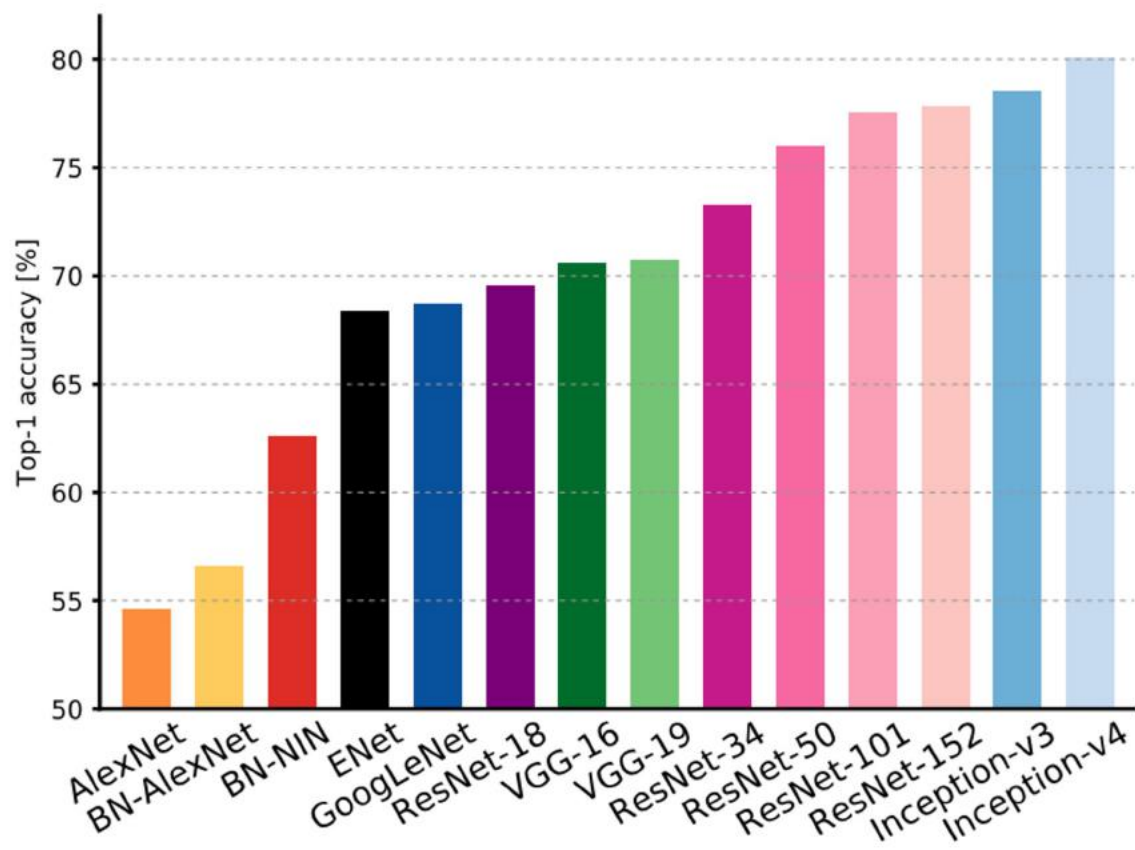
# Comparing Complexity



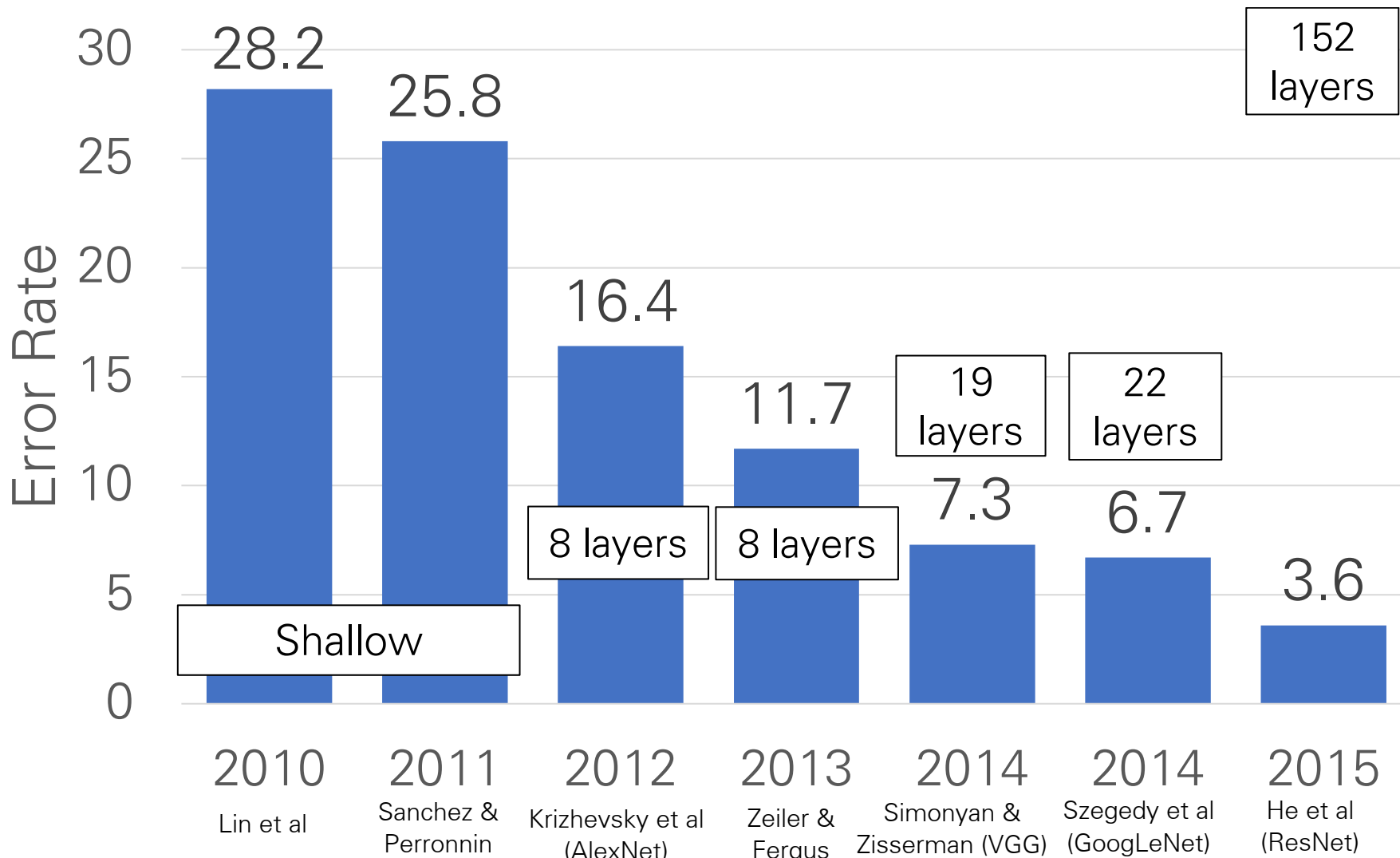
AlexNet: Low compute, lots of parameters



# Comparing Complexity



# ImageNet Classification Challenge

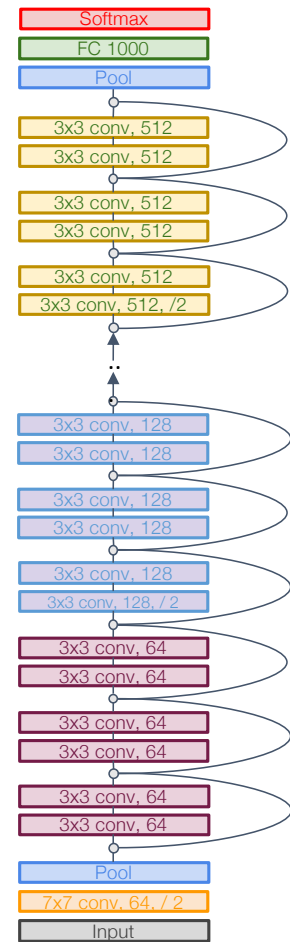
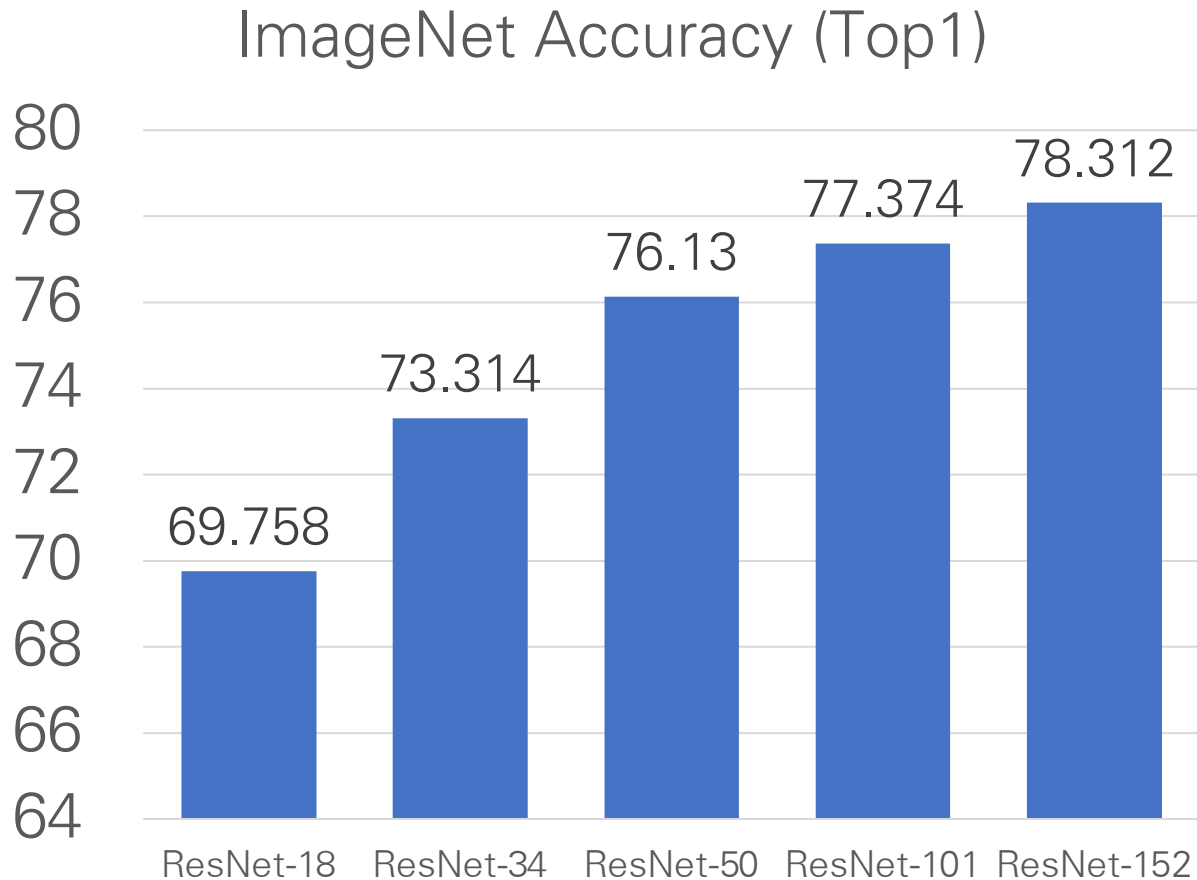


Today:  
More recent CNN  
architectures

# Post-ResNet Architectures

ResNet made it possible to increase accuracy with larger, deeper models

Many followup architectures emphasize **efficiency**: can we improve accuracy while controlling for model “complexity”?





# Measures of Model Complexity

**Parameters:** How many learnable parameters does the model have?

**Floating Point Operations (FLOPs):** How many arithmetic operations does it take to compute the forward pass of the model?

Watch out, lots of subtlety here:

- Many papers only count operations in conv layers (ignore ReLU, pooling, BatchNorm).

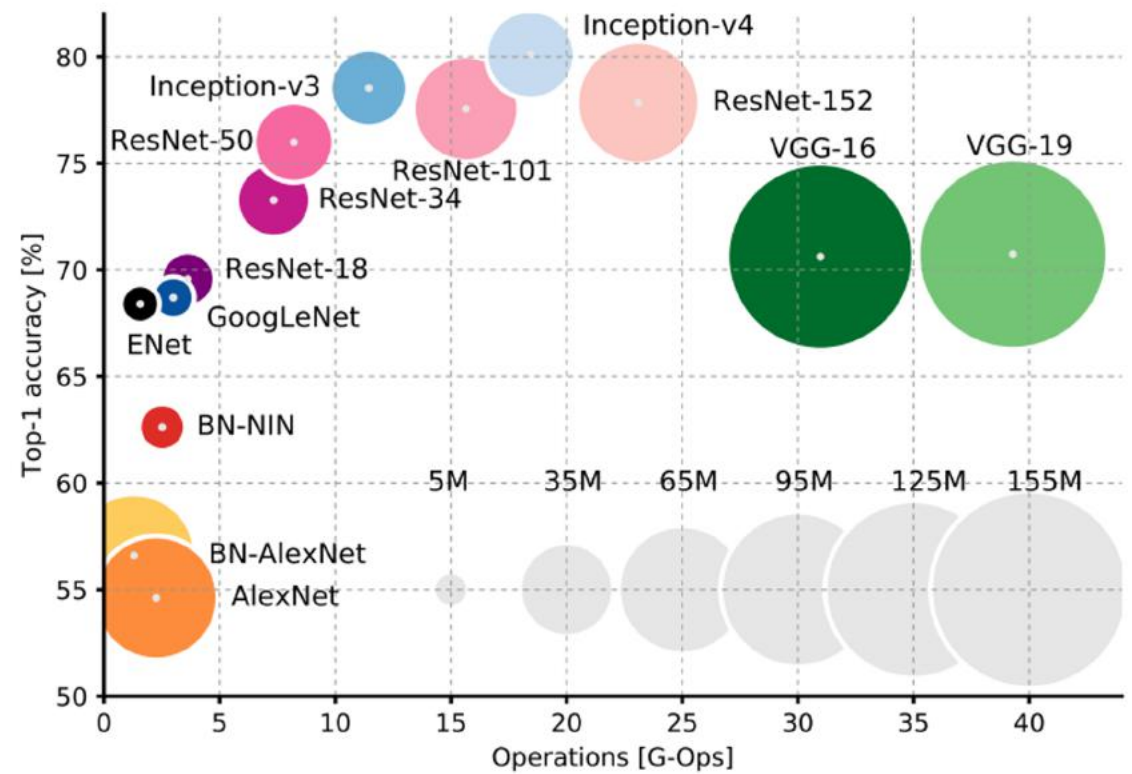
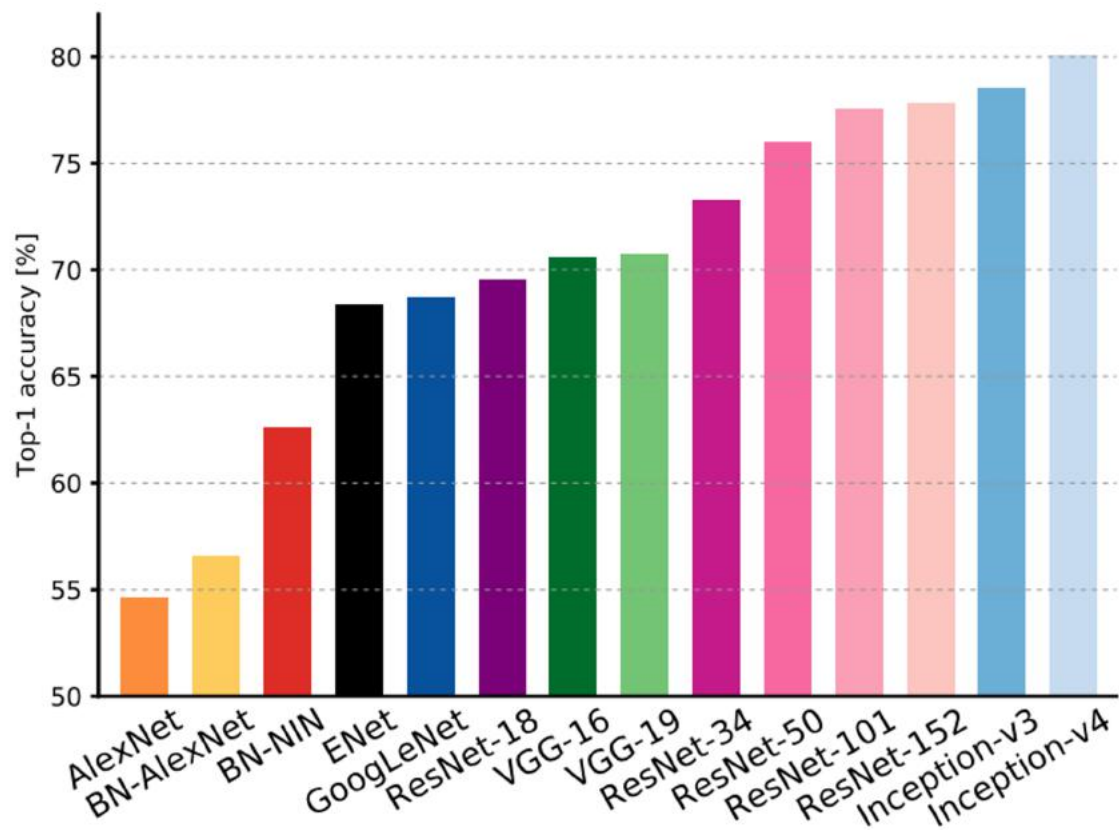
- Most papers use "1 FLOP" = "1 multiply and 1 addition" so dot product of two N-dim vectors takes N FLOPs; some papers say MADD or MACC instead of FLOP

- Other sources (e.g. NVIDIA marketing material) count "1 multiply and one addition" = 2 FLOPs, so dot product of two N-dim vectors takes 2N FLOPs

**Network Runtime:** How long does a forward pass of the model take on real hardware?



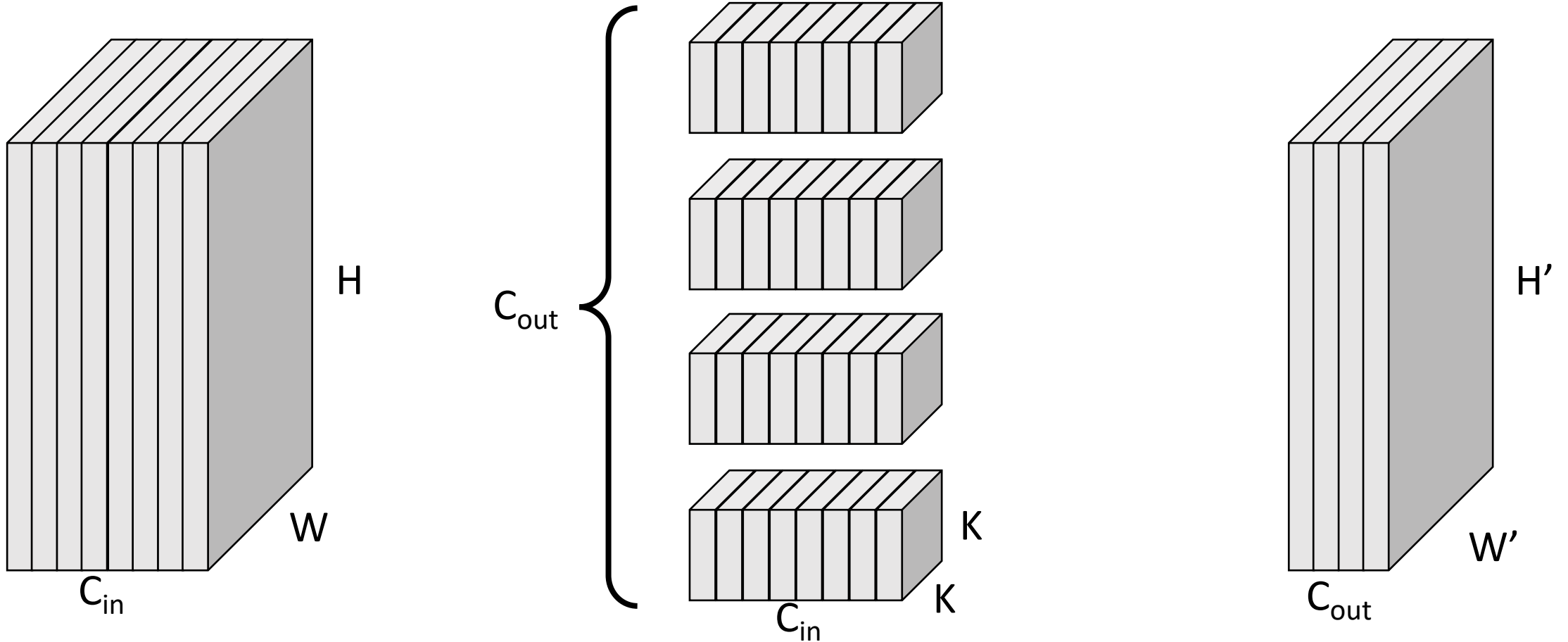
# Comparing Complexity



**Key ingredient:**  
**Grouped / Separable convolution**

# Recall: Convolution Layer

Each filter has the same number of channels as the input



Input:  $C_{in} \times H \times W$

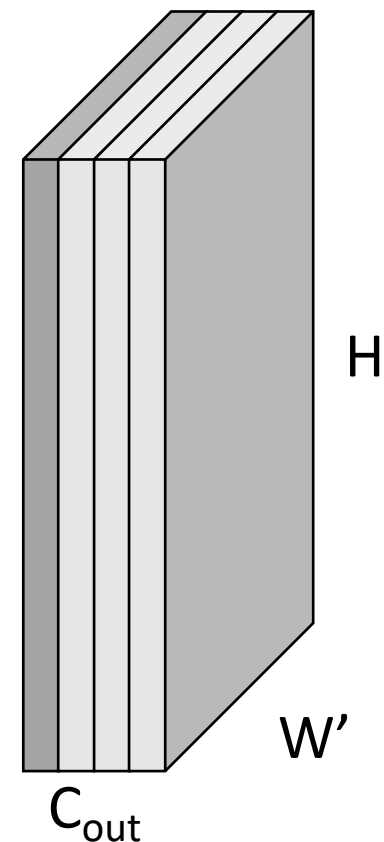
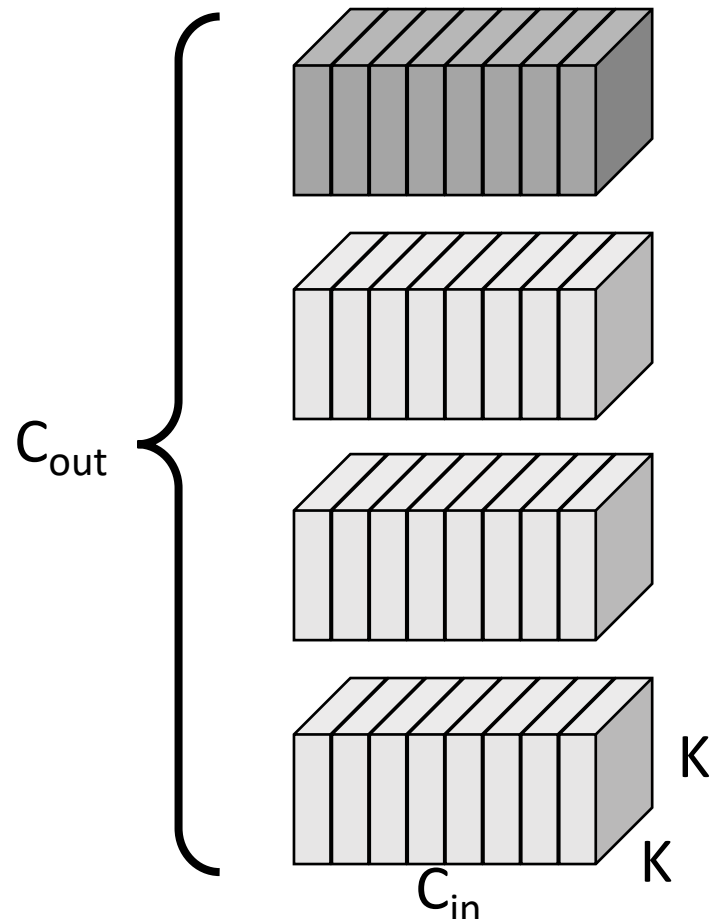
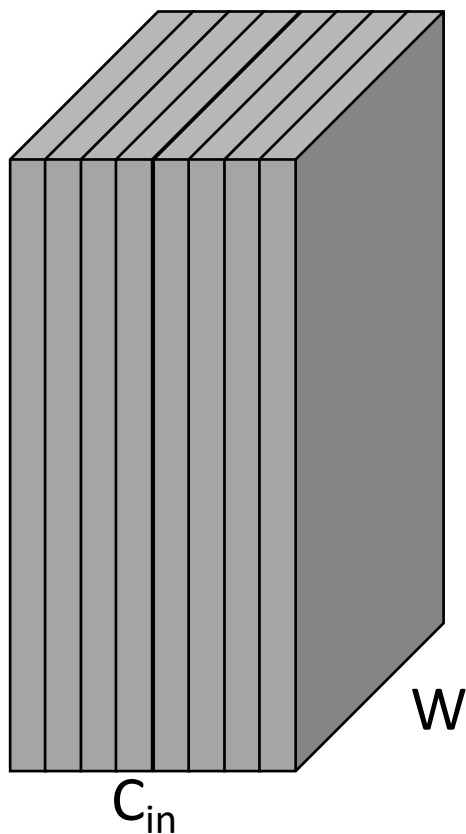
Weights:  $C_{out} \times C_{in} \times K \times K$

Output:  $C_{out} \times H' \times W'$

# Recall: Convolution Layer

Each filter has the same number of channels as the input

Each plane of the output depends on the full input and one filter



Input:  $C_{in} \times H \times W$

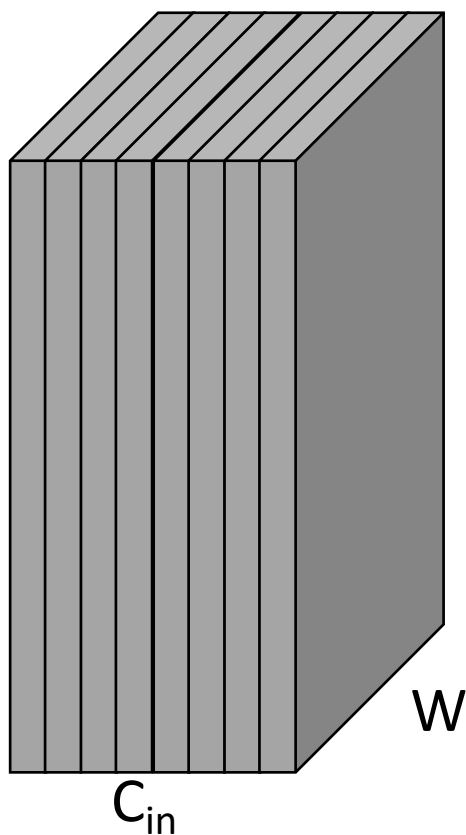
Weights:  $C_{out} \times C_{in} \times K \times K$

Output:  $C_{out} \times H' \times W'$

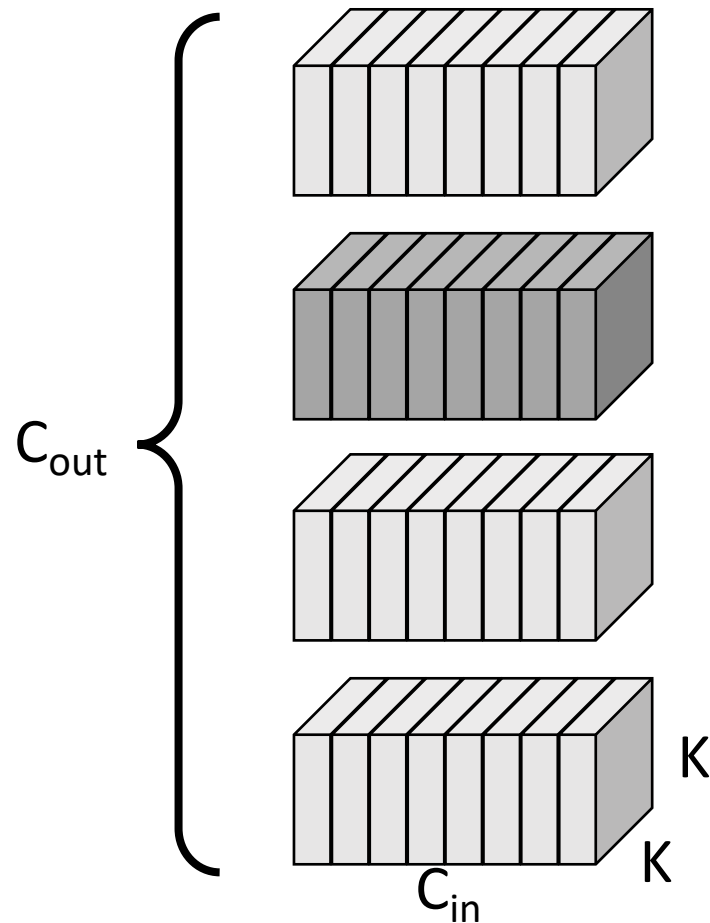
# Recall: Convolution Layer

Each filter has the same number of channels as the input

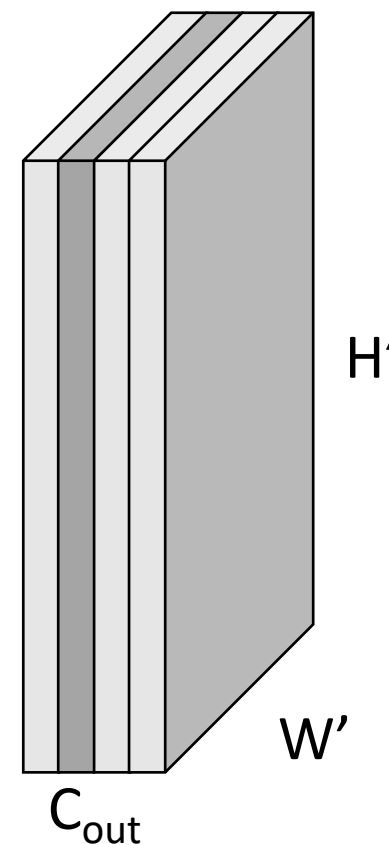
Each plane of the output depends on the full input and one filter



Input:  $C_{in} \times H \times W$



Weights:  $C_{out} \times C_{in} \times K \times K$

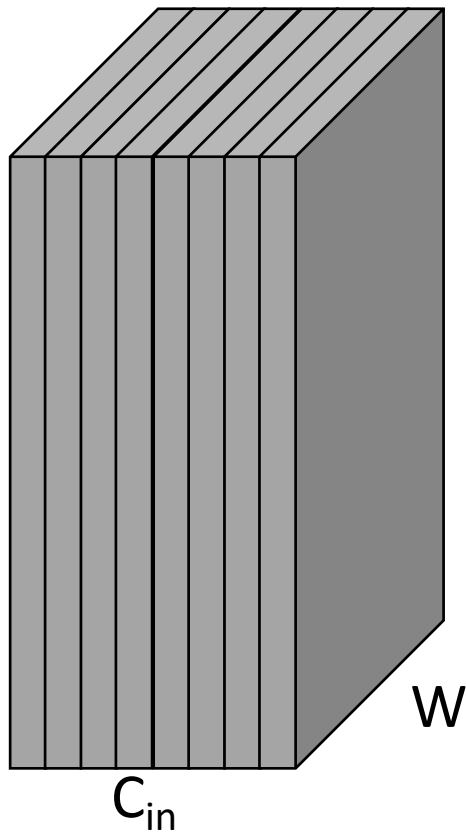


Output:  $C_{out} \times H' \times W'$

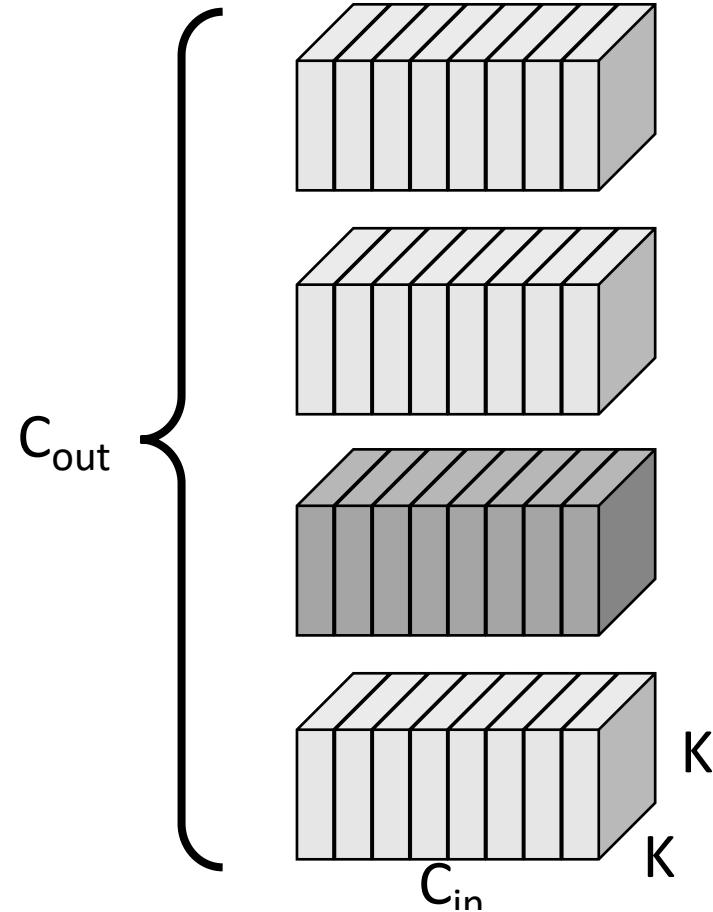
# Recall: Convolution Layer

Each filter has the same number of channels as the input

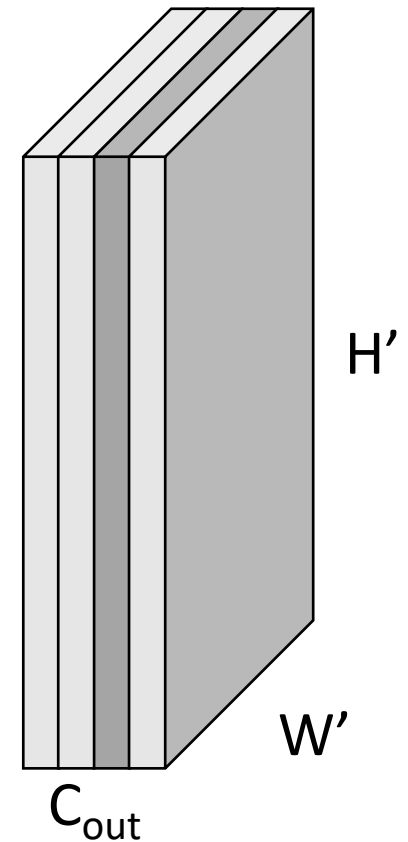
Each plane of the output depends on the full input and one filter



Input:  $C_{in} \times H \times W$



Weights:  $C_{out} \times C_{in} \times K \times K$

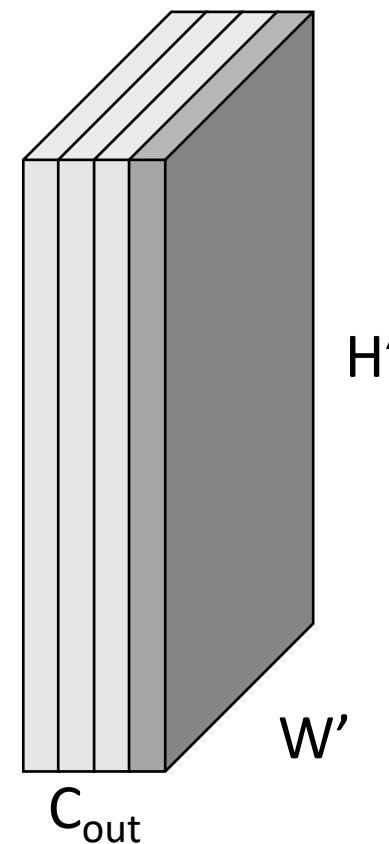
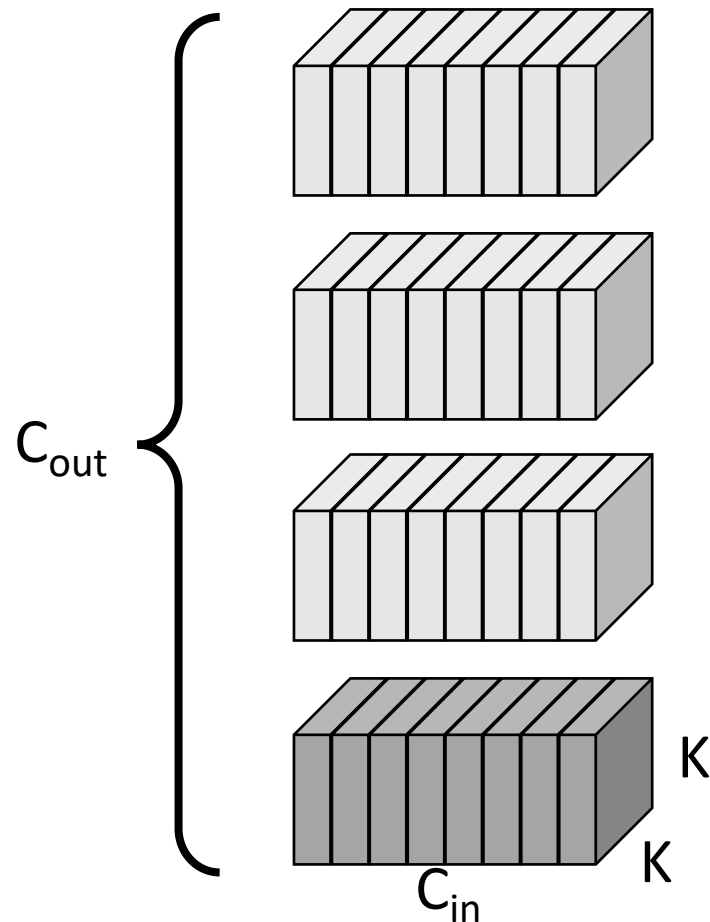
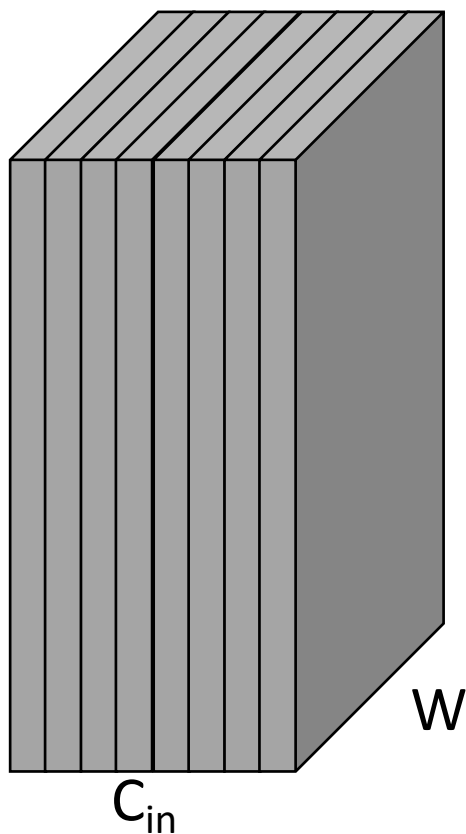


Output:  $C_{out} \times H' \times W'$

# Recall: Convolution Layer

Each filter has the same number of channels as the input

Each plane of the output depends on the full input and one filter



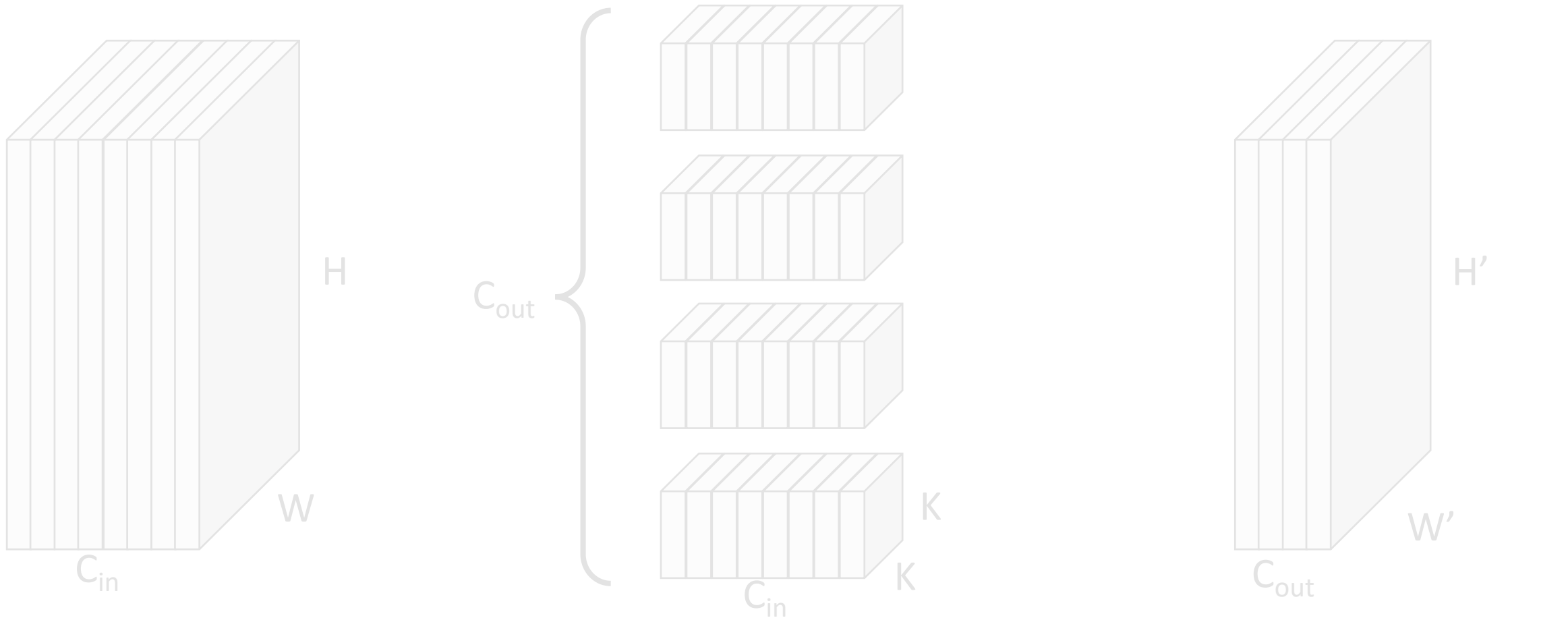
Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

Output:  $C_{out} \times H' \times W'$



# Grouped Convolution



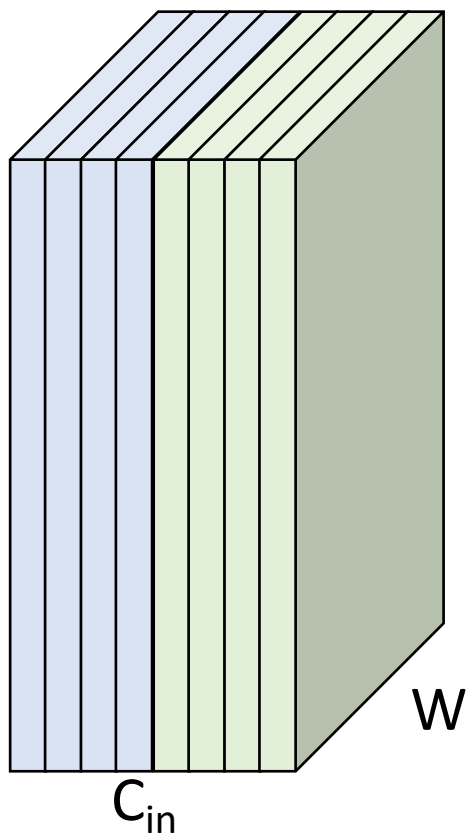
Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

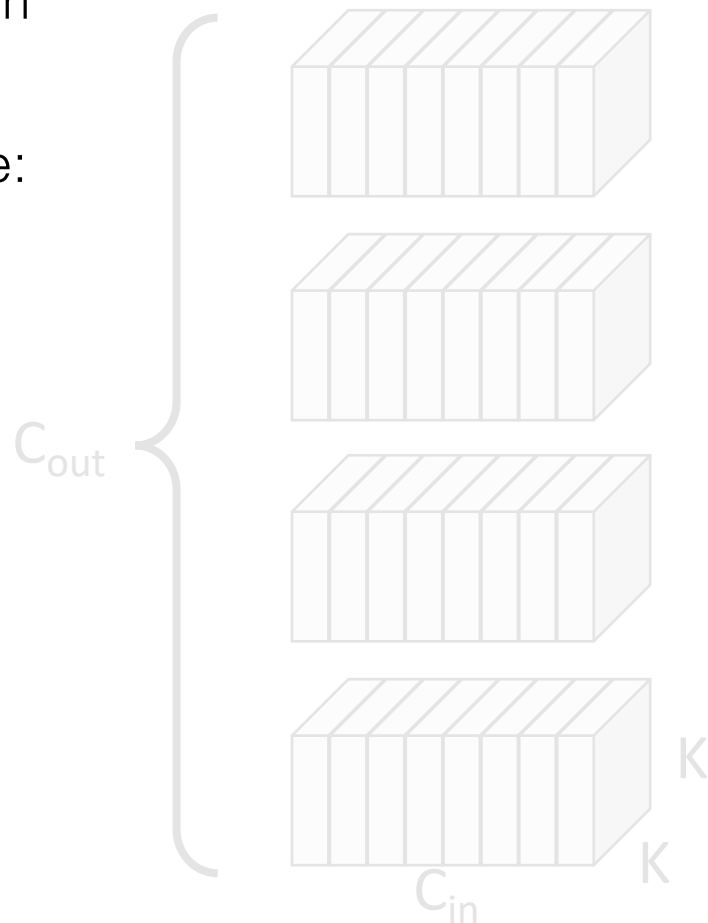
Output:  $C_{out} \times H' \times W'$

# Grouped Convolution

Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each



Example:  
 $G=2$



Input:  $C_{in} \times H \times W$

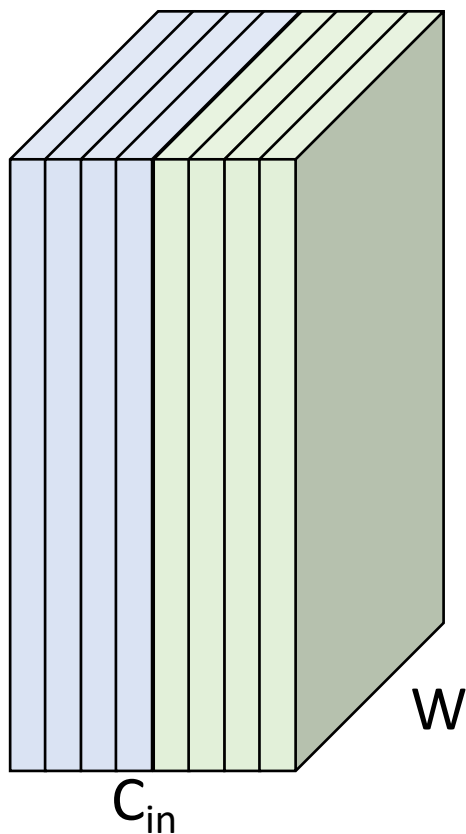
Weights:  $C_{out} \times C_{in} \times K \times K$

Output:  $C_{out} \times H' \times W'$

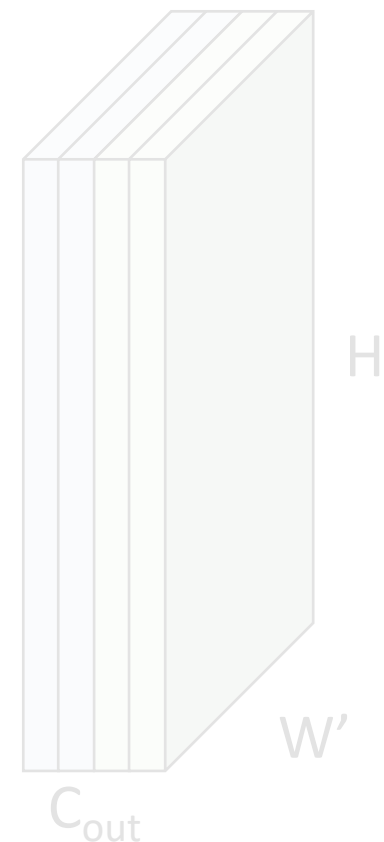
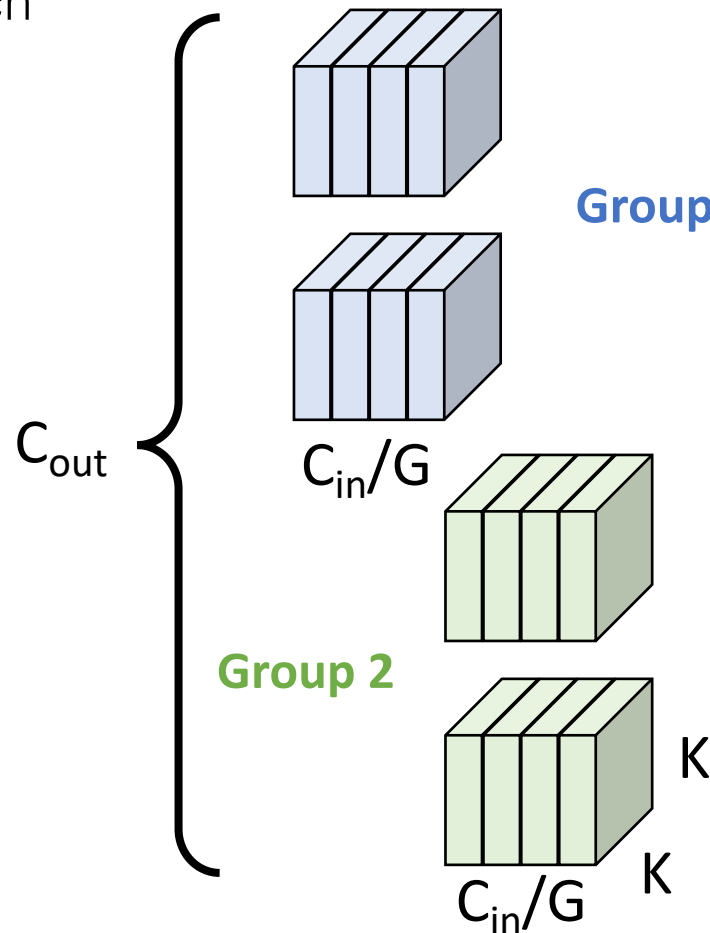
# Grouped Convolution

Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each



Example:  
 $G = 2$



Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$

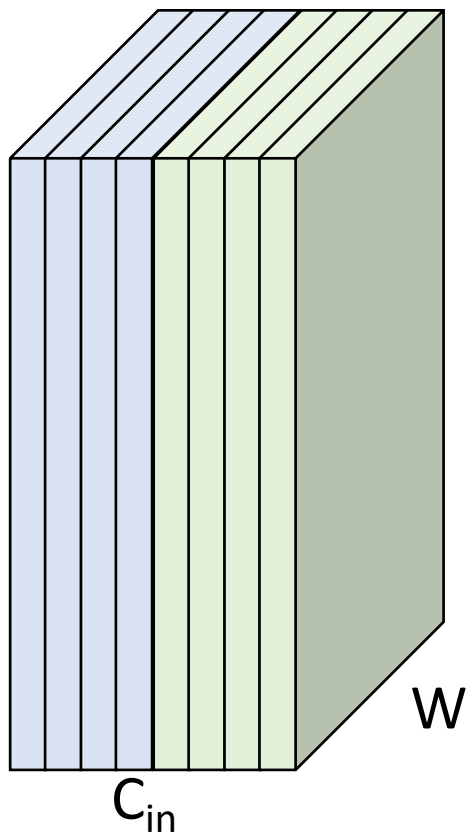
Output:  $C_{out} \times H' \times W'$

# Grouped Convolution

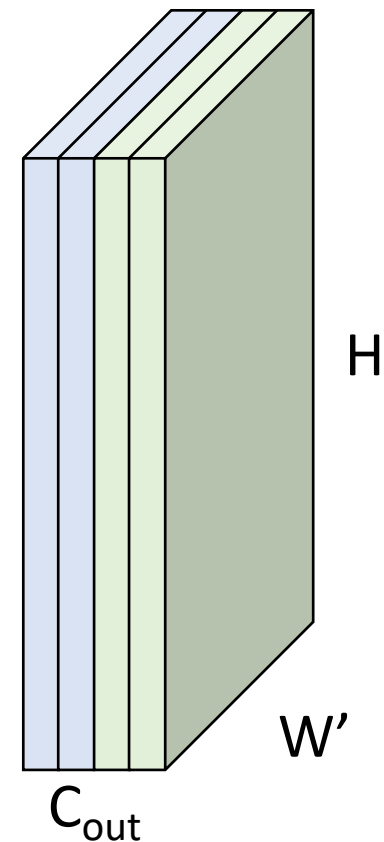
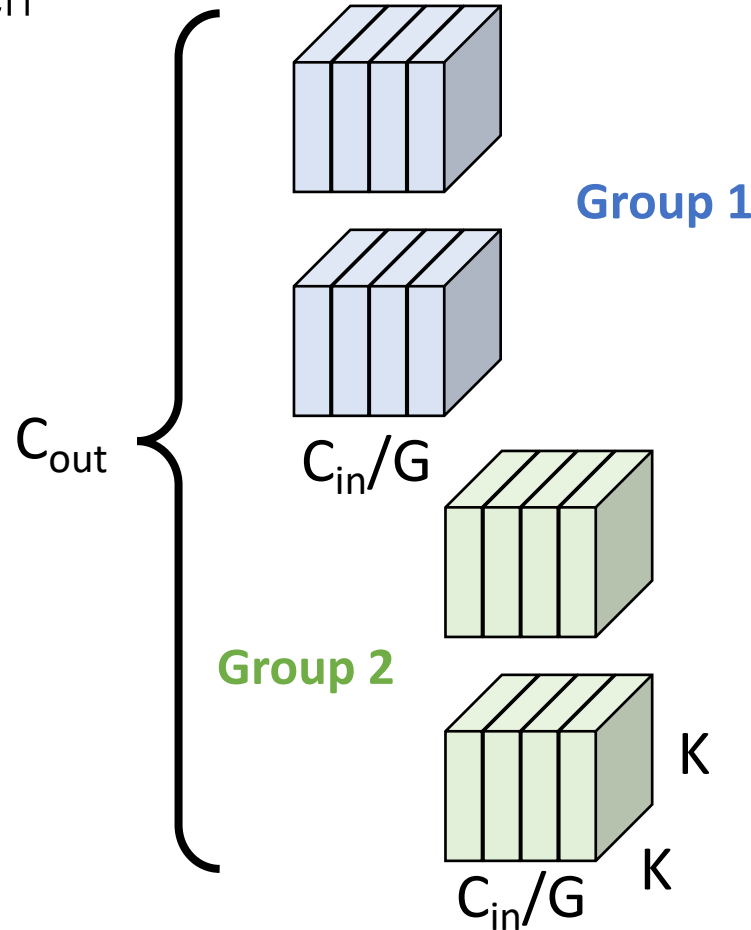
Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels

Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each



Example:  
 $G = 2$



Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times (C_{in}/G) \times K \times K$

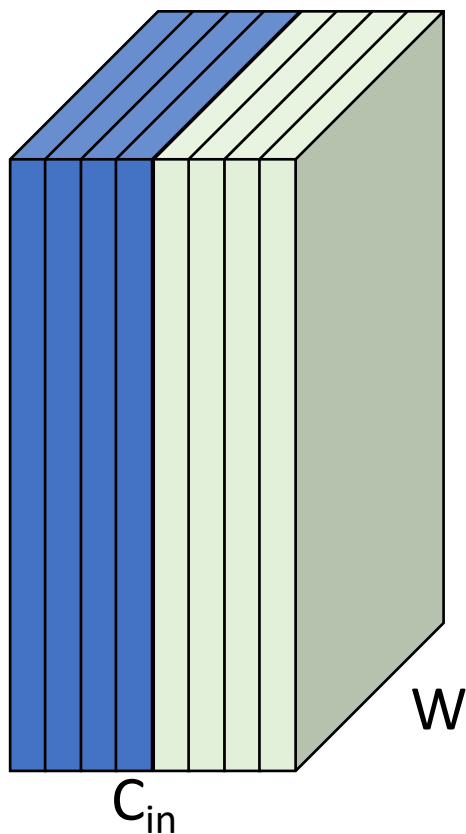
Output:  $C_{out} \times H' \times W'$

# Group Convolution

Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each

Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels

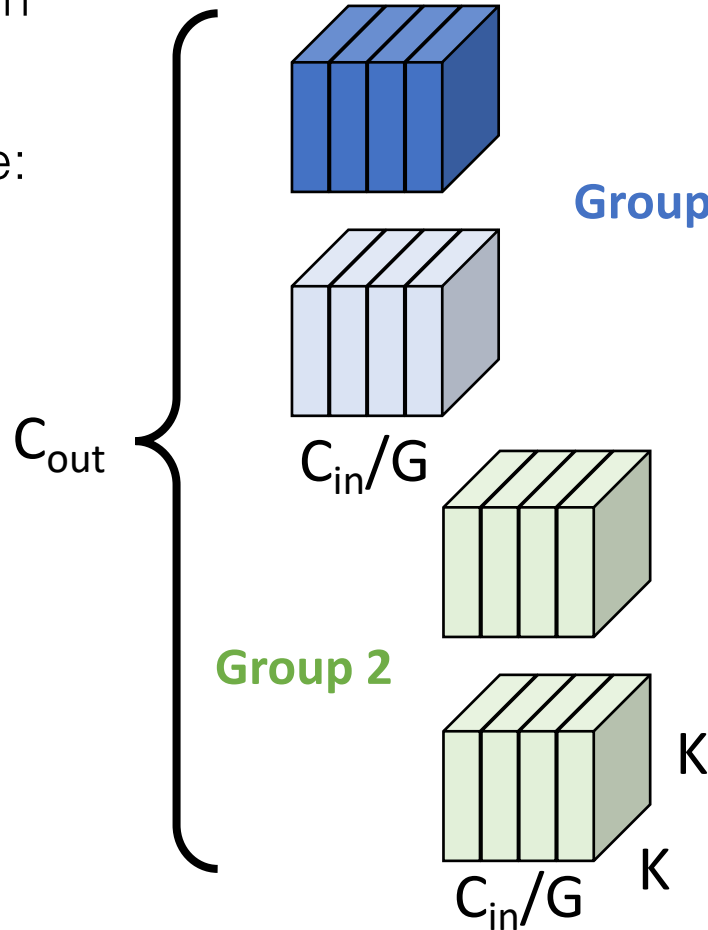


Example:  
 $G=2$

$H$

$W$

$C_{in}$



Group 1

Group 2

$C_{out}$

$C_{in}/G$

$K$

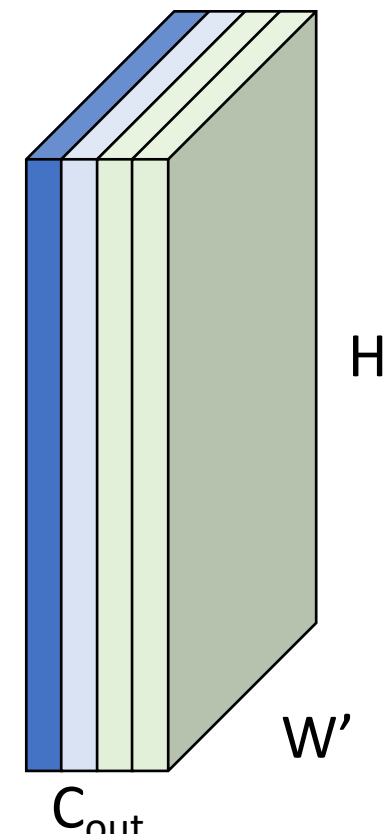
$K$

$C_{in}/G$

Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

Output:  $C_{out} \times H' \times W'$



$H'$

$W'$

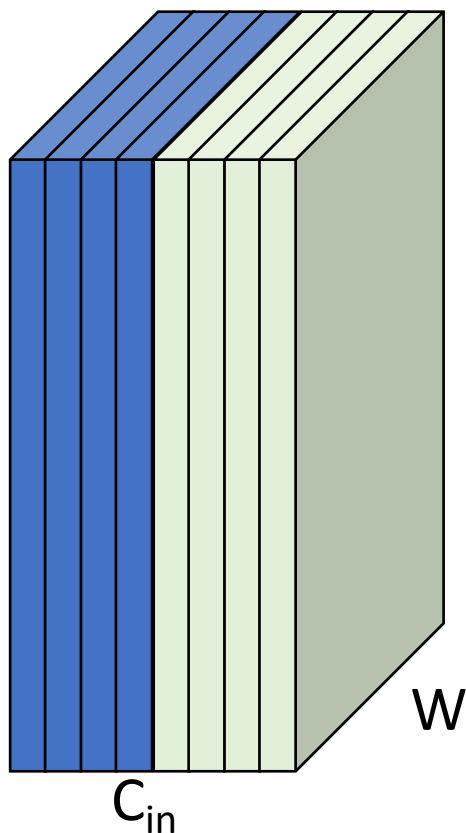
$C_{out}$

# Group Convolution

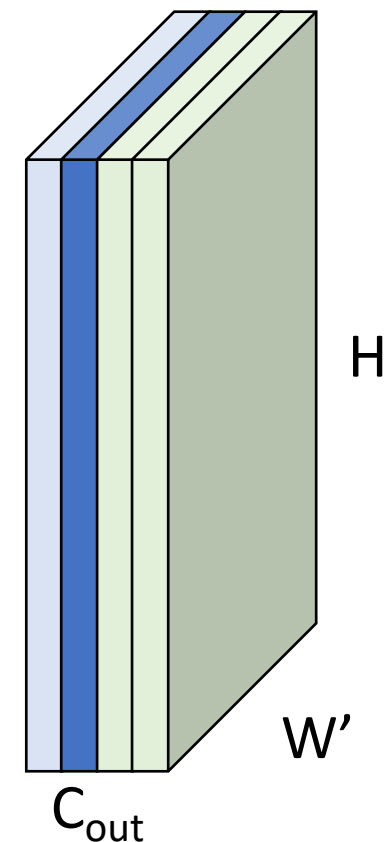
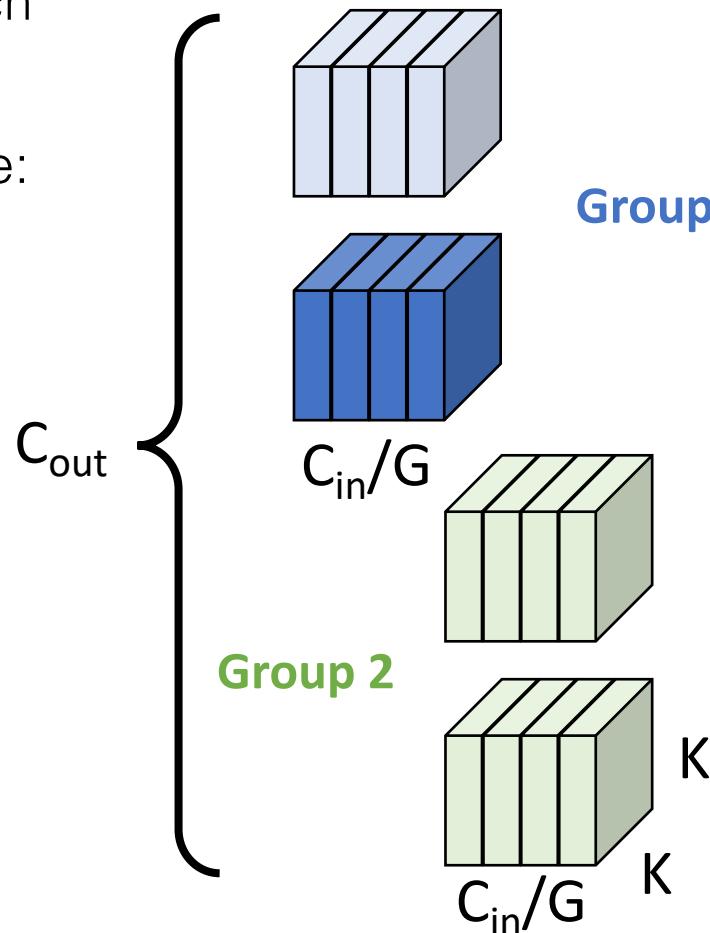
Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each

Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels



Example:  
 $G=2$



Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

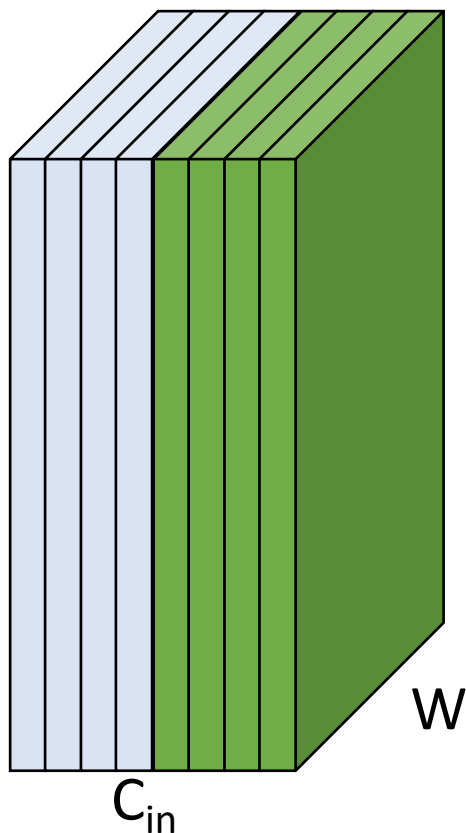
Output:  $C_{out} \times H' \times W'$

# Group Convolution

Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each

Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels

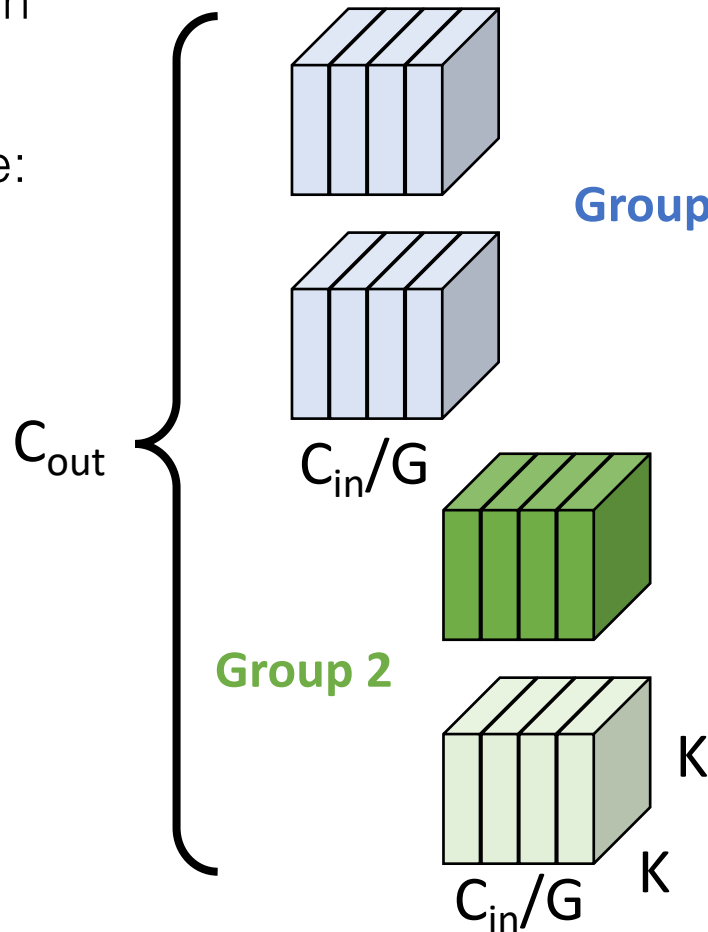


Example:  
 $G=2$

$H$

$W$

$C_{in}$



Group 1

Group 2

$C_{in}/G$

$C_{in}/G$

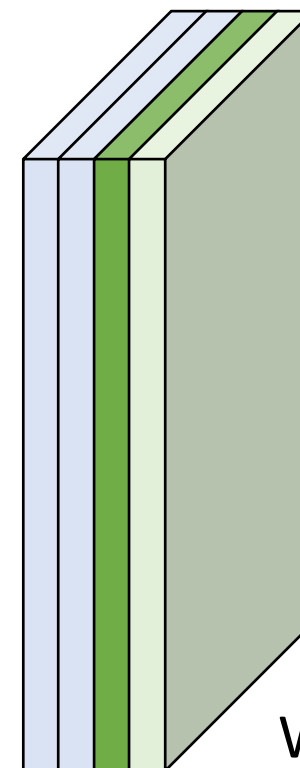
$K$

$K$

$H'$

$W'$

$C_{out}$



Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

Output:  $C_{out} \times H' \times W'$

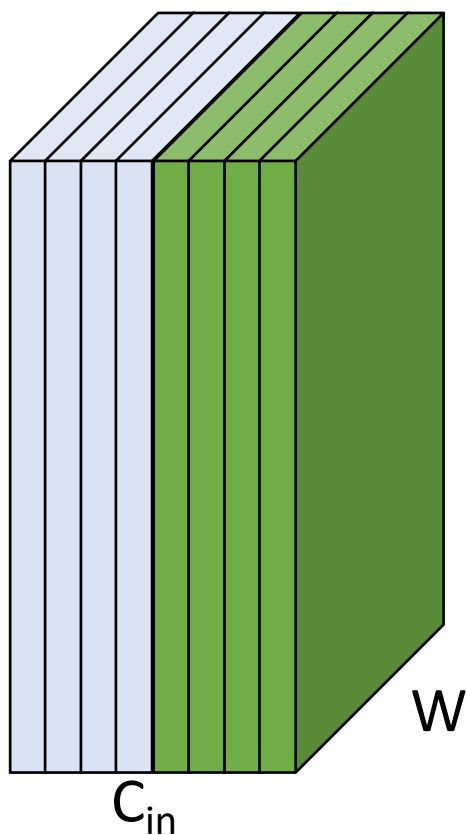


# Group Convolution

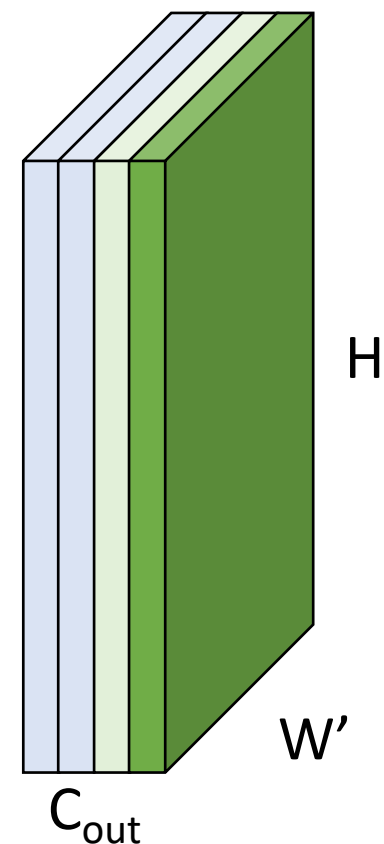
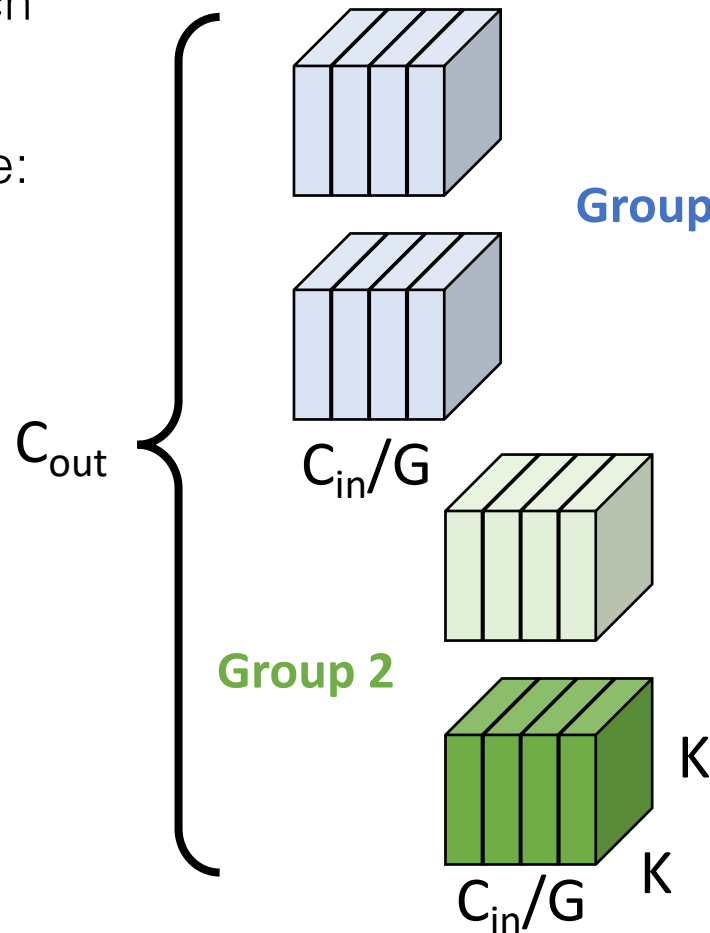
Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each

Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels



Example:  
 $G=2$



Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

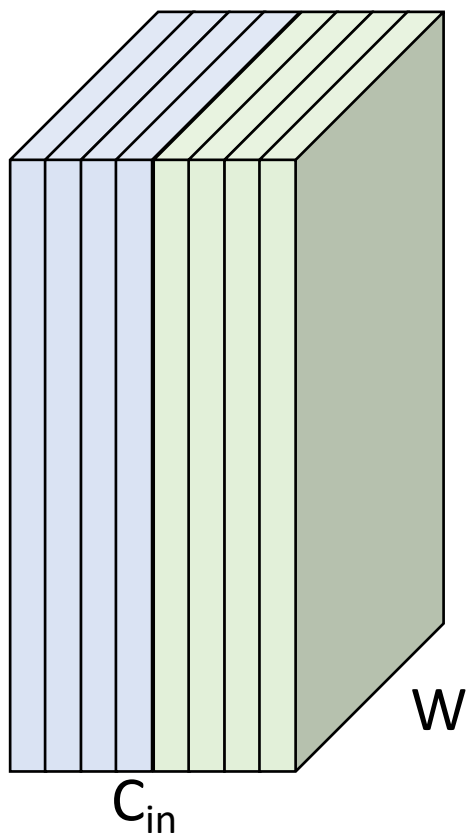
Output:  $C_{out} \times H' \times W'$

# Group Convolution

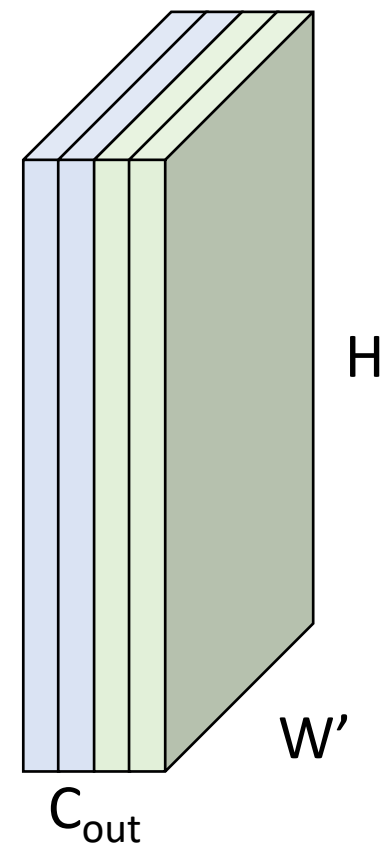
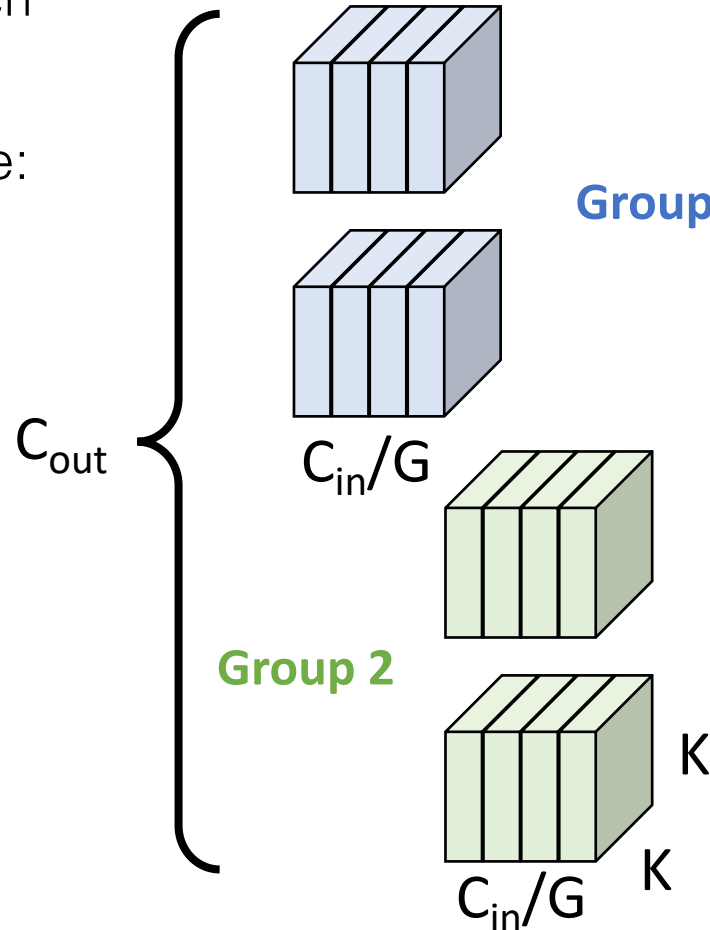
Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each

Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels



Example:  
 $G=2$



Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

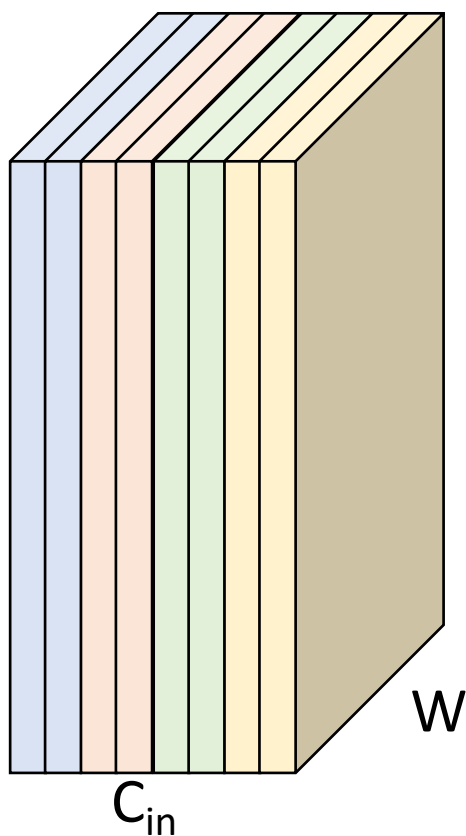
Output:  $C_{out} \times H' \times W'$

# Group Convolution

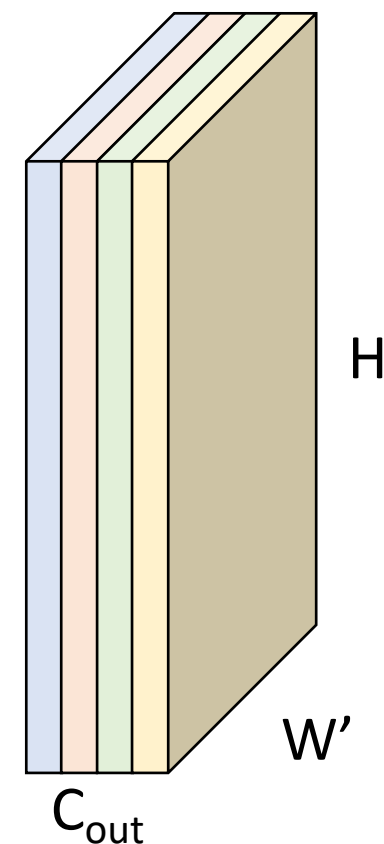
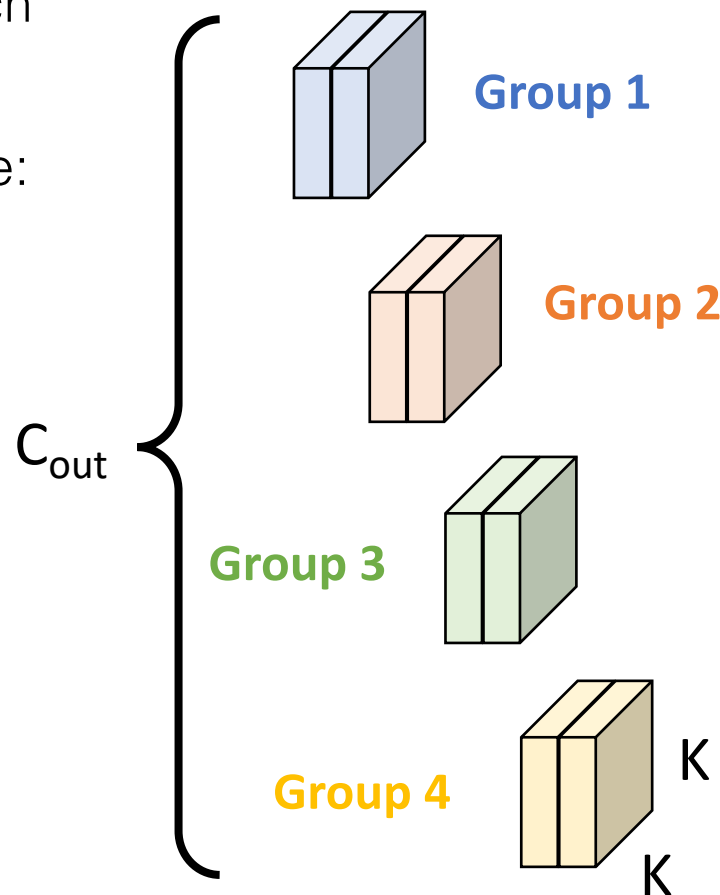
Divide channels of input into  $G$  groups with  $(C_{in}/G)$  channels each

Divide filters into  $G$  groups; each group looks at a **subset** of input channels

Each plane of the output depends on one filter and a **subset** of the input channels



Example:  
 $G=4$



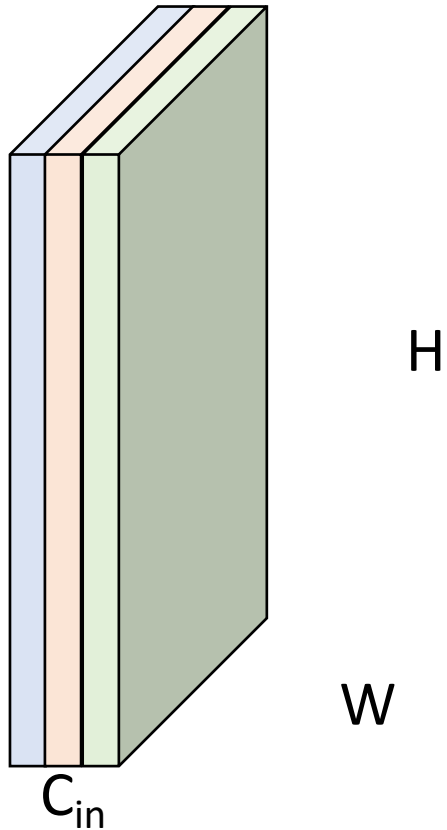
Input:  $C_{in} \times H \times W$

Weights:  $C_{out} \times C_{in} \times K \times K$

Output:  $C_{out} \times H' \times W'$

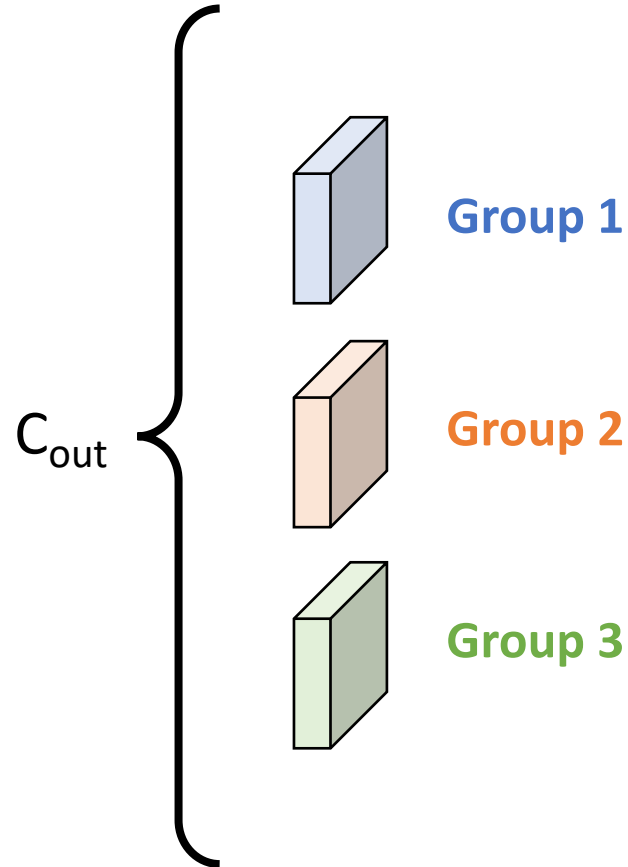
# Special Case: Depthwise Convolution

Number of groups equals number of input channels



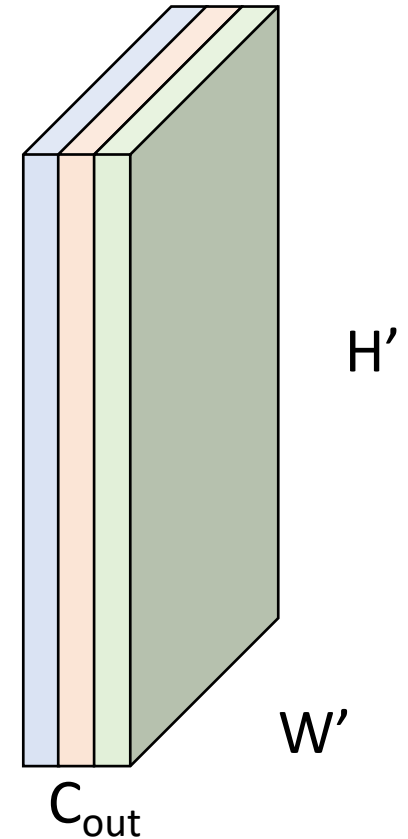
Input:  $C_{in} \times H \times W$

Common to also set  $C_{out} = G$



Weights:  $C_{out} \times 1 \times K \times K$

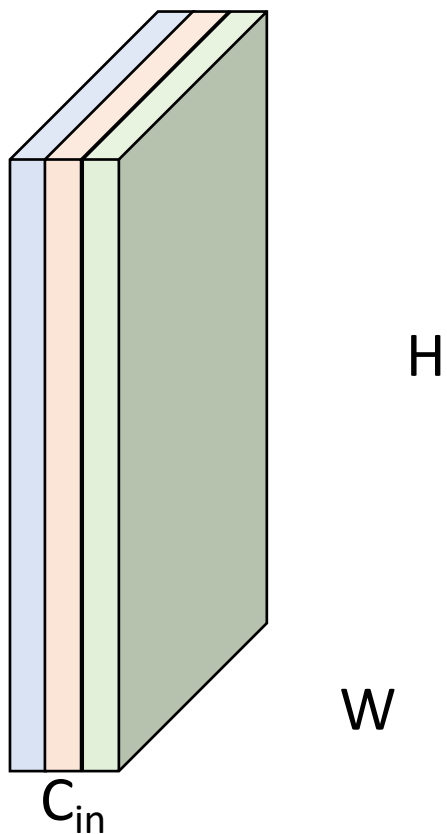
Output only mixes *spatial* information from input; **channel** information not mixed



Output:  $C_{out} \times H' \times W'$

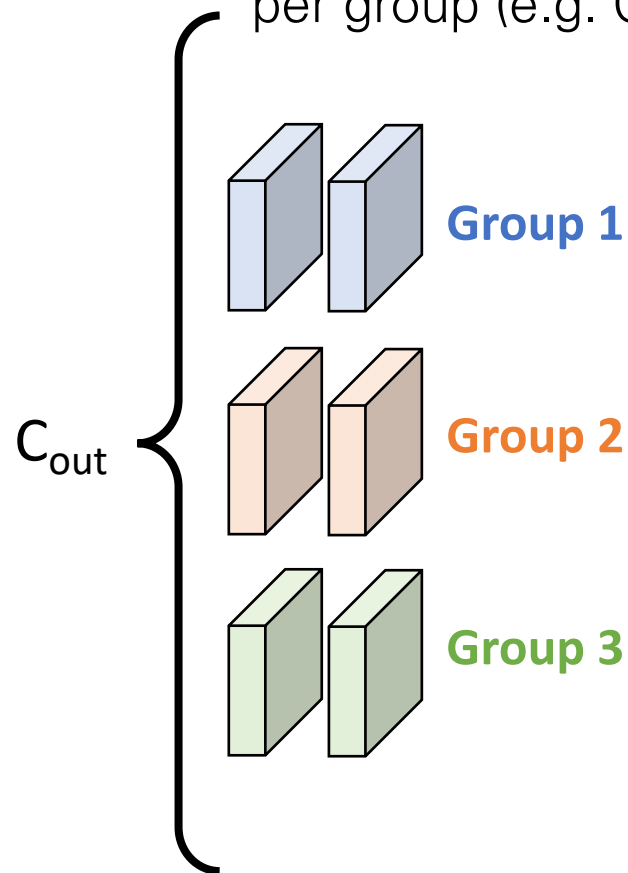
# Special Case: Depthwise Convolution

Number of groups equals number of input channels



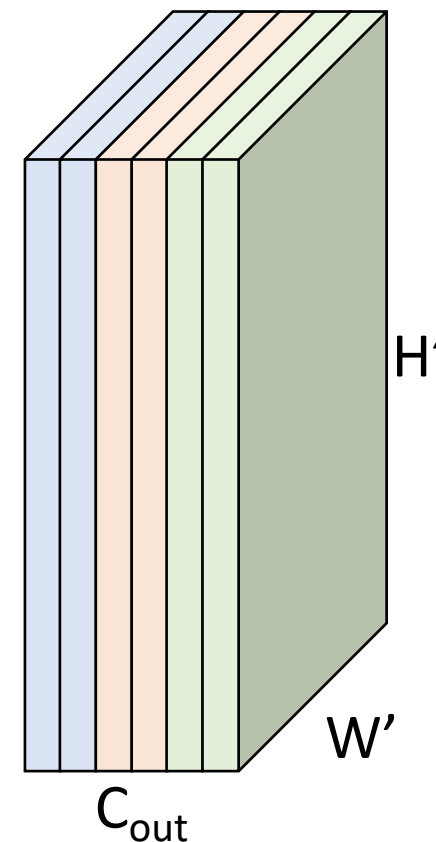
Input:  $C_{in} \times H \times W$

Can still have multiple filters per group (e.g.  $C_{out} = 2C_{in}$ )



Weights:  $C_{out} \times 1 \times K \times K$

Output only mixes *spatial* information from input; **channel** information not mixed



Output:  $C_{out} \times H' \times W'$

# Grouped Convolution vs Standard Convolution

## Grouped Convolution (G groups):

G parallel conv layers; each "sees"  
 $C_{in}/G$  input channels and produces  
 $C_{out}/G$  output channels

Input:  $C_{in} \times H \times W$

Split to  $G \times [(C_{in} / G) \times H \times W]$

Weight:  $G \times (C_{out} / G) \times (C_{in} / G) \times K \times K$

G parallel convolutions

Output:  $G \times [(C_{out} / G) \times H' \times W']$

Concat to  $C_{out} \times H' \times W'$

FLOPs:  $C_{out} C_{in} K^2 HW / G$

## Standard Convolution (groups=1)

Input:  $C_{in} \times H \times W$

Weight:  $C_{out} \times C_{in} \times K \times K$

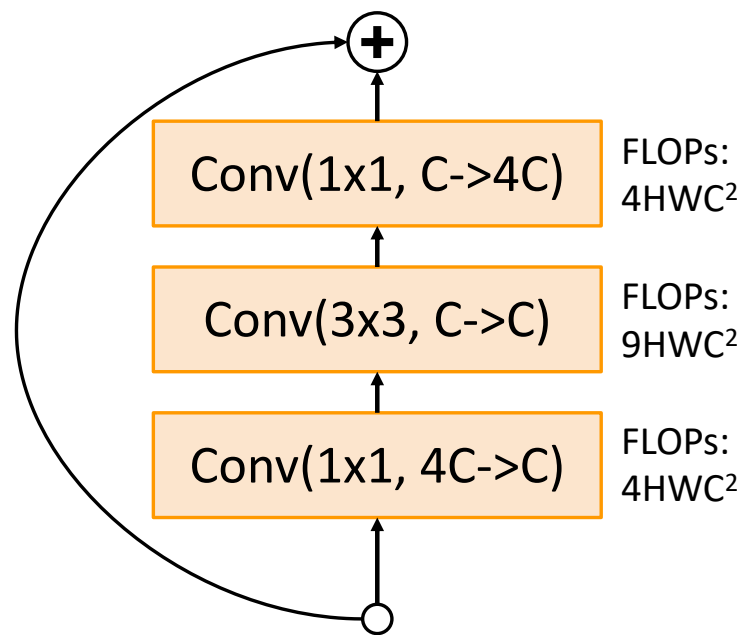
Output:  $C_{out} \times H' \times W'$

FLOPs:  $C_{out} C_{in} K^2 HW$

All convolutional kernels touch  
all  $C_{in}$  channels of the input

Using G groups reduces  
FLOPs by a factor of G!

# Improving ResNets

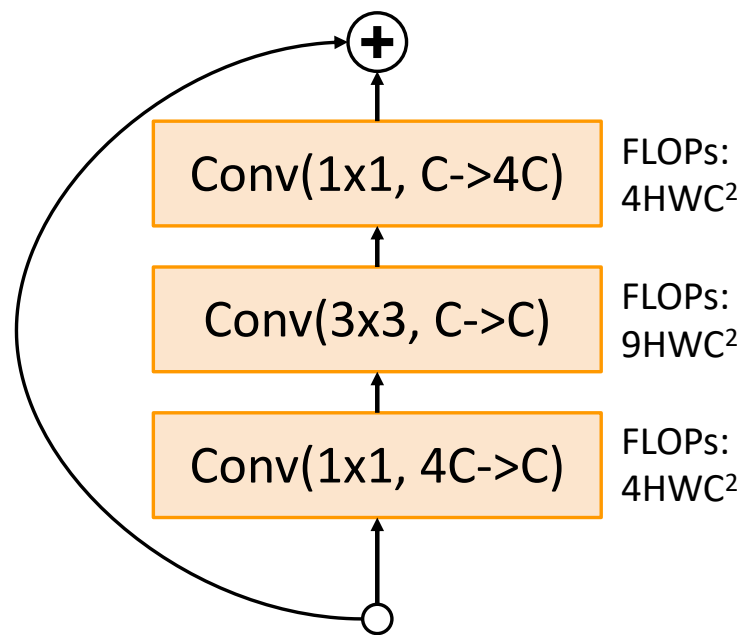


“Bottleneck”  
Residual block

Total FLOPs:  
 $17HWC^2$

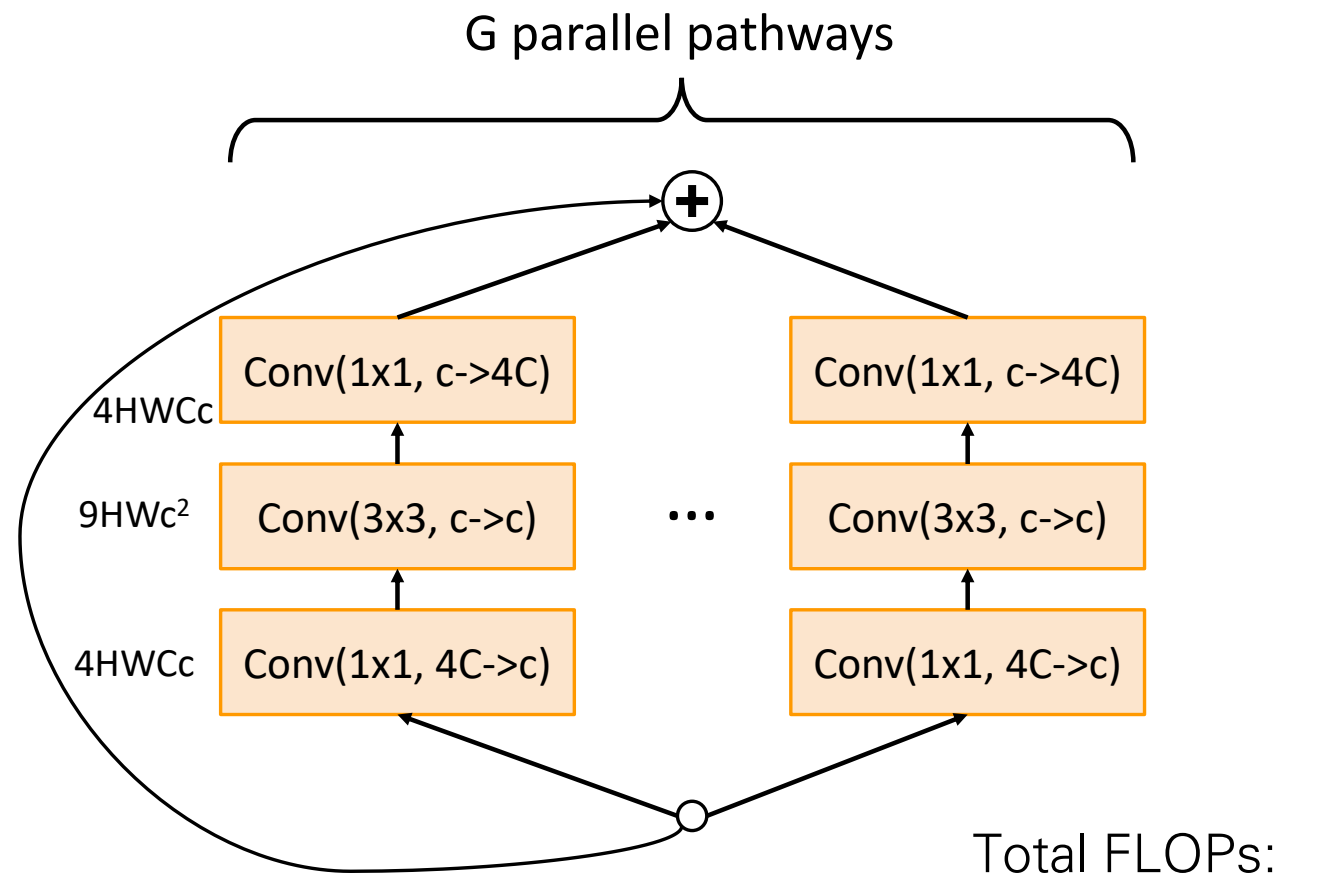


# Improving ResNets: ResNeXt



“Bottleneck”  
Residual block

Total FLOPs:  
 $17HWC^2$

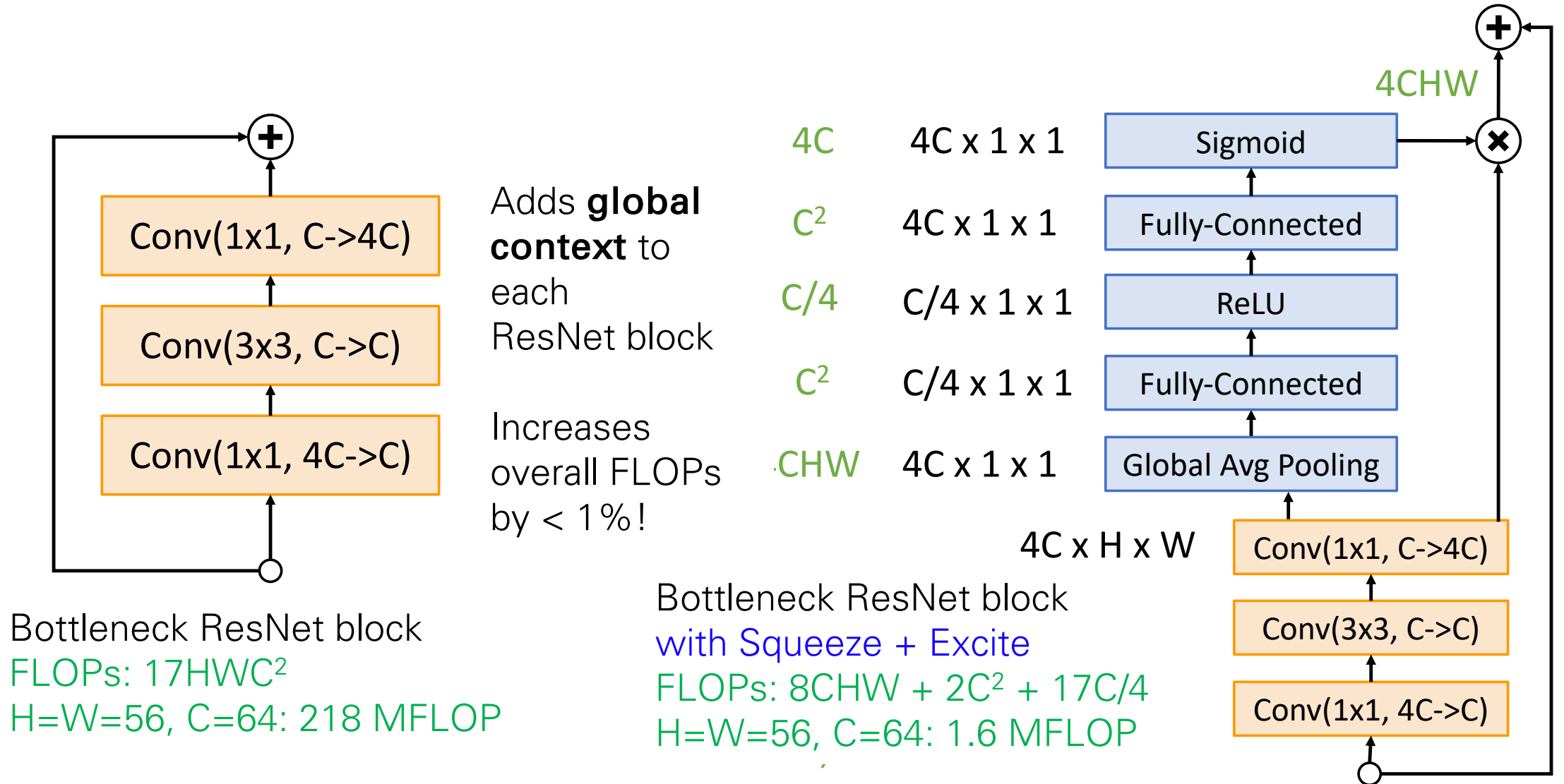


Same FLOPs when  
 $9Gc^2 + 8GCc - 17C^2 = 0$

Total FLOPs:  
 $(8Cc + 9c^2) * HWG$

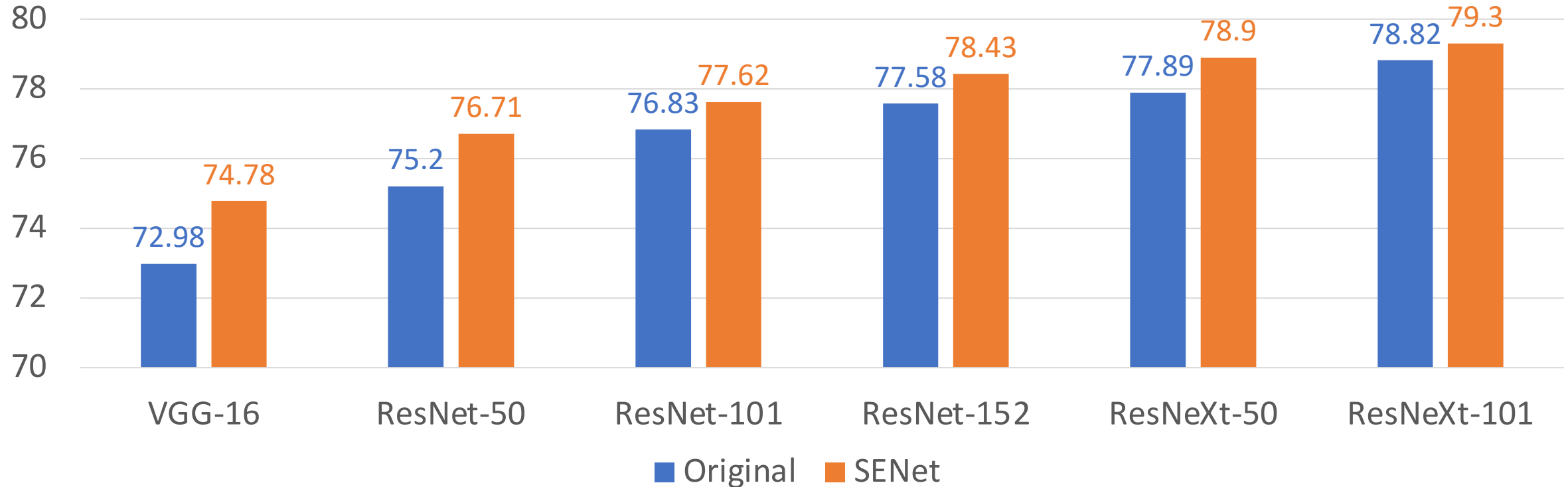
Example:  $C=64, G=4, c=24$ ;  $C=64, G=32, c=4$

# Squeeze-and-Excitation Networks (SENet)



# Squeeze-and-Excitation Networks (SENet)

ImageNet Top-1 Accuracy



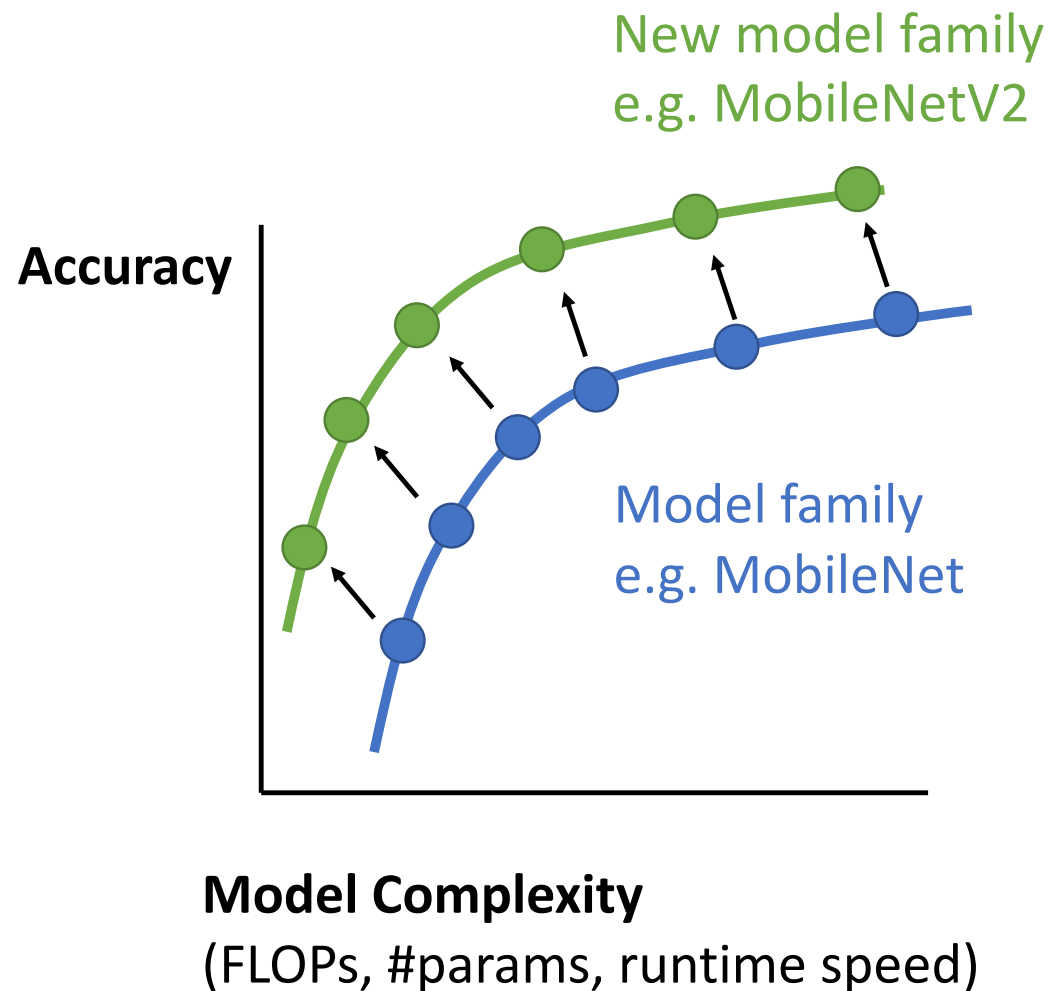
Add SE to any architecture, enjoy 1-2% boost in accuracy

# Recall: Convolution Layer

Instead of pushing for the largest network with biggest accuracy, consider tiny networks and accuracy / complexity tradeoff

Compare **families of models**:

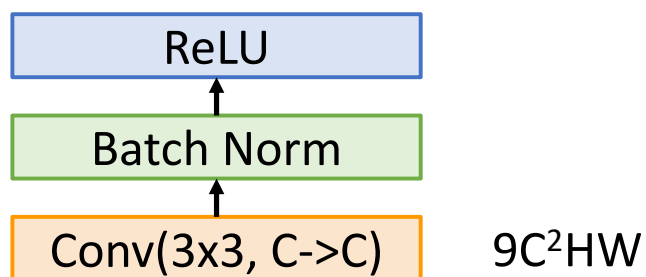
One family is better than another if it moves the whole curve up and to the left



# MobileNets: Tiny Networks (For Mobile Devices)

## Standard Convolution Block

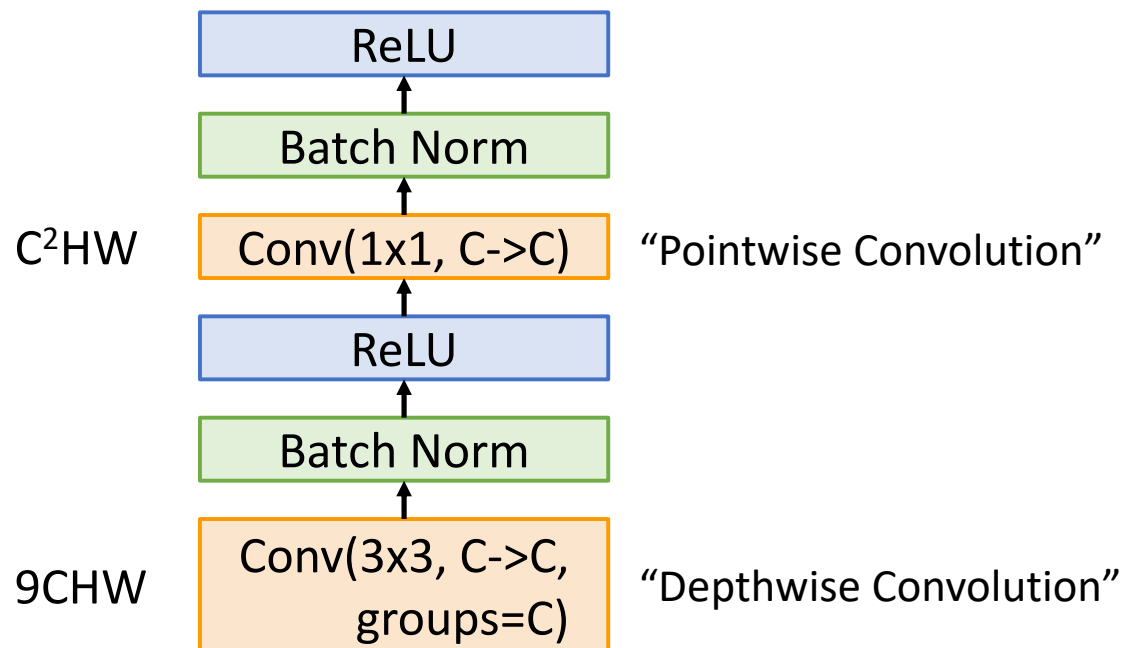
Total cost:  $9C^2HW$



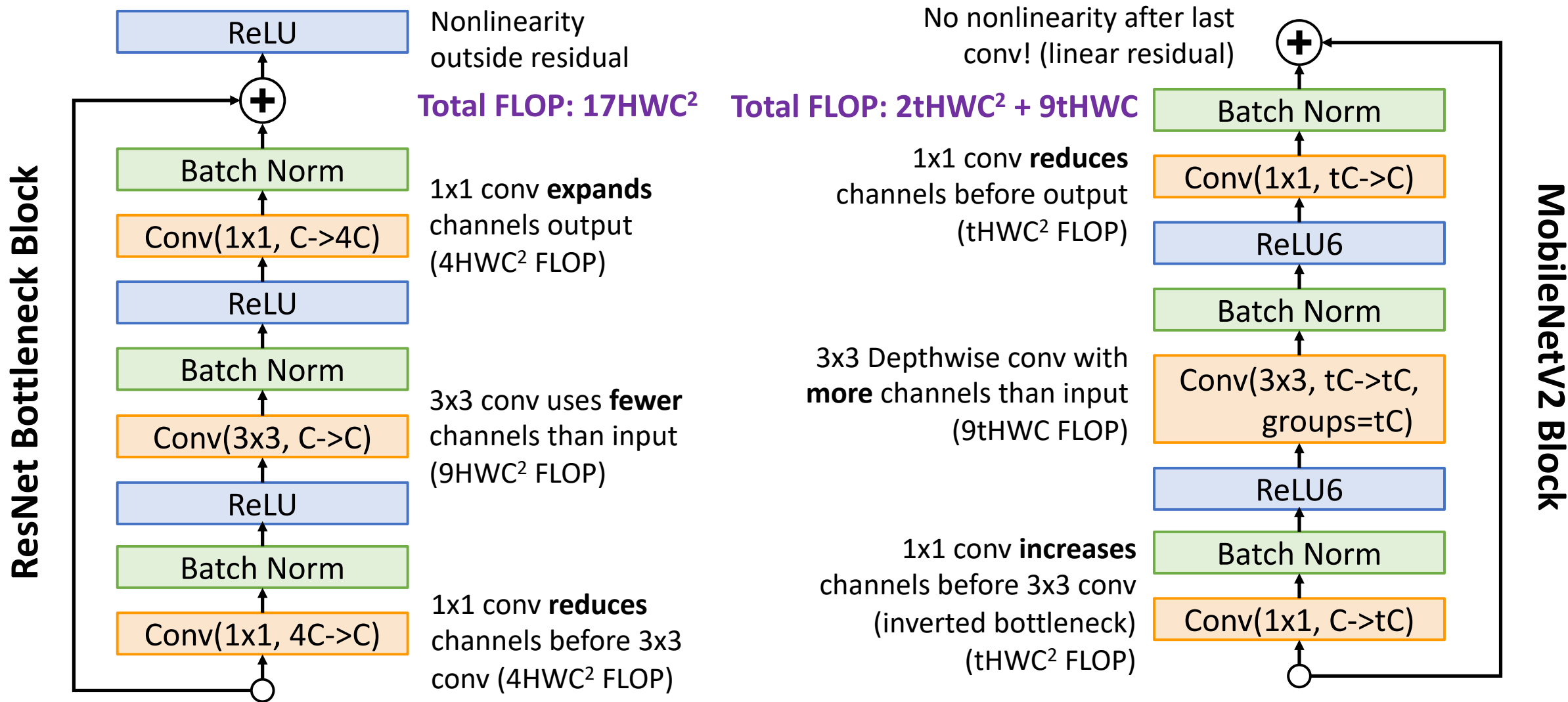
$$\begin{aligned}\text{Speedup} &= 9C^2 / (9C + C^2) \\ &= 9C / (9 + C) \\ &\Rightarrow 9 \text{ (as } C \rightarrow \text{inf)}\end{aligned}$$

## Depthwise Separable Convolution

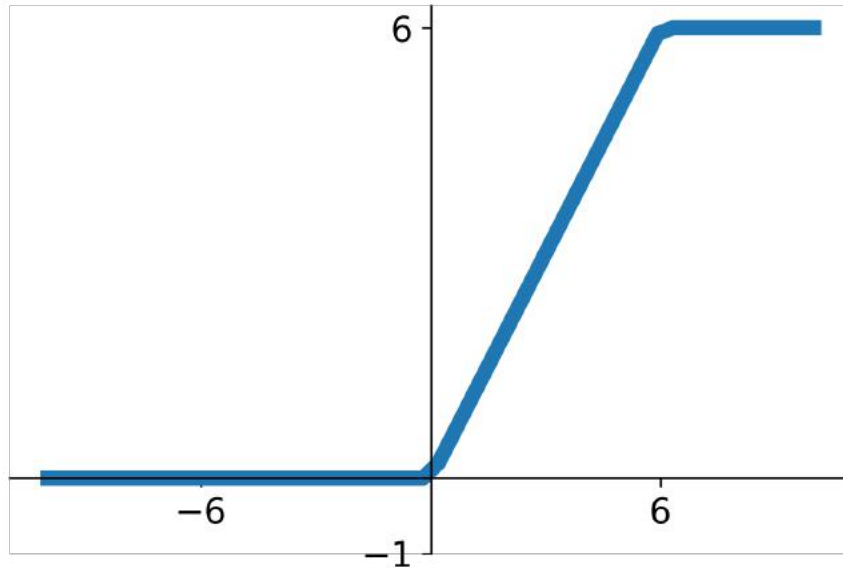
Total cost:  $(9C + C^2)HW$



# MobileNetV2: Inverted Bottleneck, Linear Residual

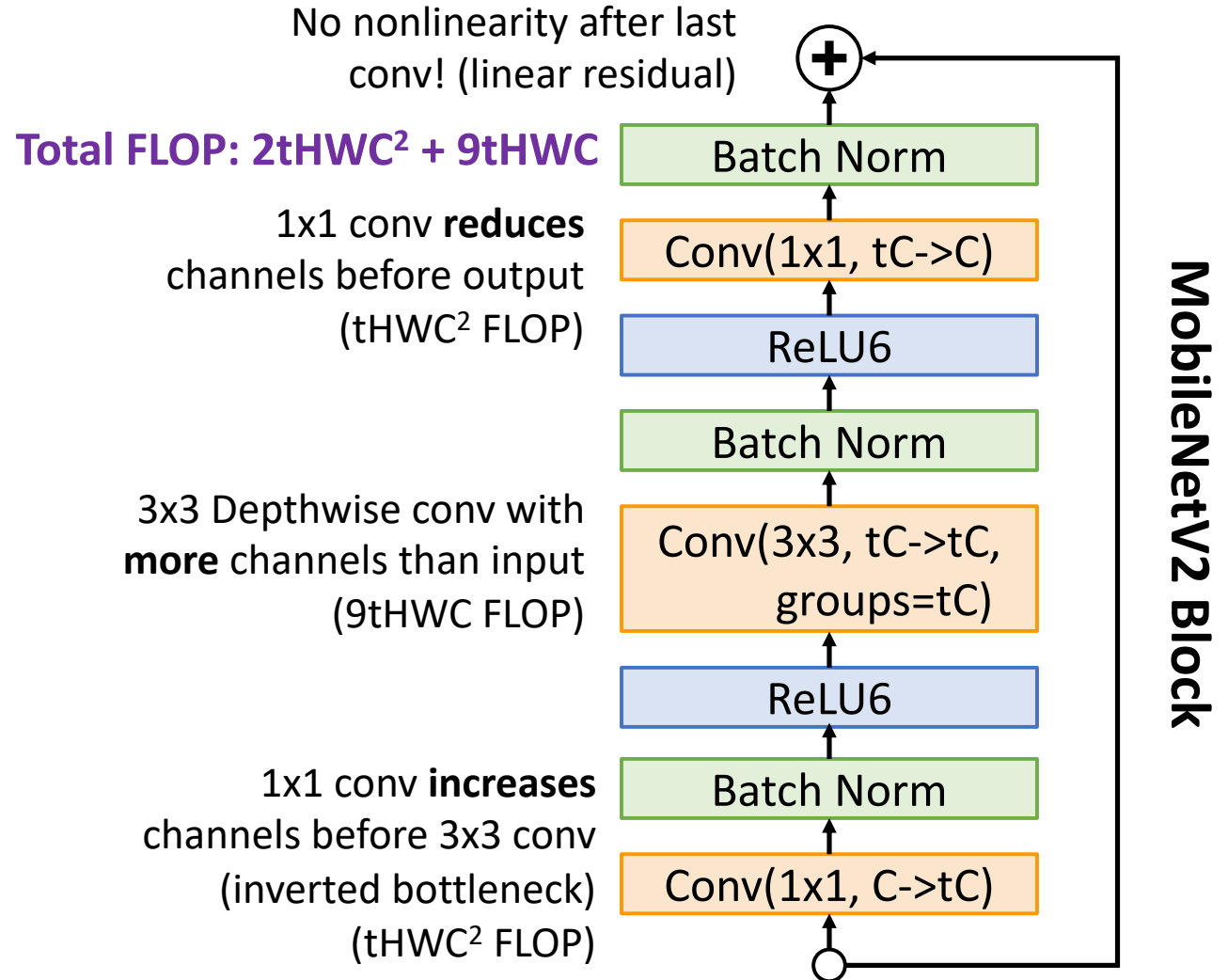


# MobileNetV2: Inverted Bottleneck, Linear Residual



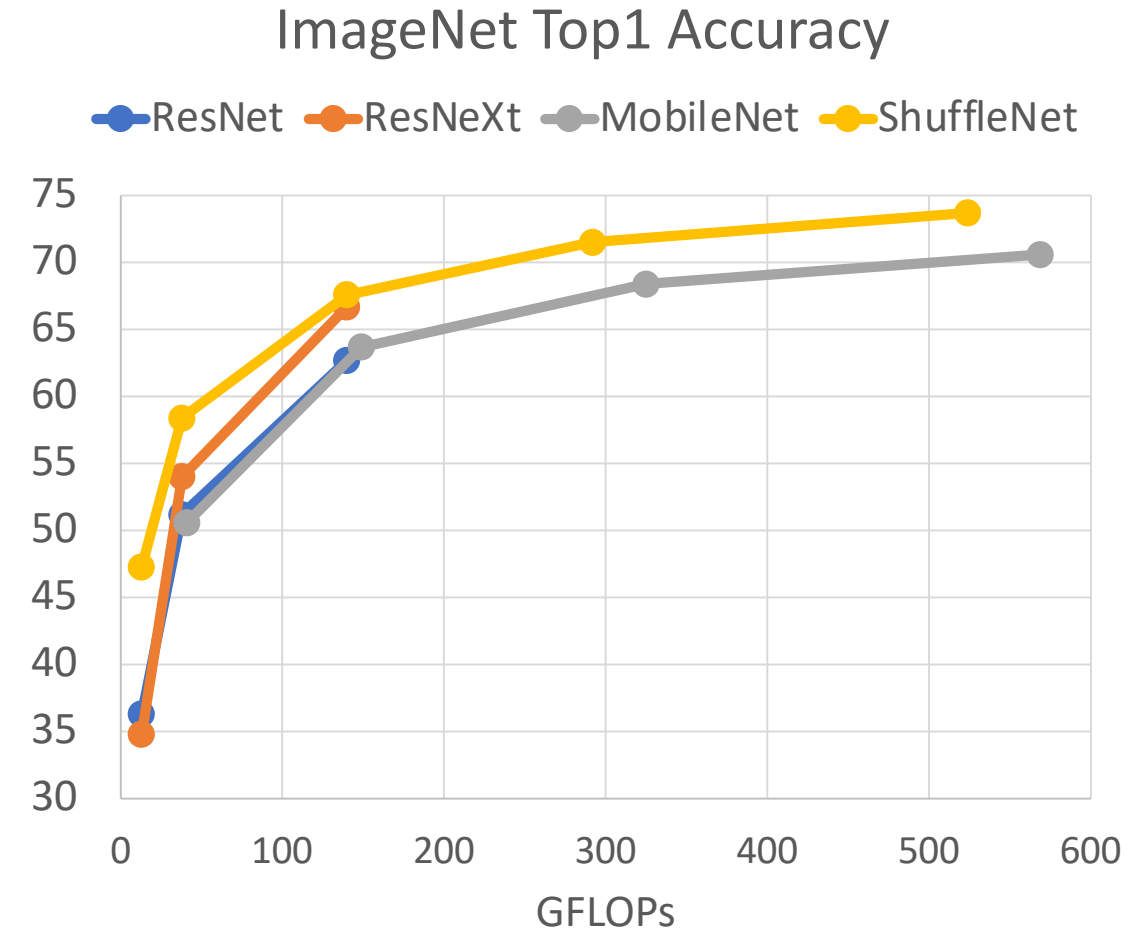
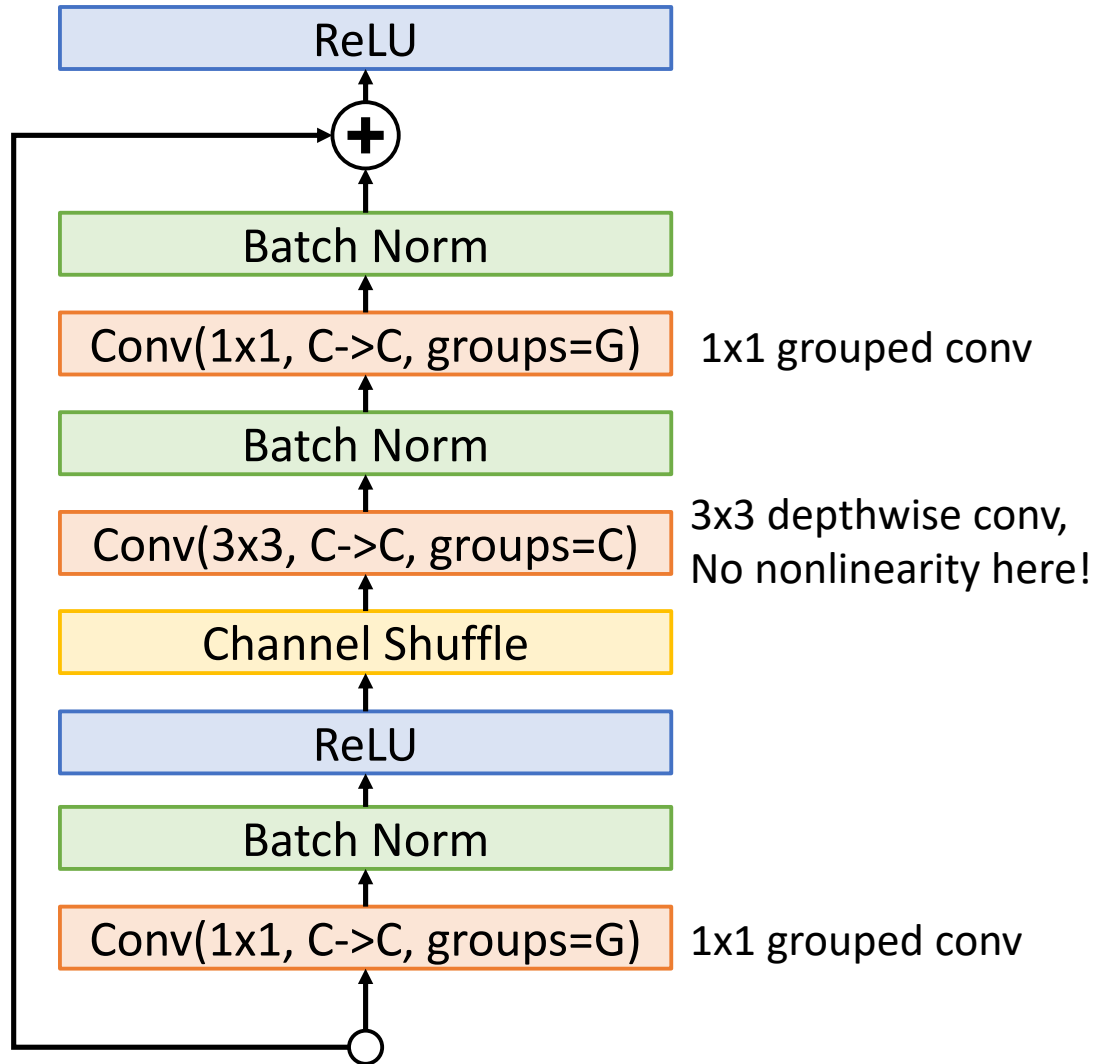
$$ReLU6(x) = \begin{cases} 0 & \text{if } x \leq 0 \\ x & \text{if } 0 < x < 6 \\ 6 & \text{if } x \geq 6 \end{cases}$$

Keeps activations in reasonable range when running inference in low precision



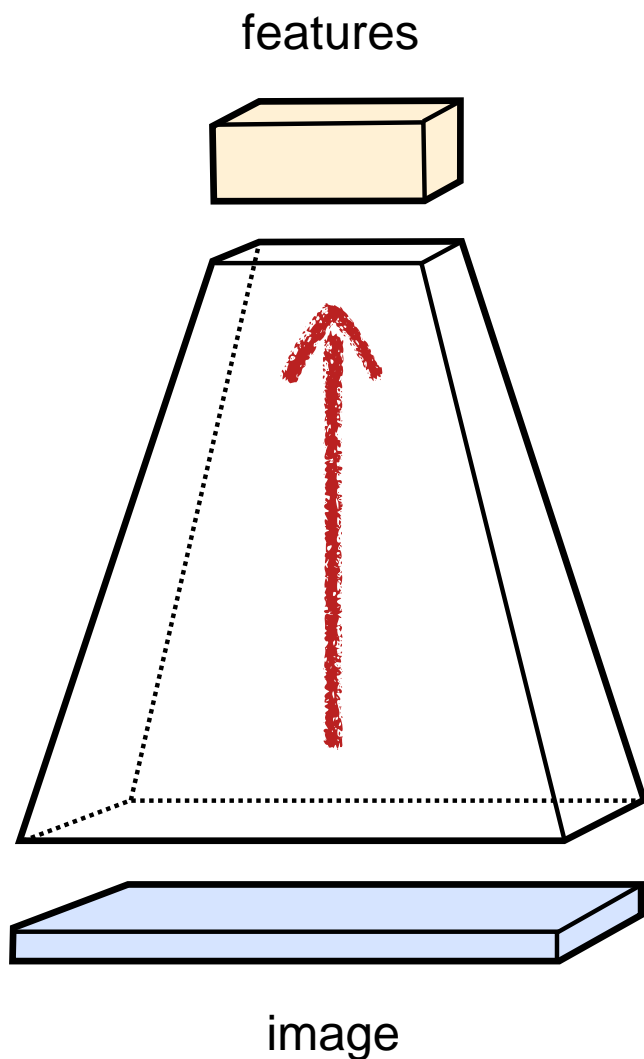


# ShuffleNet



# Design Guidelines

# Design Guidelines



## Guideline 1: Avoid tight bottlenecks

- From bottom to top

- The spatial resolution  $H \times W$  decreases
- The number of channels  $C$  increases

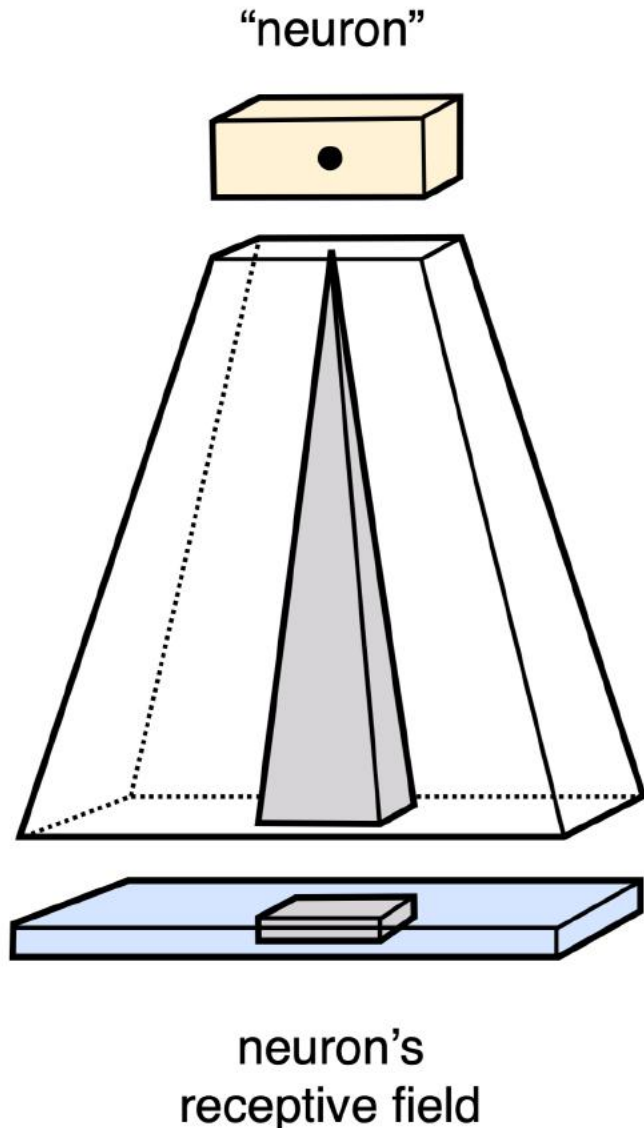
- Guideline

- Avoid tight information bottleneck
- Decrease the data volume  $H \times W \times C$  slowly

K. Simonyan and A. Zisserman. **Very deep convolutional networks for large-scale image recognition**. In ICLR 2015.

C. Szegedy, V. Vanhoucke, S. Ioffe, and J. Shlens. **Rethinking the inception architecture for computer vision**. In CVPR 2016.

# Receptive Field



## Must be large enough

- **Receptive field of a neuron**

- The image region influencing a neuron
- Anything happening outside is invisible to the neuron

- **Importance**

- Large image structures cannot be detected by neurons with small receptive fields

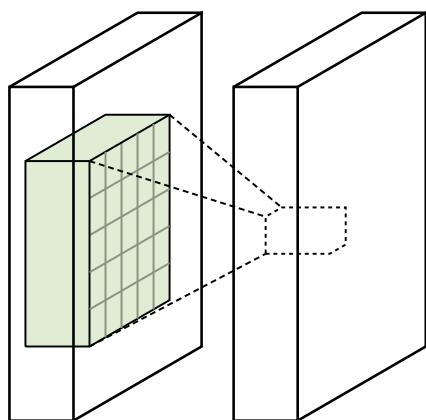
- **Enlarging the receptive field**

- Large filters
- Chains of small filters

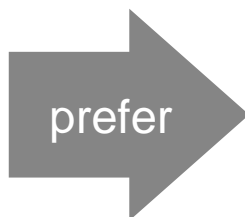
# Design Guidelines

## Guideline 2: Prefer small filter chains

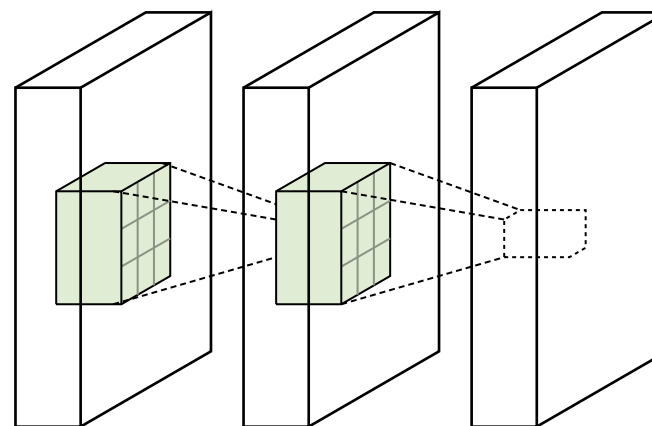
One big filter bank



5 × 5 filters  
+ ReLU



Two smaller filter banks



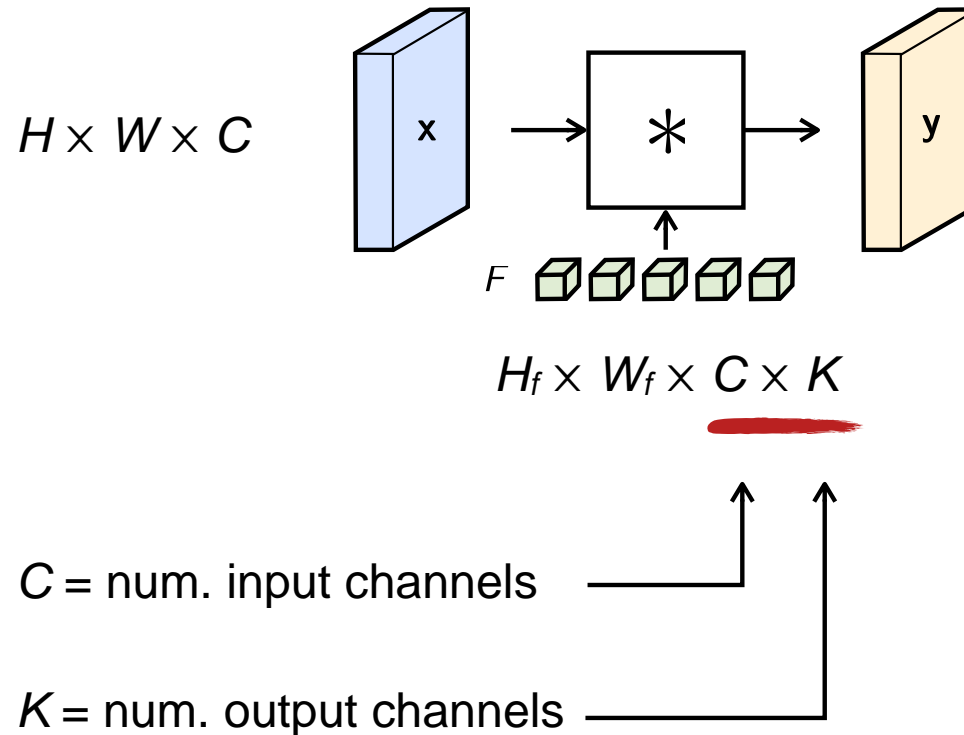
3 × 3 filters + ReLU    3 × 3 filters + ReLU

- **Remark:** 101 ResNet layers same size/speed as 16 VGG-VD layers
- **Reason:** Far fewer feature channels (quadratic speed/space gain)
- **Moral:** Optimize your architecture

# Design Guidelines

## Guideline 3:

Keep the number of channels at bay



Num. of operations

$$\frac{H \times H_f}{\text{stride}} \times \frac{W \times W_f}{\text{stride}} \times \underline{C \times K}$$

Num. of parameters

$$H_f \times W_f \times \underline{C \times K}$$

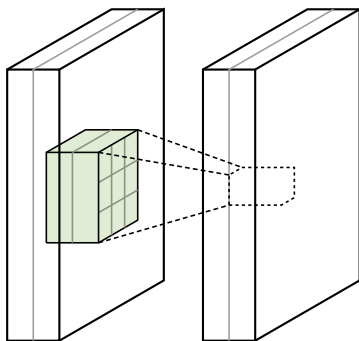
complexity  $\propto \underline{C \times K}$

# Design Guidelines

## Guideline 4:

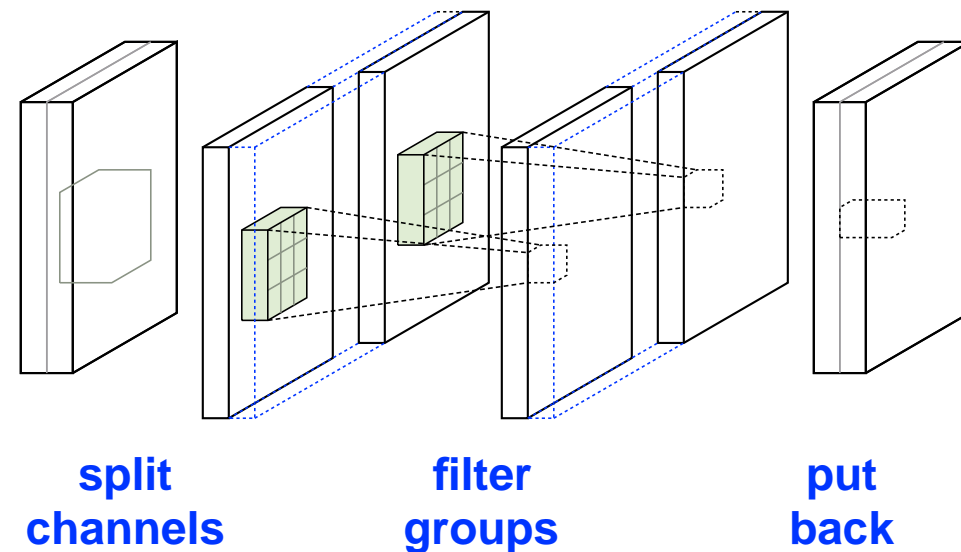
Less  
computations  
with filter  
groups

$M$  filters



consider  
instead

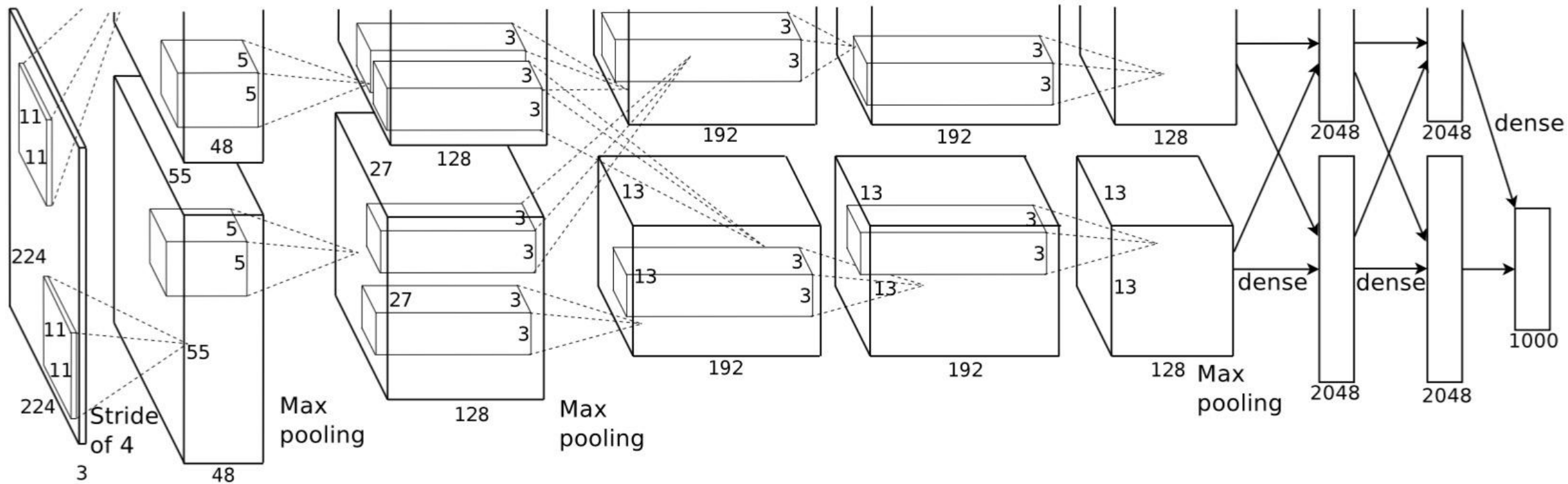
$G$  groups of  $M/G$  filters



Did we see this before?

$$\text{complexity} \propto (C \times K) / G$$

# AlexNet

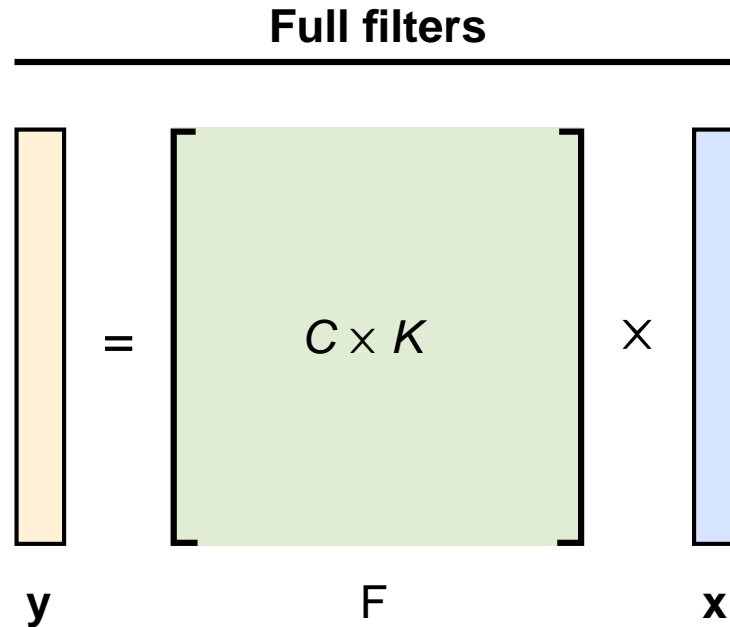




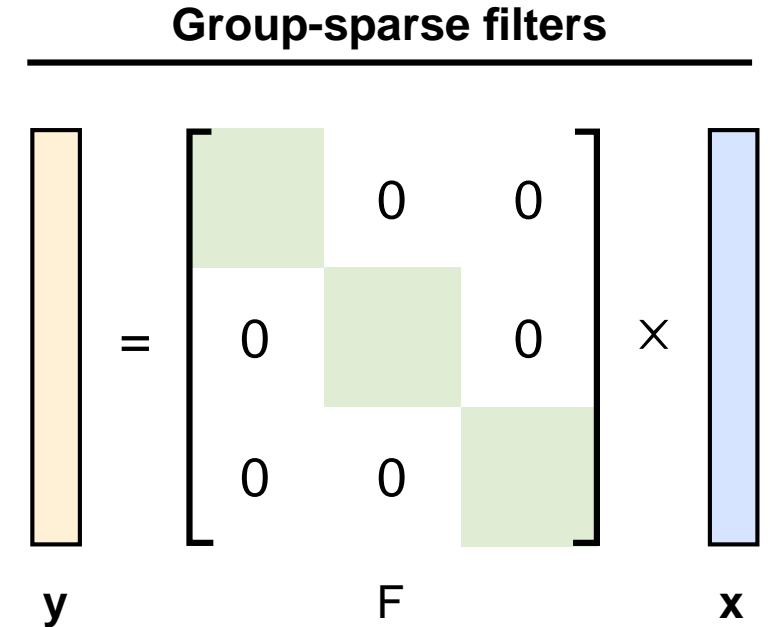
# Design Guidelines

## Guideline 4:

Less computations with filter groups



complexity:  $C \times K$



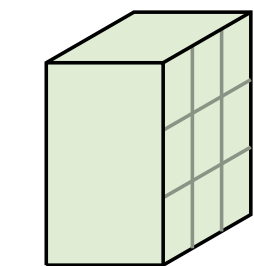
complexity:  $C \times K / G$

**Groups** = filters, seen as a matrix, have a “block” structure

# Design Guidelines

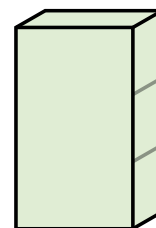
## Guideline 5:

### Low-rank decompositions



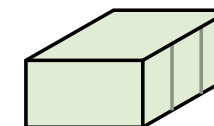
**filter bank**  
 $3 \times 3 \times C \times K$

decompose spatially



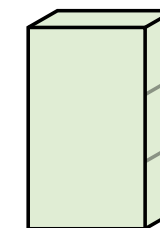
**vertical**  
 $1 \times 3 \times C \times K$

\*



**horizontal**  
 $3 \times 1 \times K \times K$

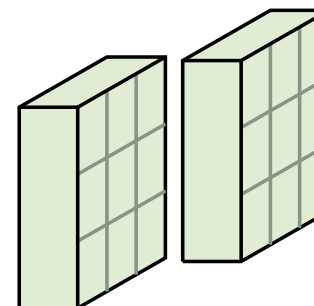
\*



**vertical**  
 $1 \times 3 \times K \times K$

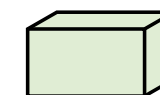


decompose channels



**groups**  
 $3 \times 3 \times C/G \times K/G$

\*

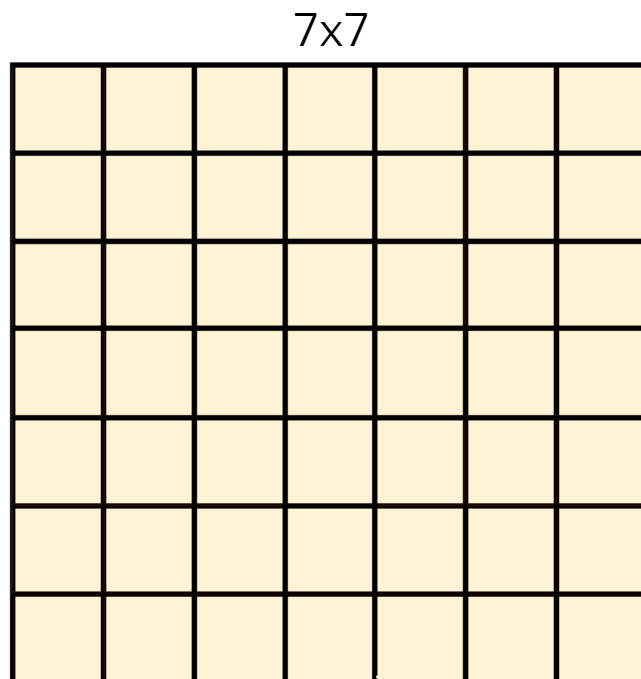


**"network in network"**  
 $1 \times 1 \times K \times K$

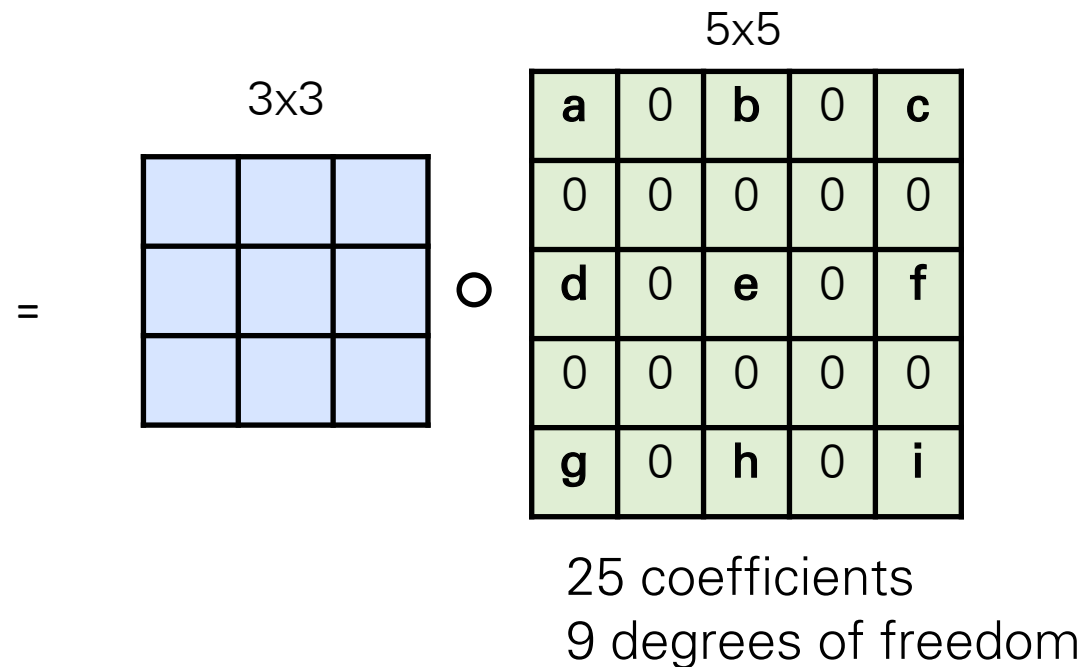
Make sure to mix the information

# Design Guidelines

## Guideline 6: Dilated Convolutions



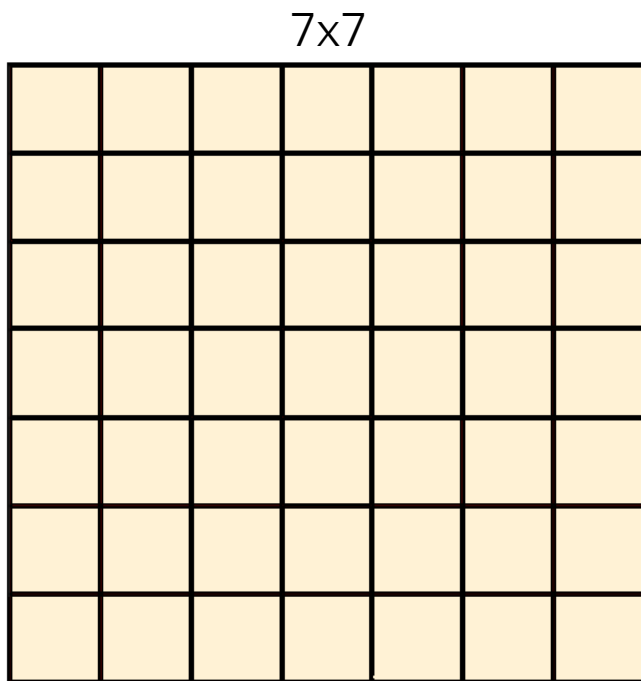
49 coefficients  
18 degrees of freedom



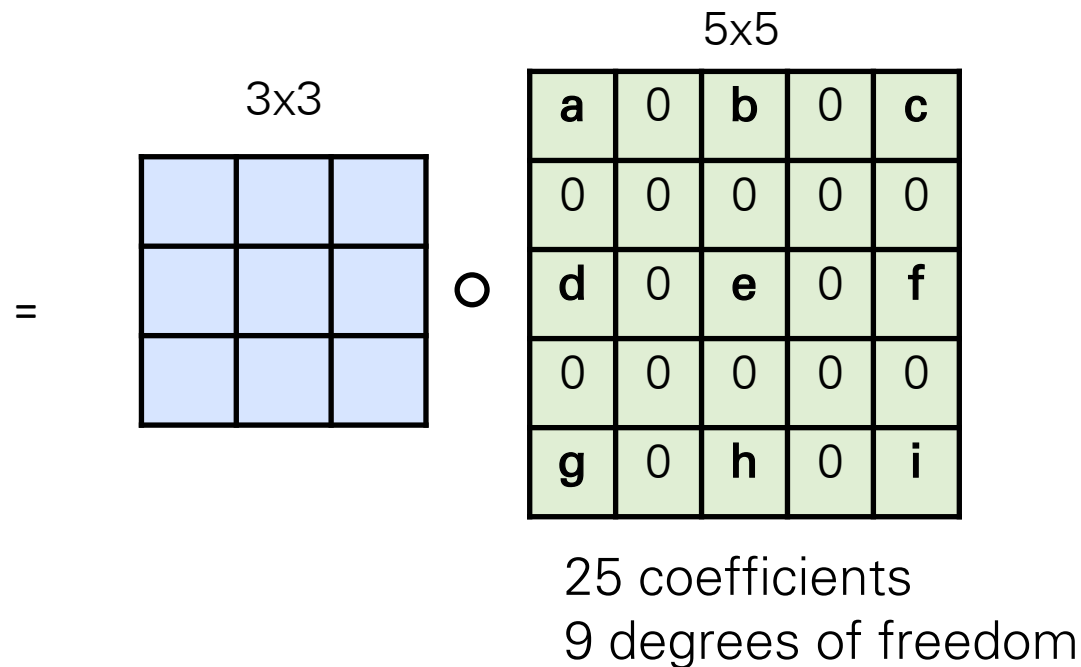
Exponential expansion of the receptive field without loss of resolution

# Design Guidelines

## Guideline 6: Dilated Convolutions

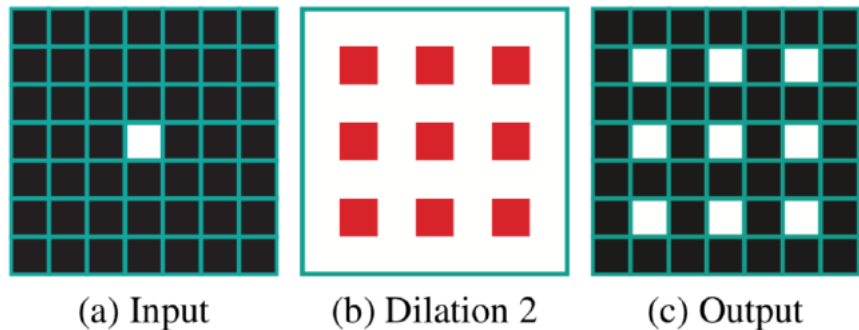


49 coefficients  
18 degrees of freedom



Exponential expansion  
of the receptive field  
without loss of resolution

What is lost?



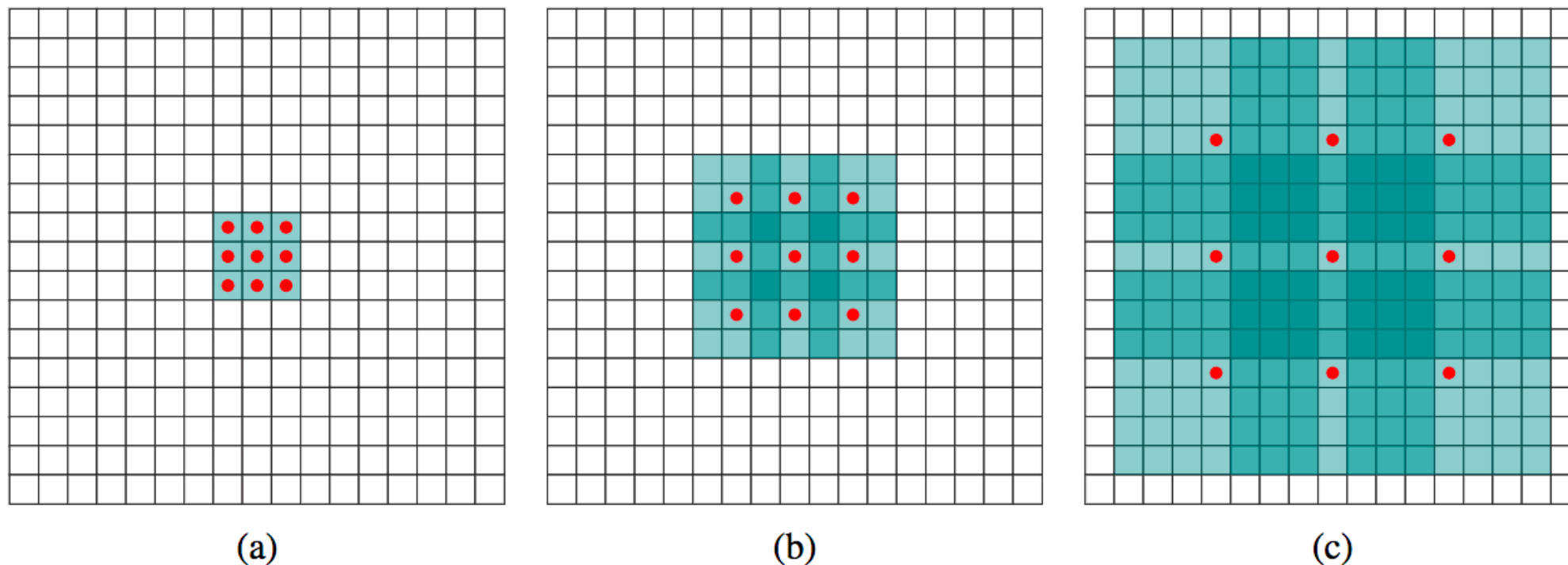


Figure 1: Systematic dilation supports exponential expansion of the receptive field without loss of resolution or coverage. (a)  $F_1$  is produced from  $F_0$  by a 1-dilated convolution; each element in  $F_1$  has a receptive field of  $3 \times 3$ . (b)  $F_2$  is produced from  $F_1$  by a 2-dilated convolution; each element in  $F_2$  has a receptive field of  $7 \times 7$ . (c)  $F_3$  is produced from  $F_2$  by a 4-dilated convolution; each element in  $F_3$  has a receptive field of  $15 \times 15$ . The number of parameters associated with each layer is identical. The receptive field grows exponentially while the number of parameters grows linearly.

[<https://arxiv.org/pdf/1511.07122.pdf>]

# CNN Architectures Summary

- Early work (AlexNet->VGG->ResNet): **bigger networks work better**
- New focus on **efficiency**: Improve accuracy, control for network complexity
- Grouped, Depthwise, Dilated convolution appear in many modern architectures
- **Squeeze-and-Excite** adds accuracy boost to just about any architecture while only adding a tiny amount of FLOPs and runtime
- Tiny networks for **mobile devices** (MobileNet, ShuffleNet)
- **Neural Architecture Search (NAS)** promised to automate architecture design
- More recent work has moved towards **careful improvements to ResNet-like architectures**
- ResNet and ResNeXt are still surprisingly strong and popular architectures!

# Transfer Learning with Convolutional Neural Networks

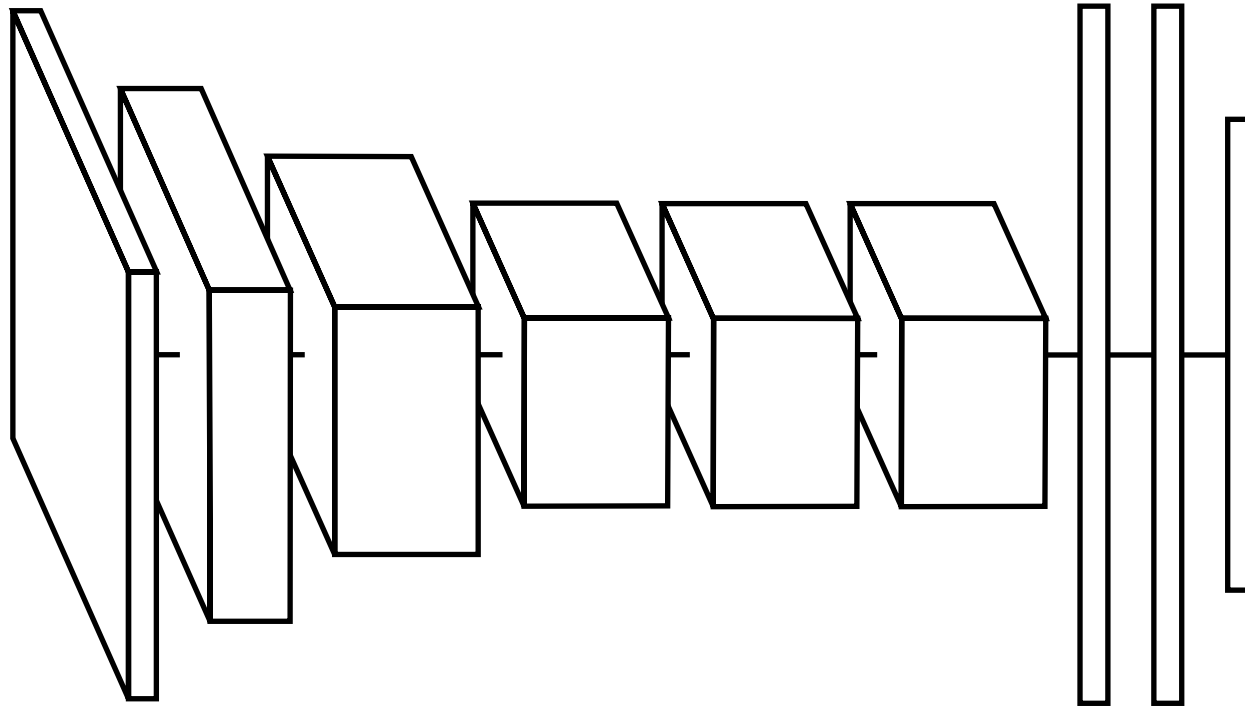
# Beyond CNNs

- Do features extracted from the CNN generalize other tasks and datasets?
  - Donahue et al. (2013), Chatfield et al. (2014), Razavian et al. (2014), Yosinski et al. (2014), etc.
- CNN activations as deep features
- Finetuning CNNs



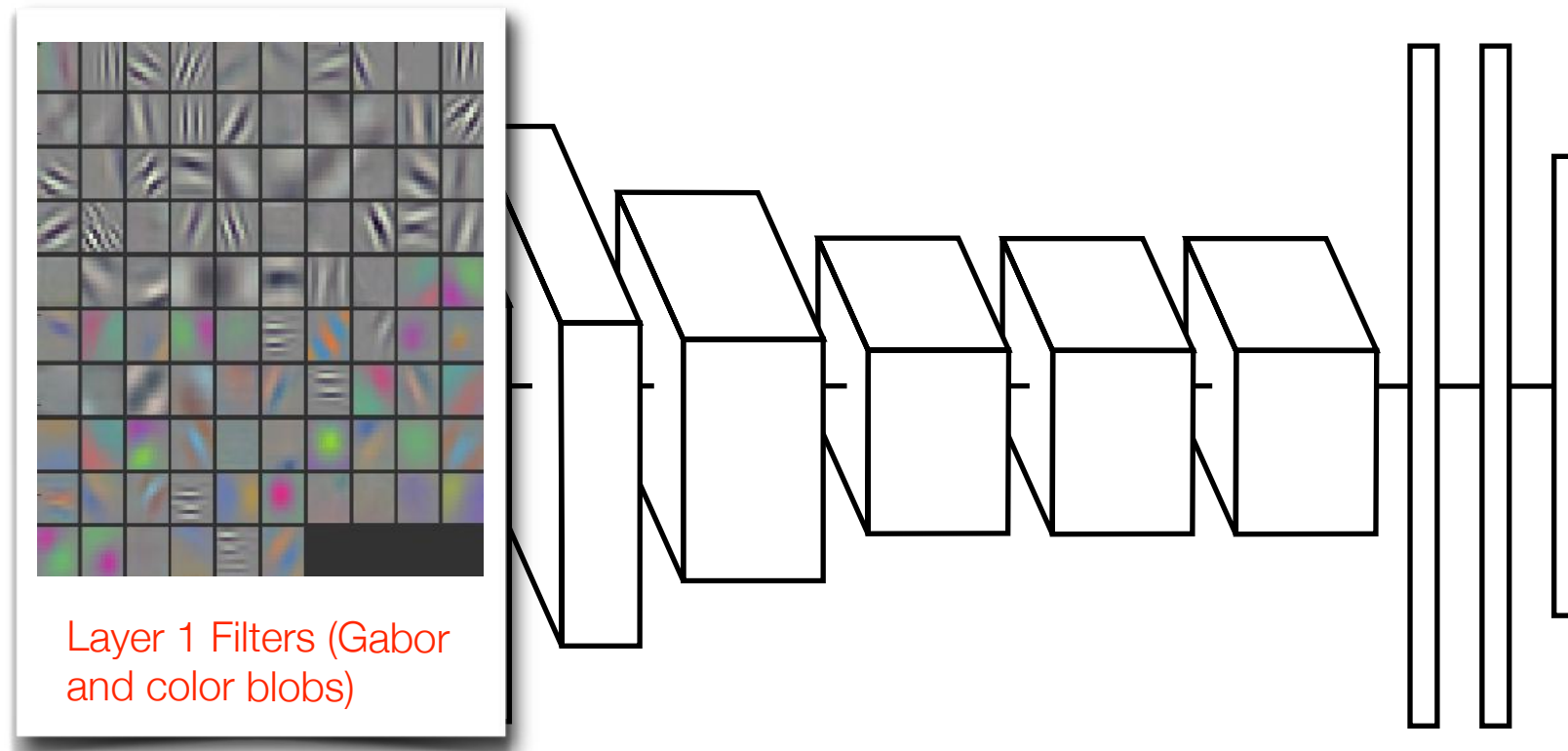
# CNN activations as deep features

- CNNs discover effective representations. Why not to use them?



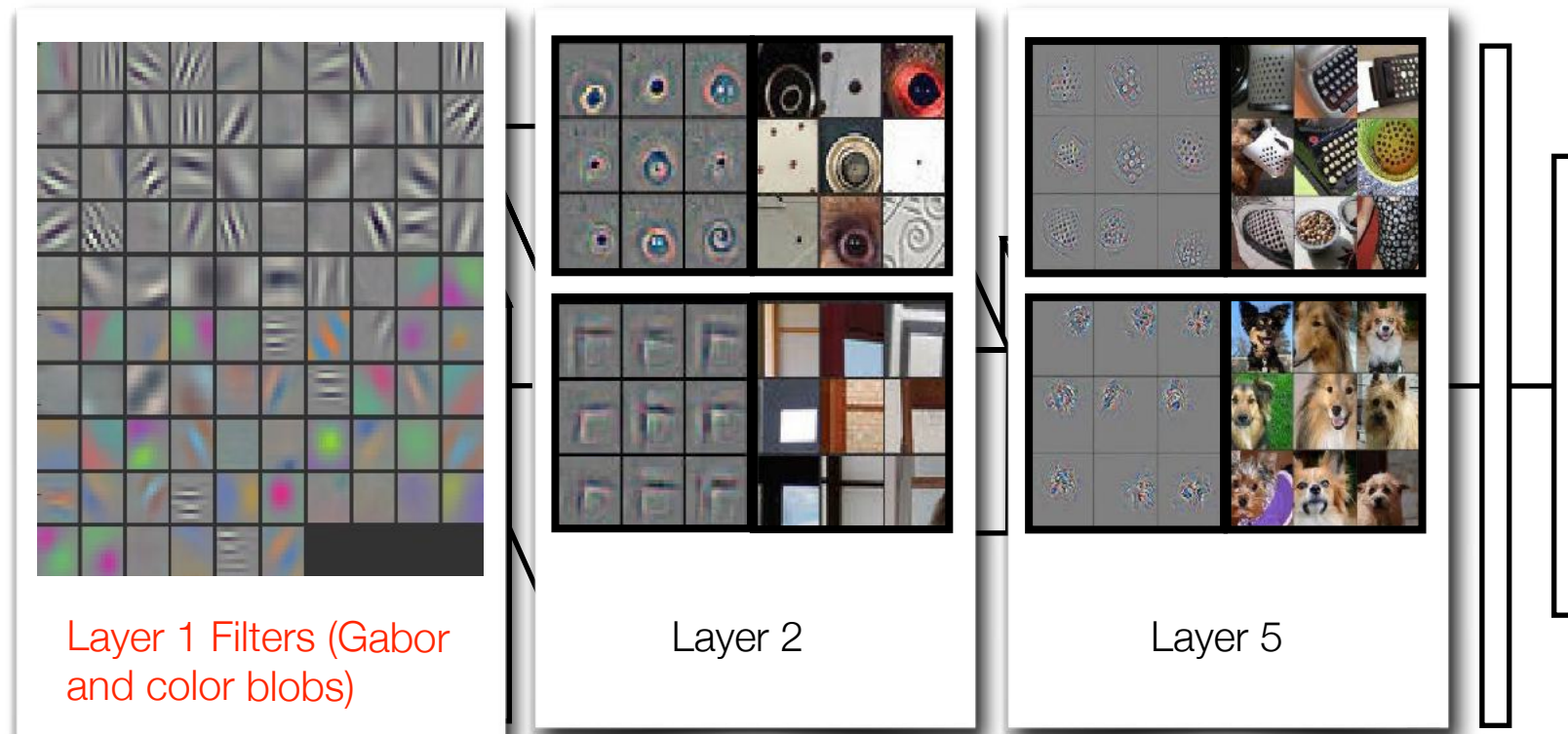
# CNN activations as deep features

- CNNs discover effective representations. Why not to use them?



# CNN activations as deep features

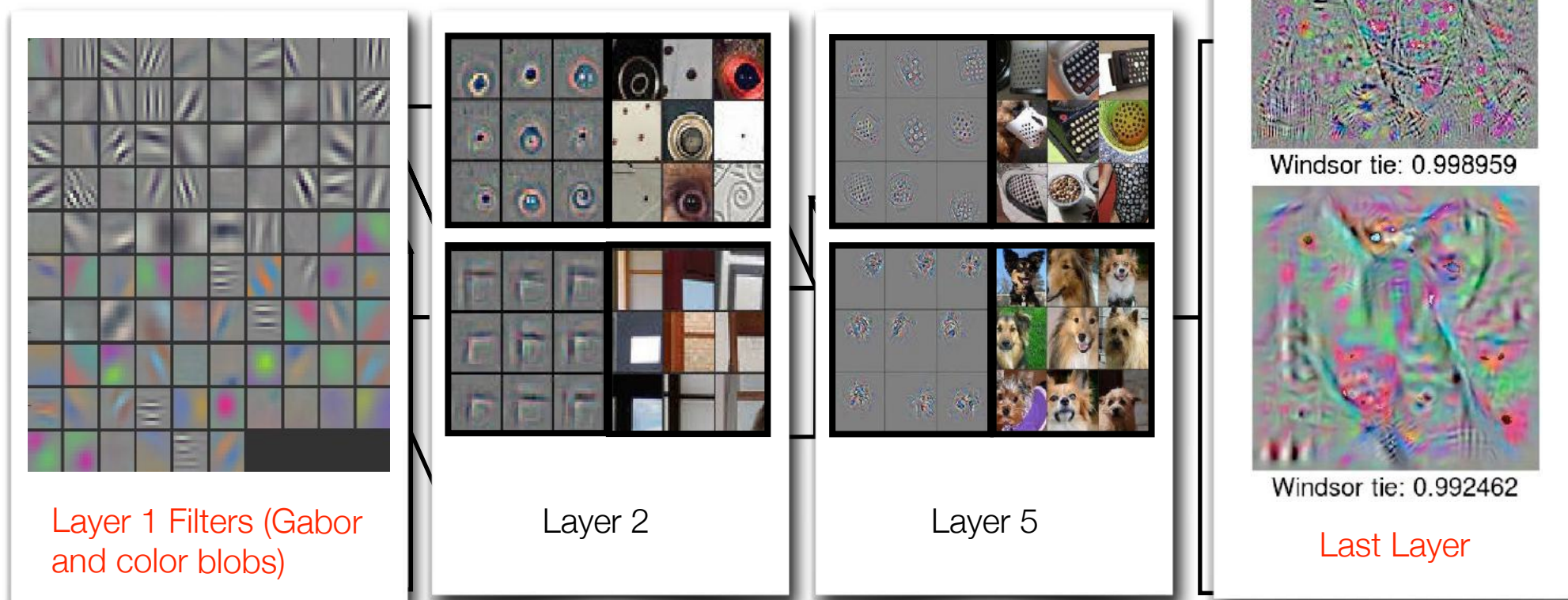
- CNNs discover effective representations. Why not to use them?



Zeiler et al., 2014

# CNN activations as deep features

- CNNs discover effective representations. Why not



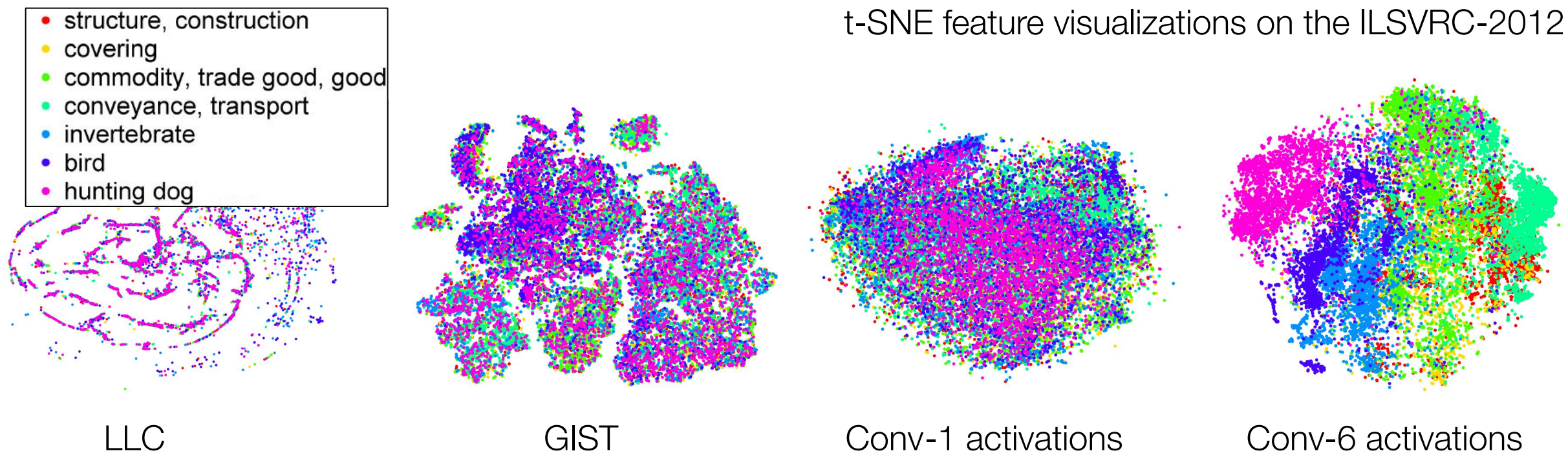
Zeiler et al., 2014

Nguyen et al., 2014



# CNNs as deep features

- CNNs discover effective representations. Why not to use them?



# Transfer Learning with CNNs

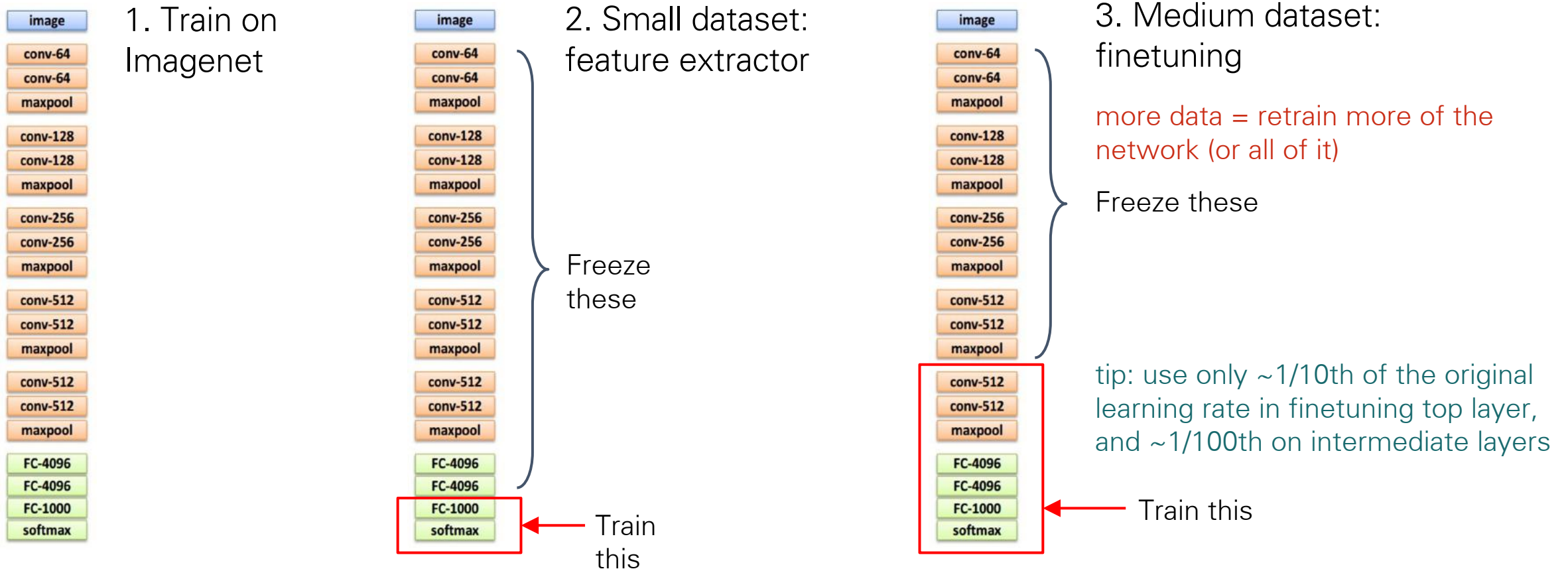
- A CNN trained on a (large enough) dataset generalizes to other visual tasks





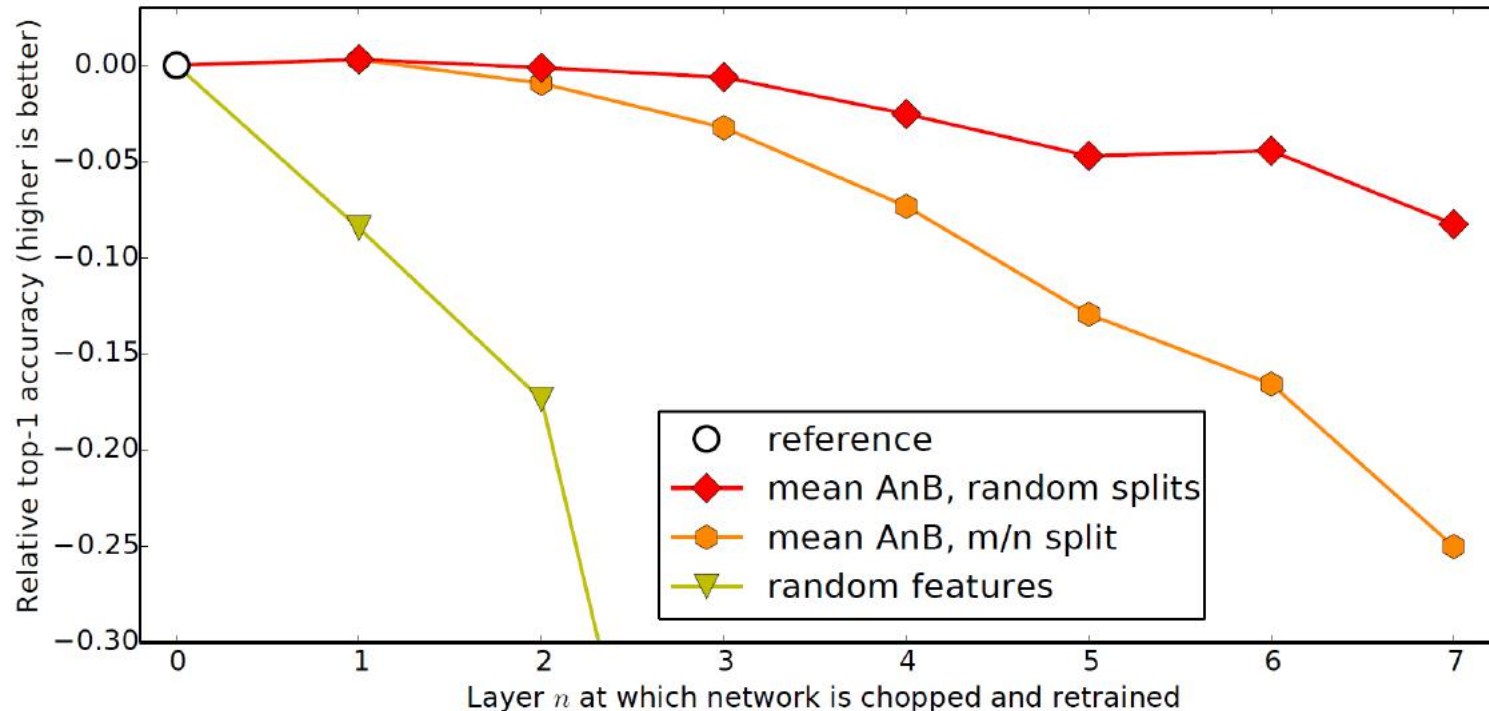
# Transfer Learning with CNNs

- Keep layers 1-7 of our ImageNet-trained model fixed
- Train a new softmax classifier on top using the training images of the new dataset.



# How transferable are features in CNN networks?

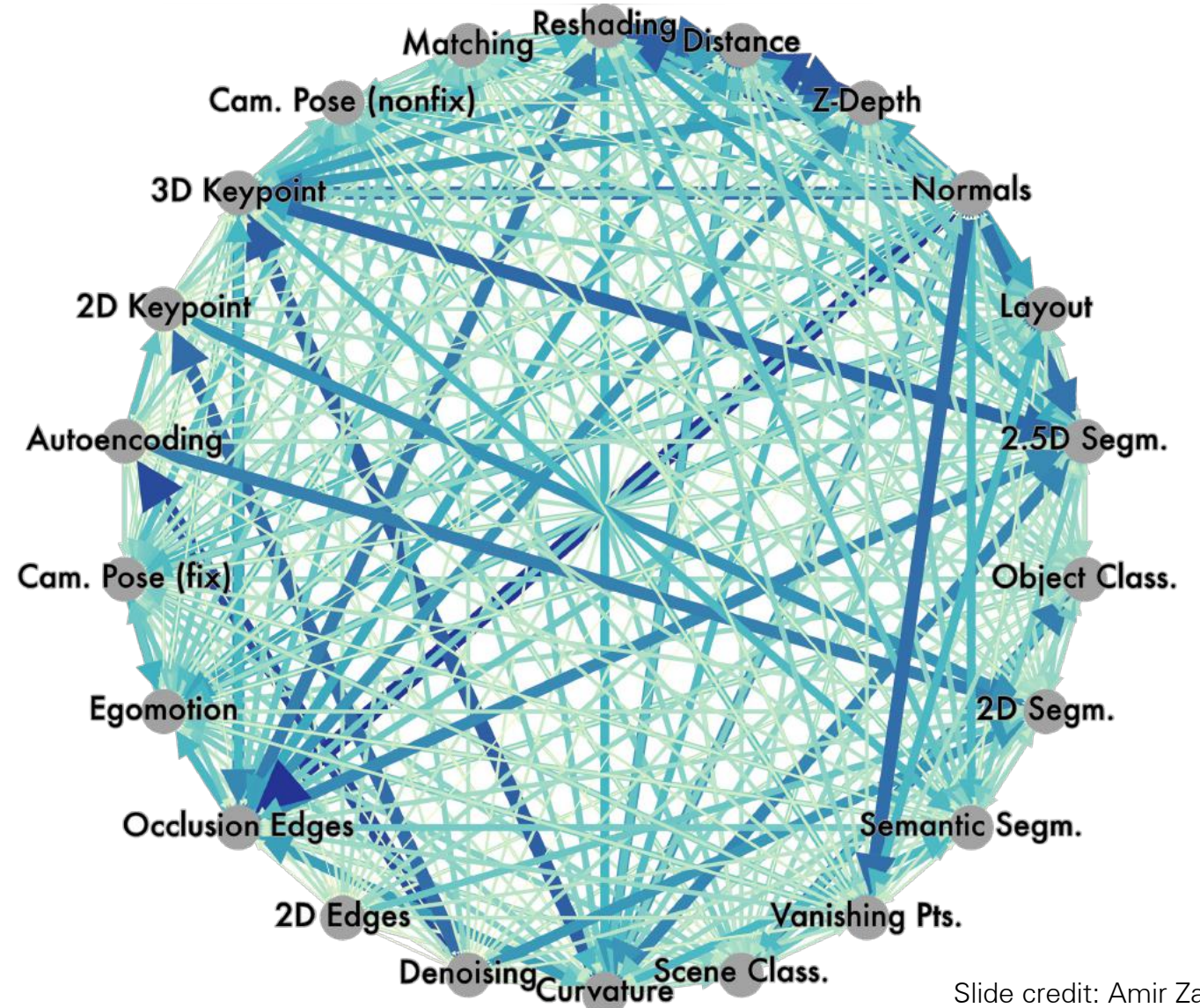
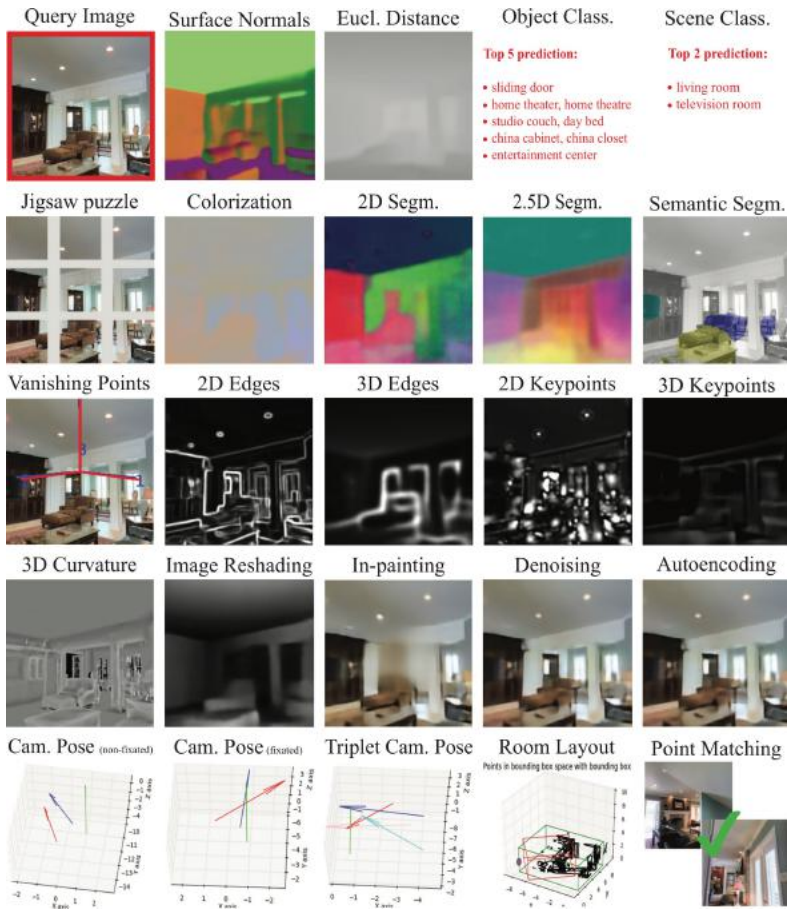
- Divide ImageNet into man-made objects A (449 classes) and natural objects B (551 classes)
- The transferability of features decreases as the distance between the base task and target task increases





# How transferable are features in CNN networks?

- An open research problem



Slide credit: Amir Zamir



# Semantic Segmentation



Sky

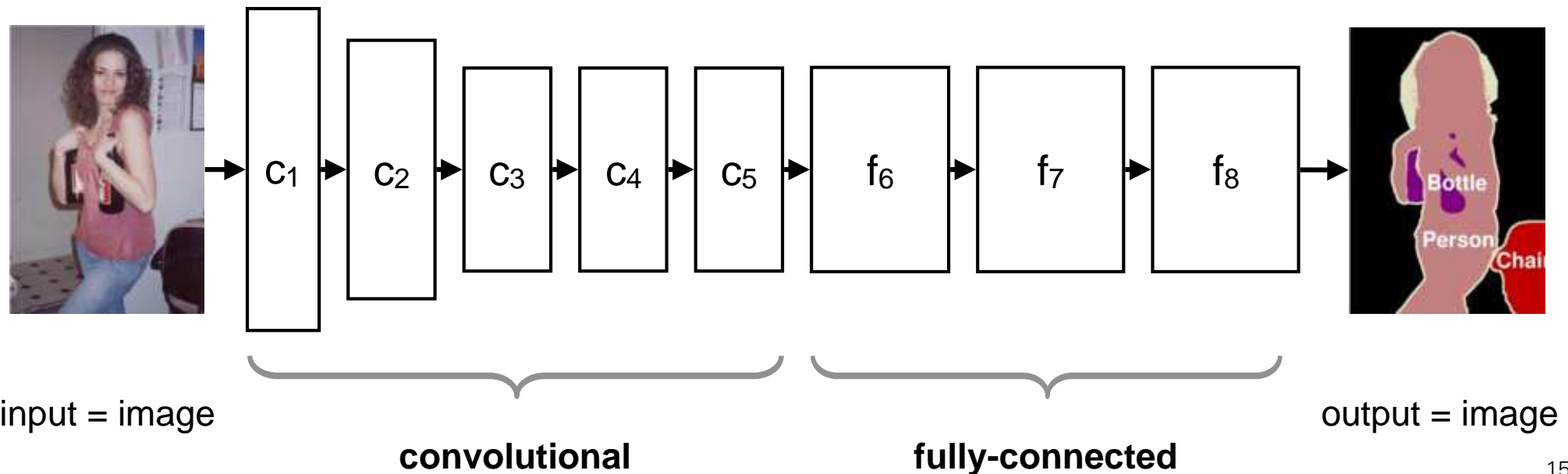
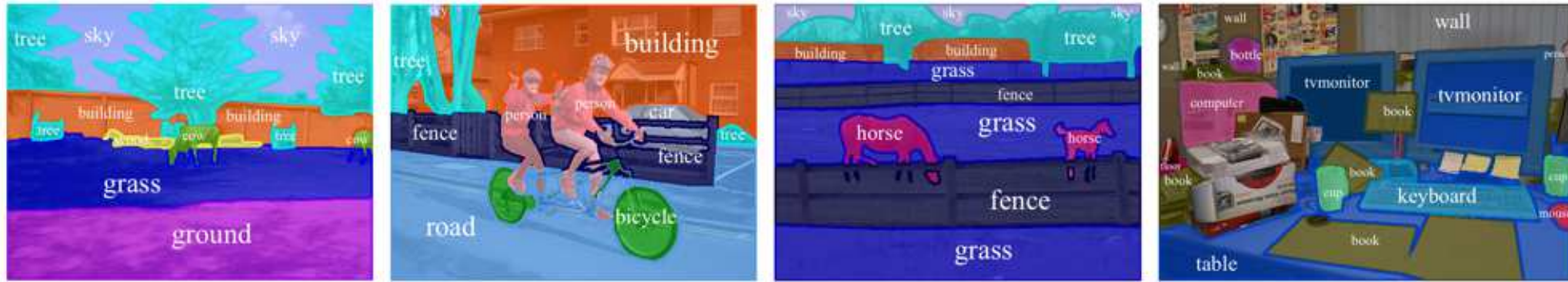
Building

Window

Door

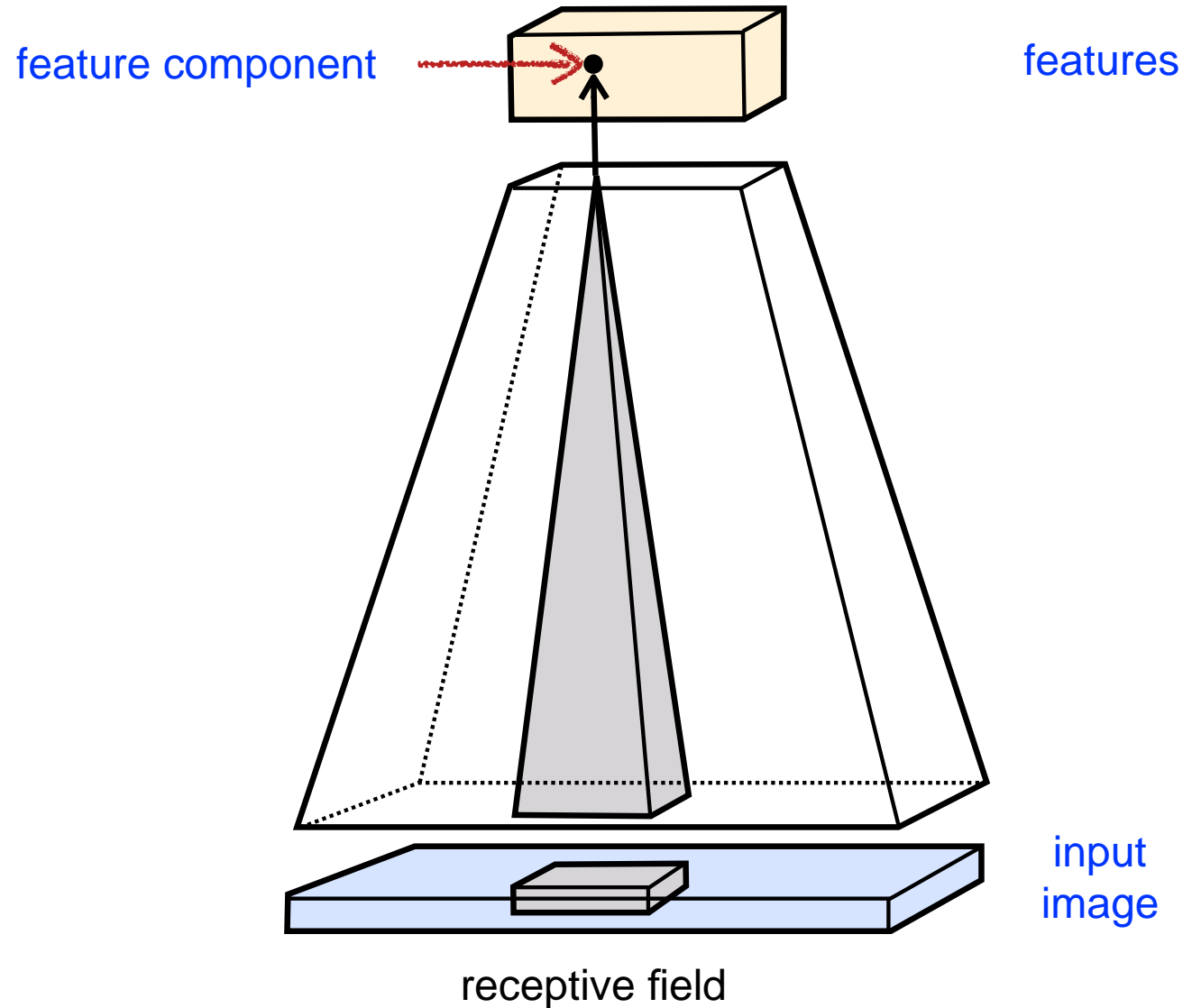
# Semantic Image Segmentation

- Label individual pixels



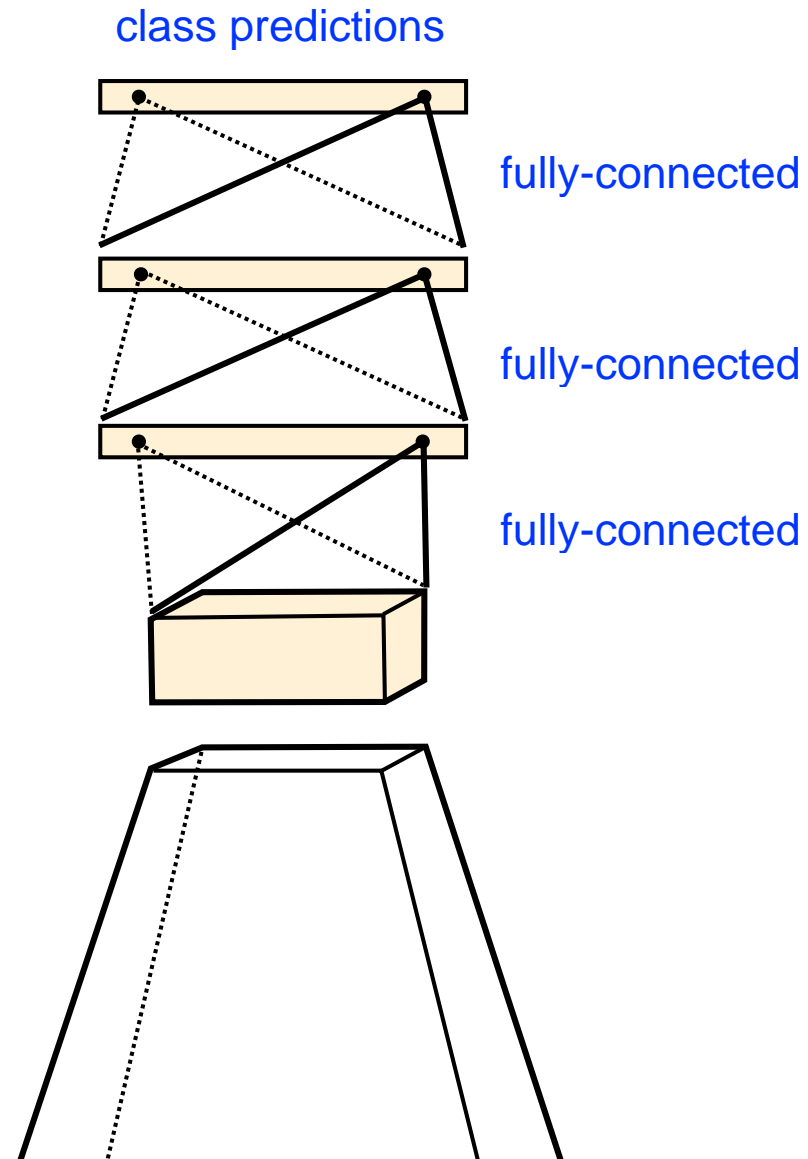
# Convolutional Layers

- Local receptive field



# Fully Connected Layers

- Global receptive field

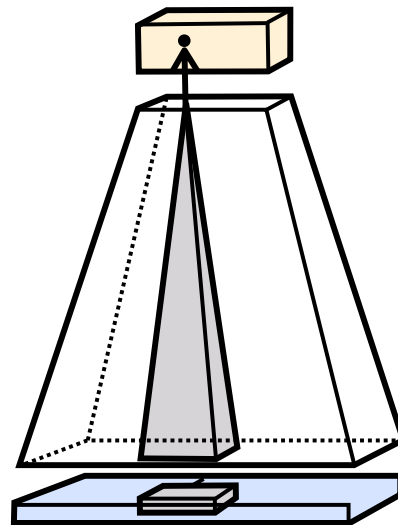


# Convolutional vs. Fully Connected

- Comparing the receptive fields

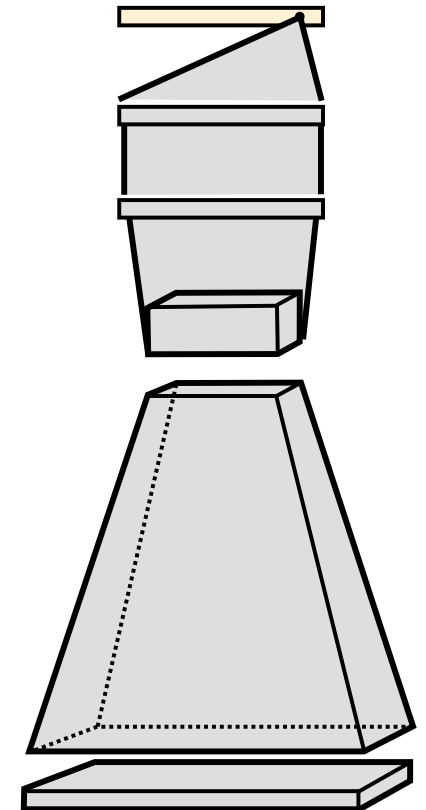
## Downsampling filters

Responses are spatially selective, can be used to localize things.



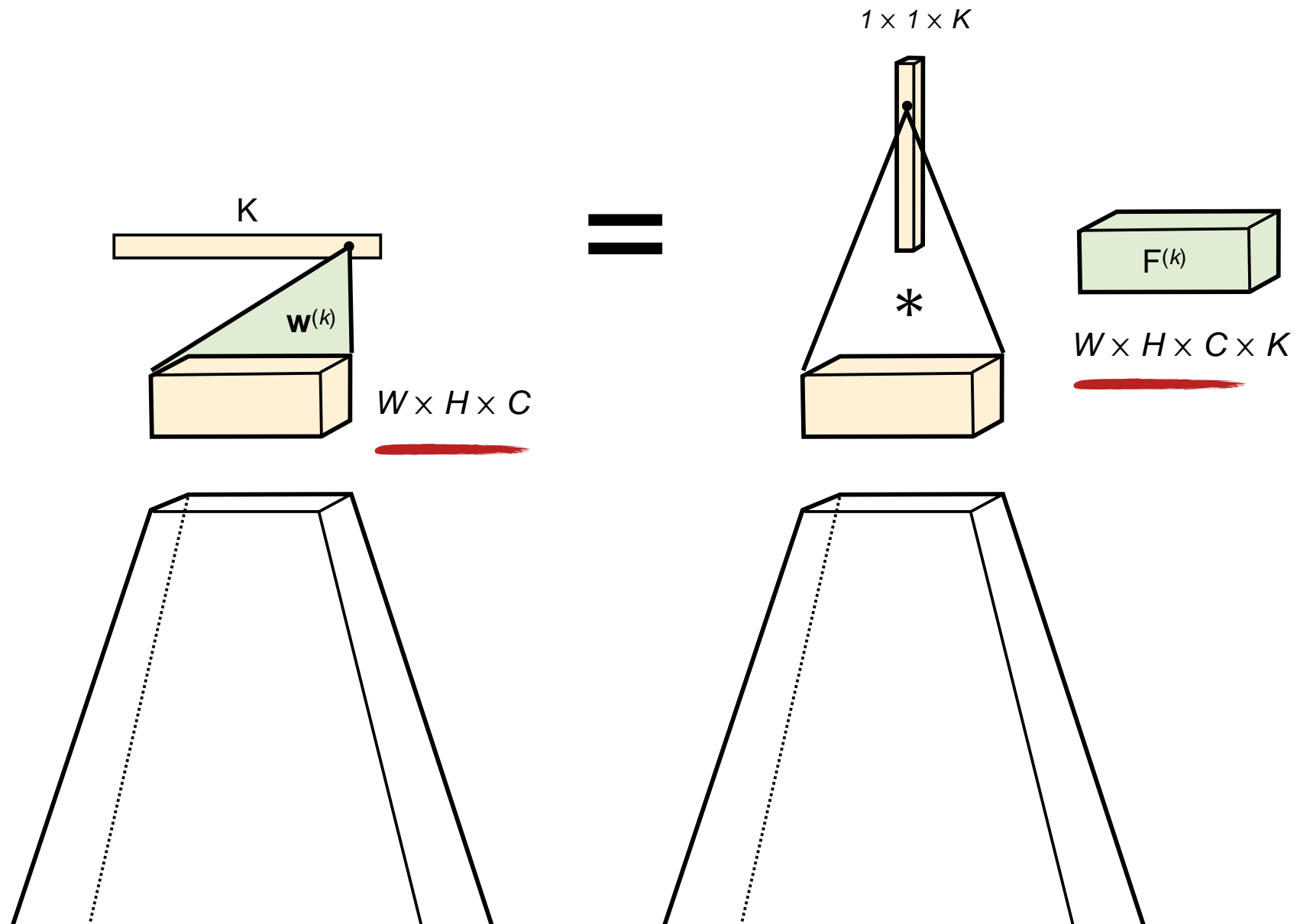
## Upsampling filters

Responses are global, do not characterize well position

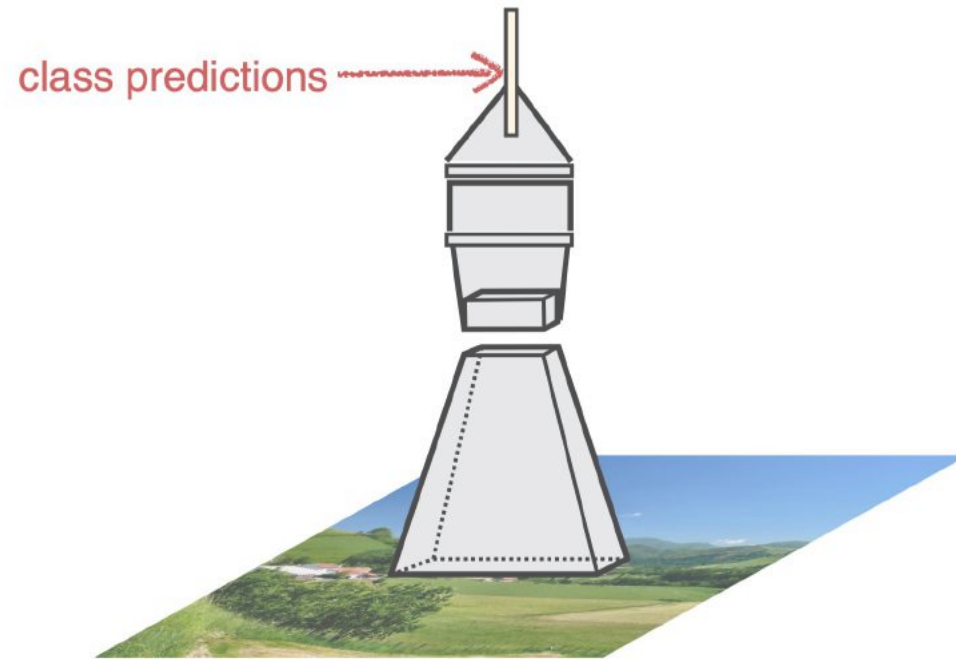


Which one is more useful for pixel level labelling?

# Fully-Connected Layer = Large Filter

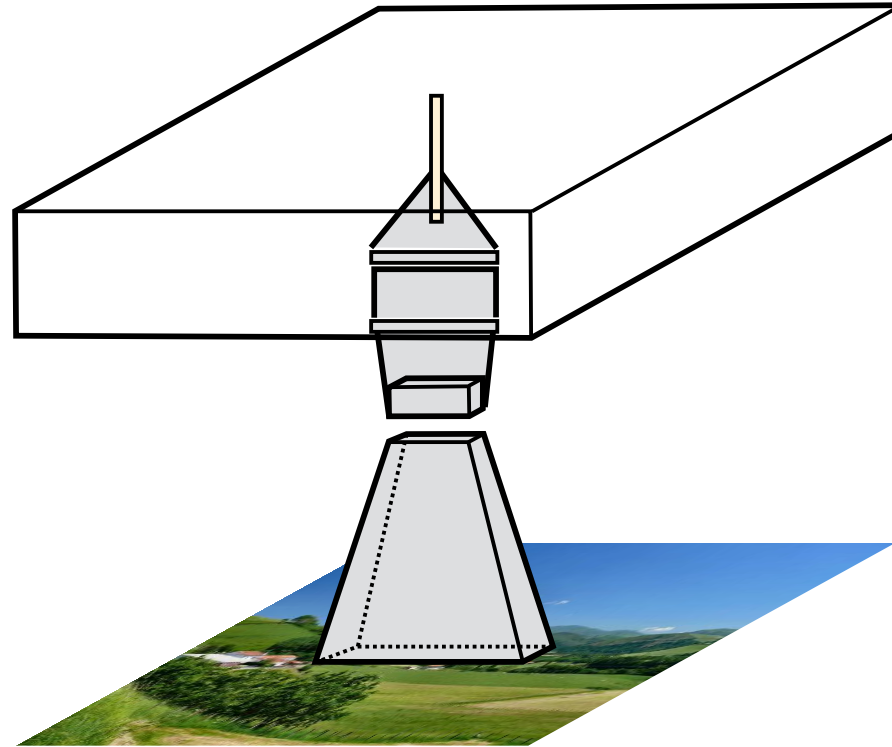


# Fully-Convolutional Neural Networks





# Fully-Convolutional Neural Networks



- **Dense evaluation**

- Apply the whole network convolutional
- Estimates a vector of class probabilities at each pixel

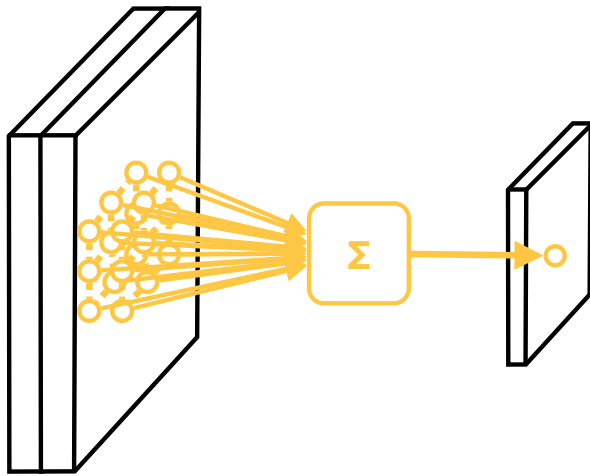
- **Downsampling**

- In practice most network downsample the data fast
- The output is very low resolution (e.g. 1/32 of original)

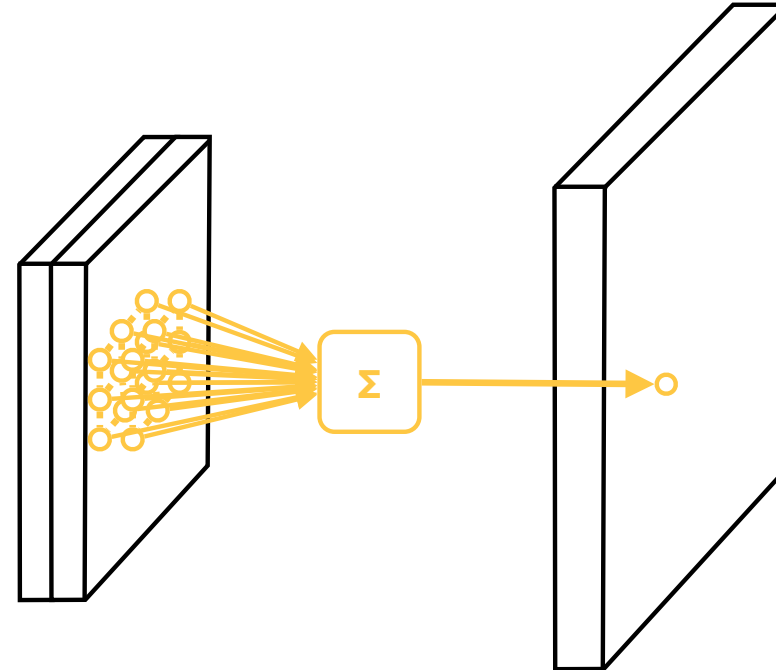
# Upsampling The Resolution

- Interpolating filter

**Downsampling filters**



**Upsampling filters**

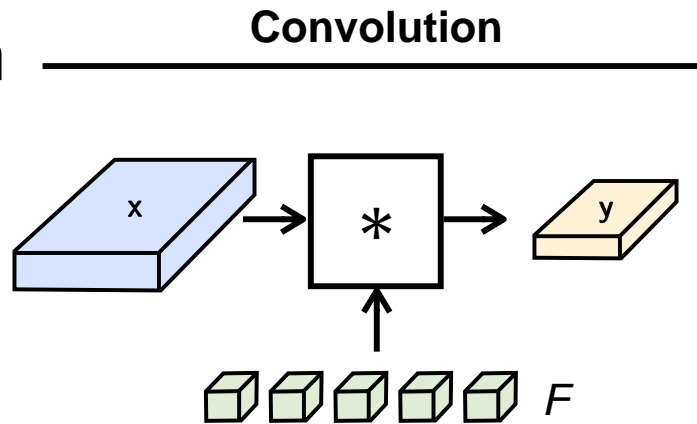


Upsampling filters allow to increase the resolution of the output

Very useful to get full-resolution segmentation results

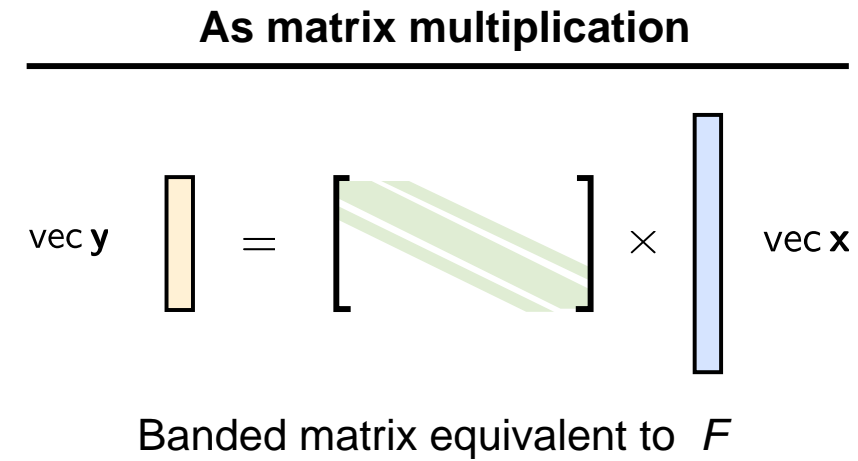
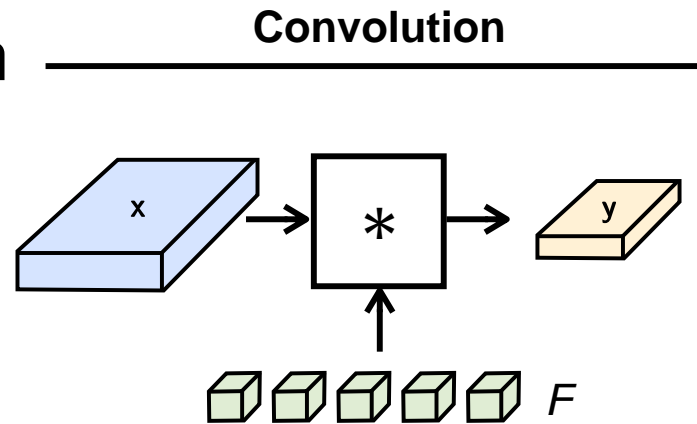
# Deconvolution Layer

- Or convolution transpose



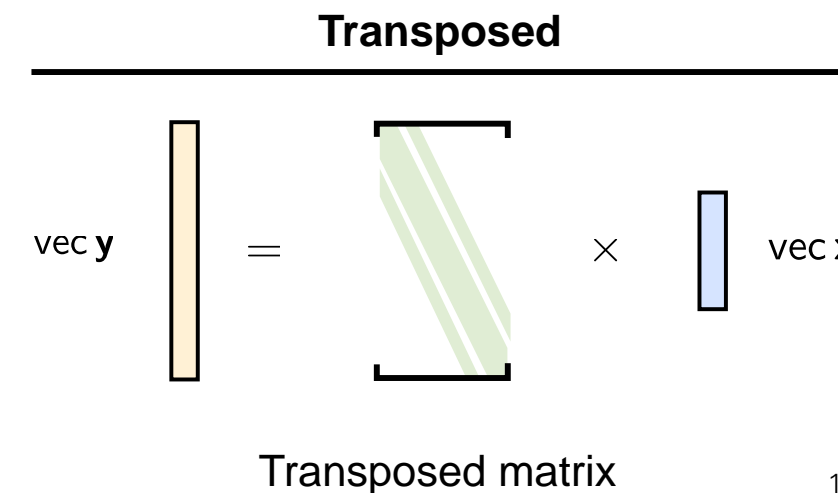
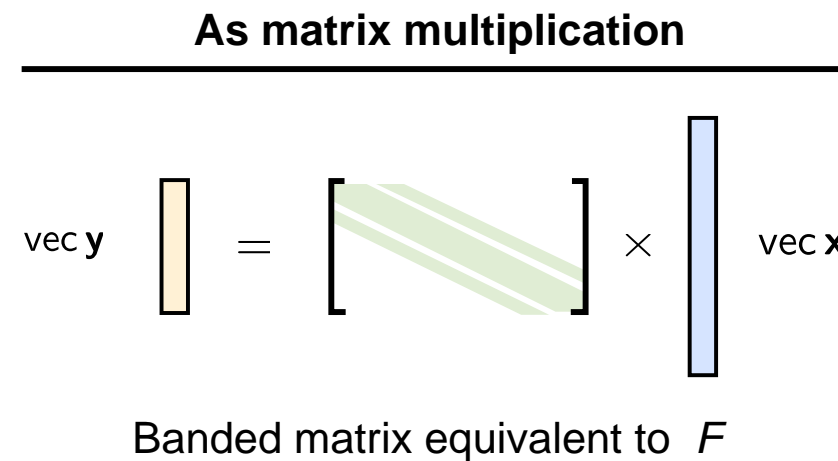
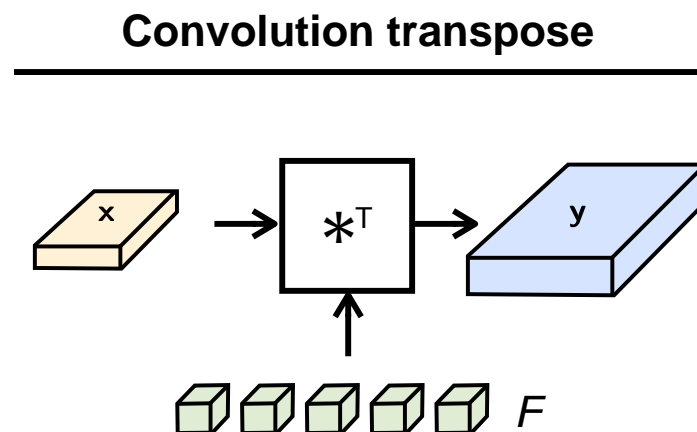
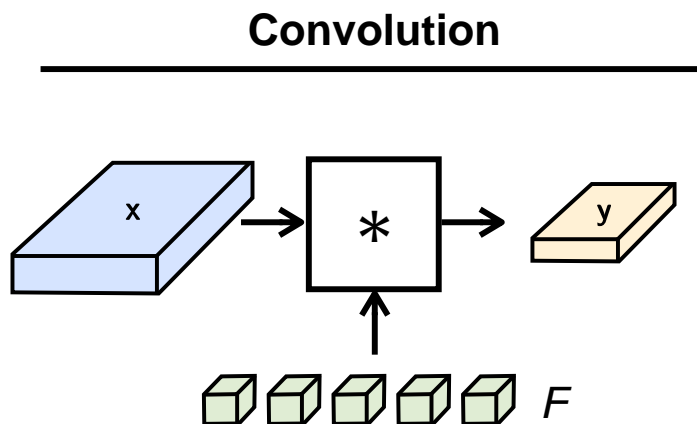
# Deconvolution Layer

- Or convolution transpose



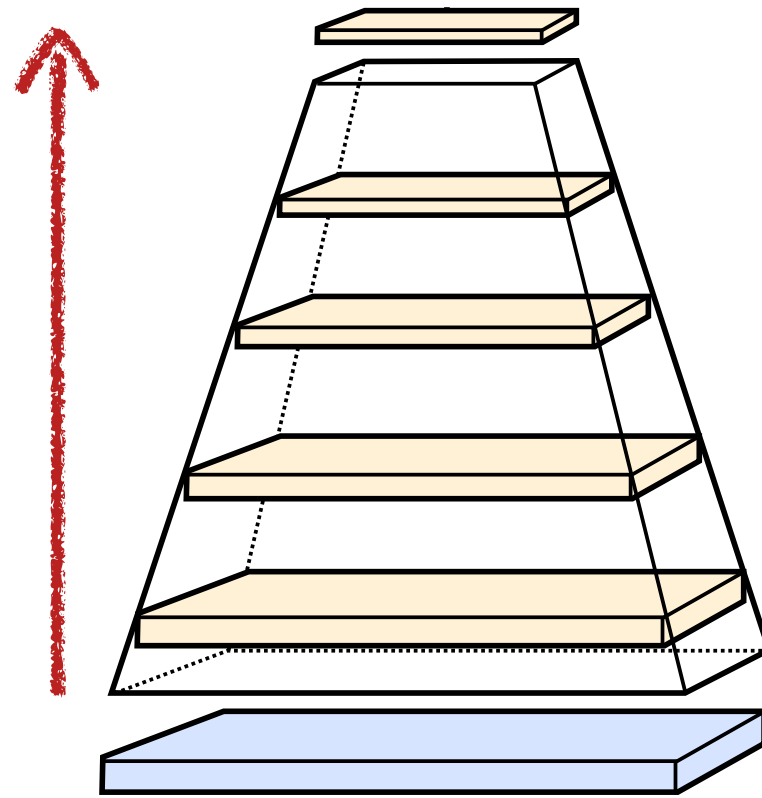
# Deconvolution Layer

- Or convolution transpose



# U-Architectures

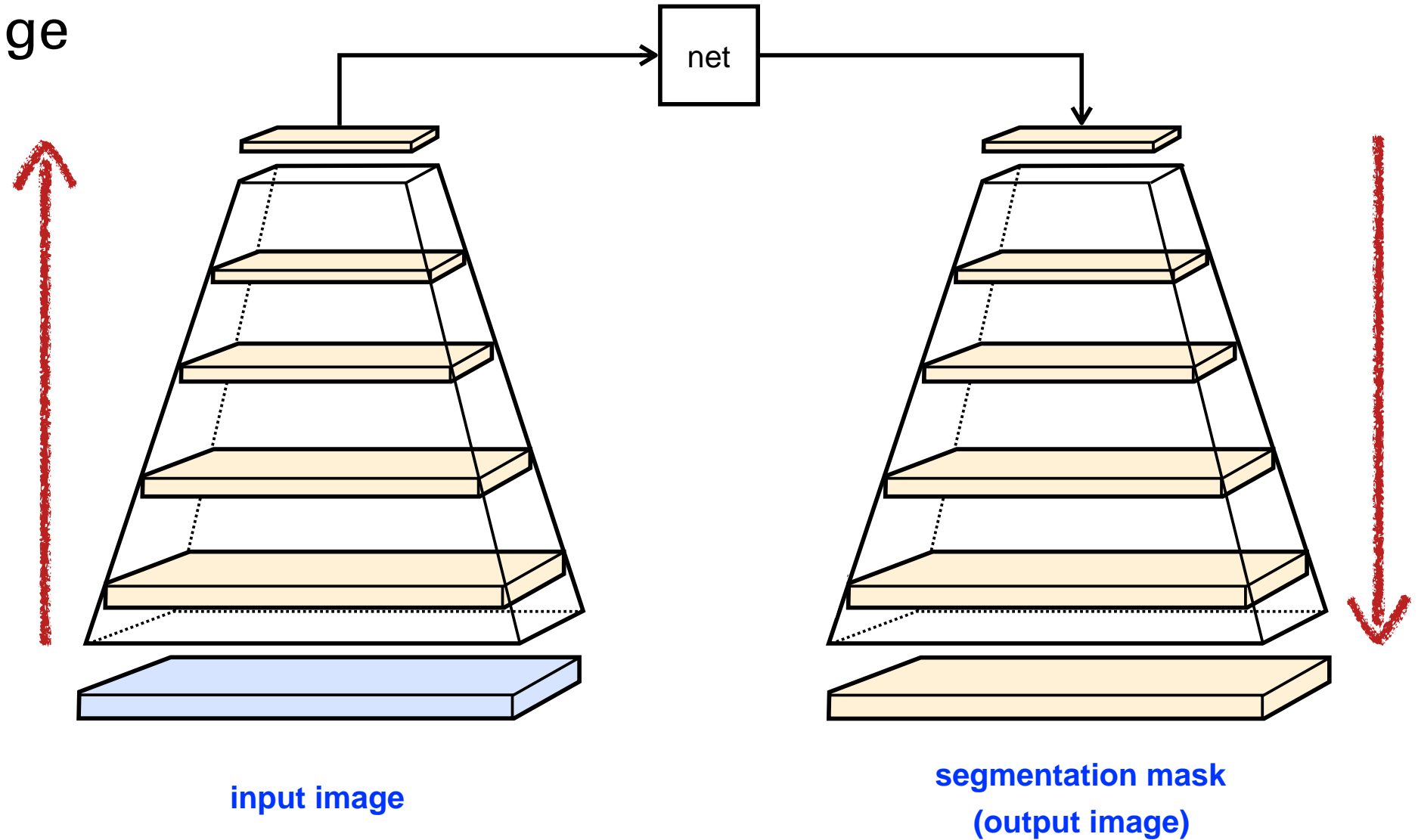
- Image to image



input image

# U-Architectures

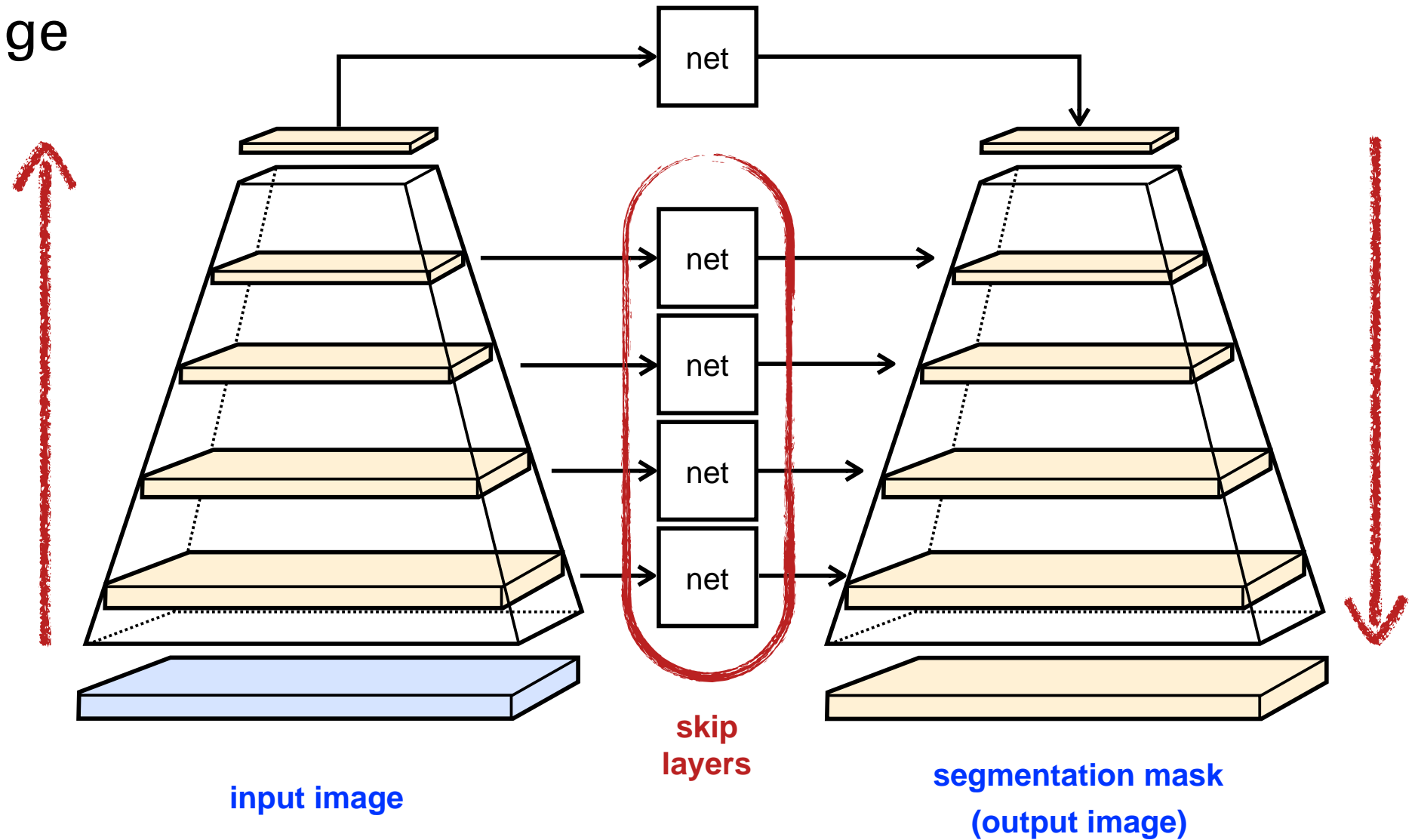
- Image to image





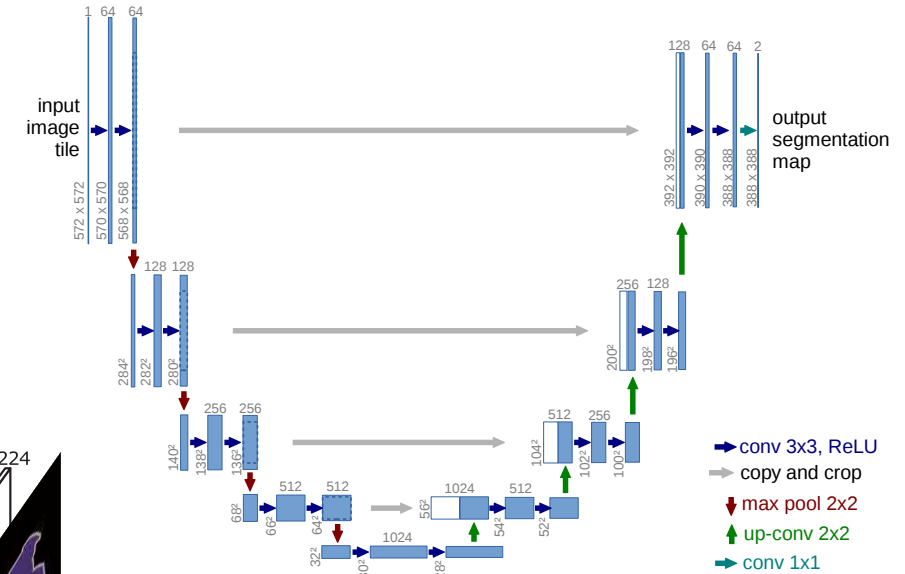
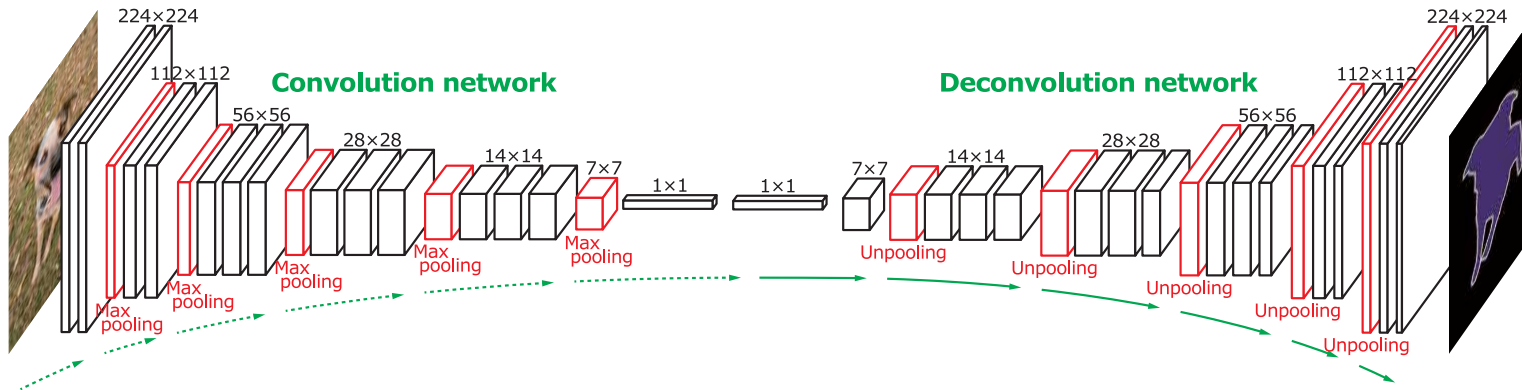
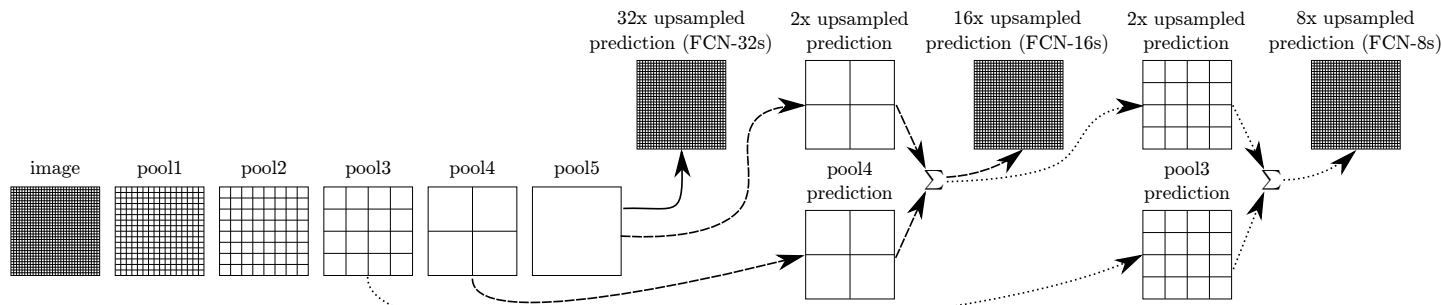
# U-Architectures

- Image to image



# U-Architectures

- Several variants: FCN, U-arch, deconvolution, ...



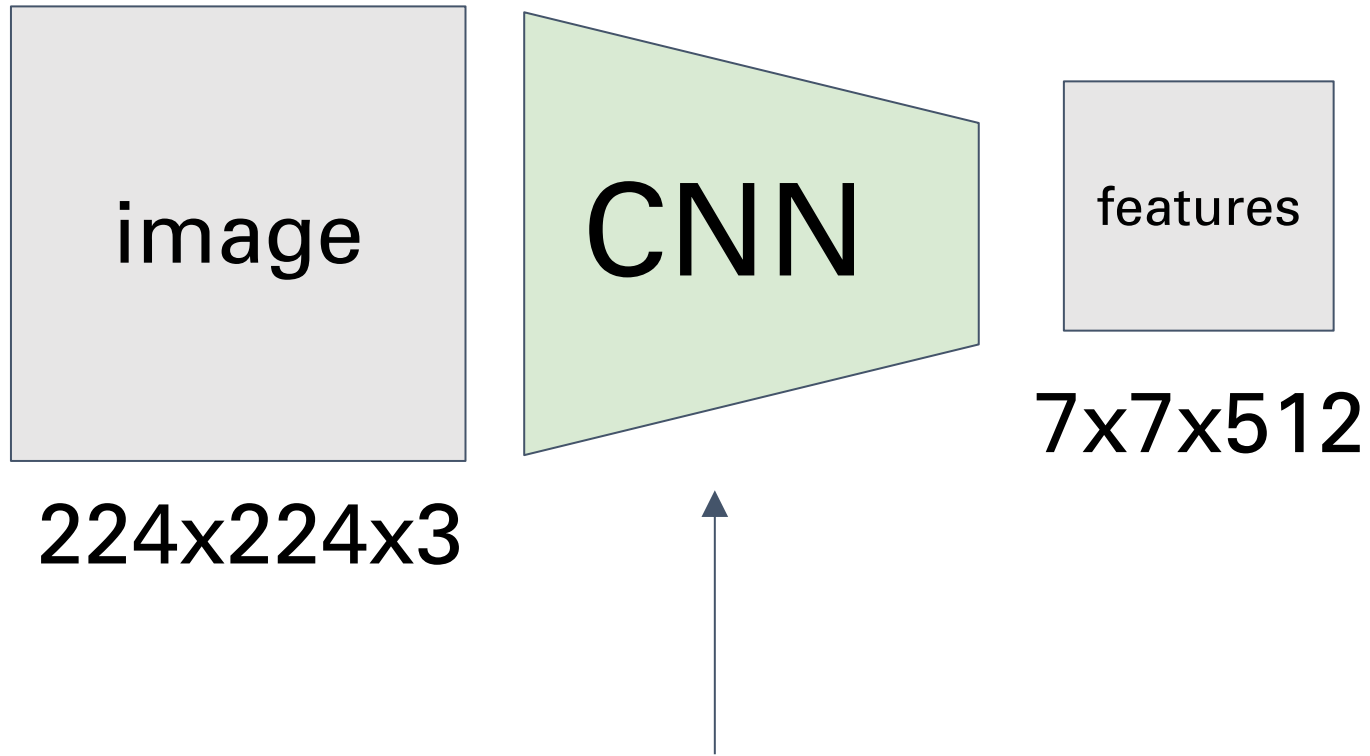
J. Long, E. Shelhamer, and T. Darrell. **Fully convolutional models for semantic segmentation.** In CVPR 2015

H. Noh, S. Hong, and B. Han. **Learning deconvolution network for semantic segmentation.** In ICCV 2015

O. Ronneberger, P. Fischer, and T. Brox. **U-net: Convolutional networks for biomedical image segmentation.** In MICCAI 2015

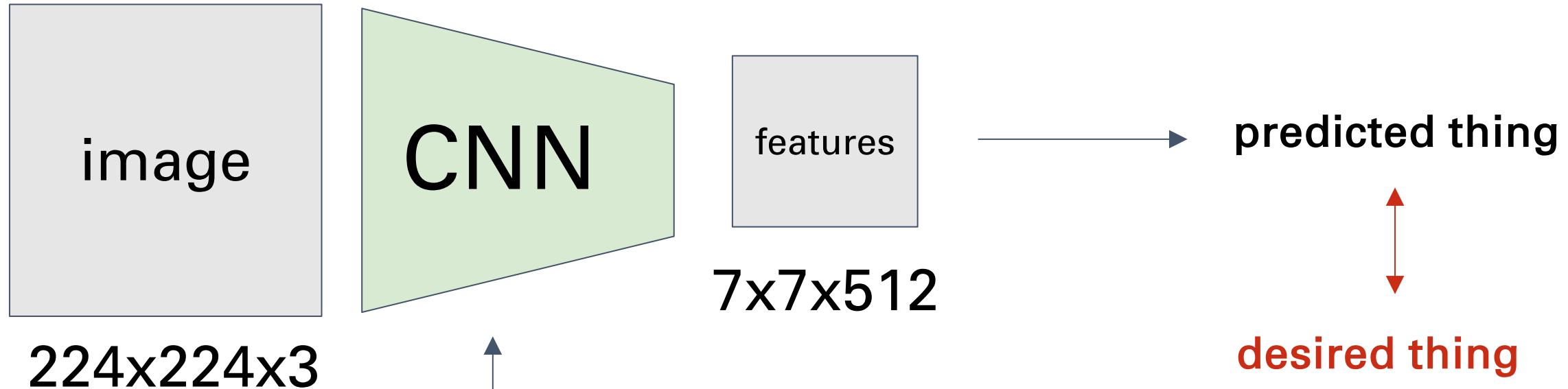
Addressing other tasks...

# Addressing other tasks...



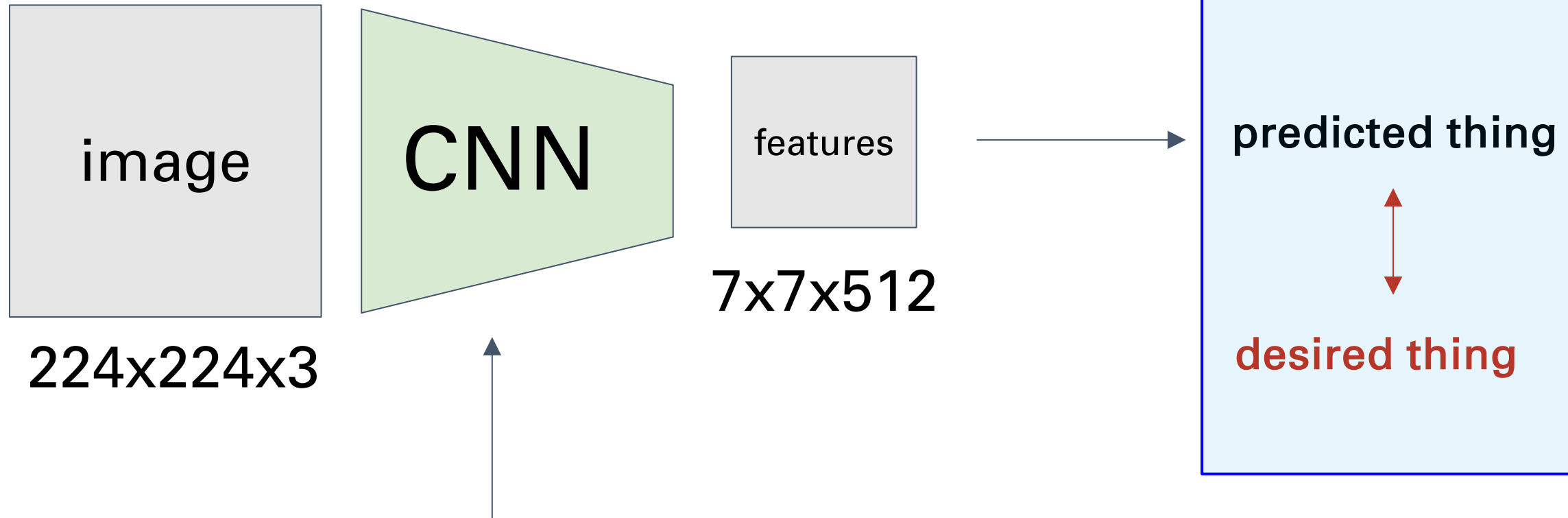
A block of compute with a few million parameters.

# Addressing other tasks...



A block of compute with a few million parameters.

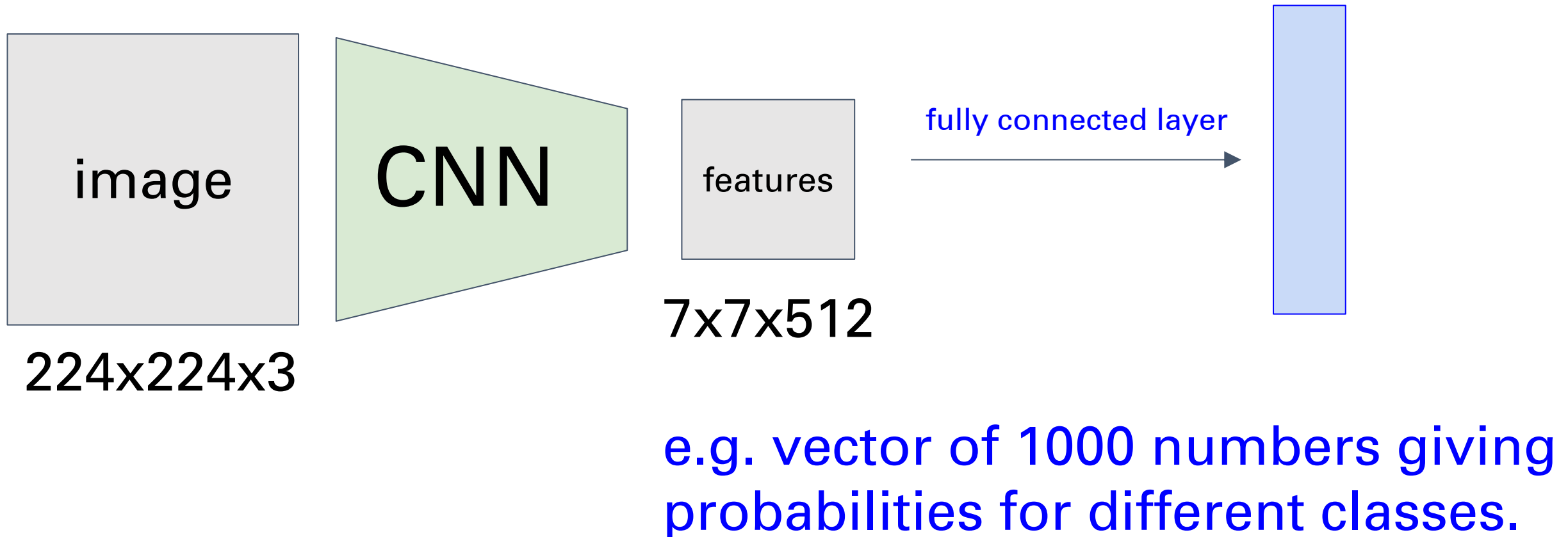
# Addressing other tasks...



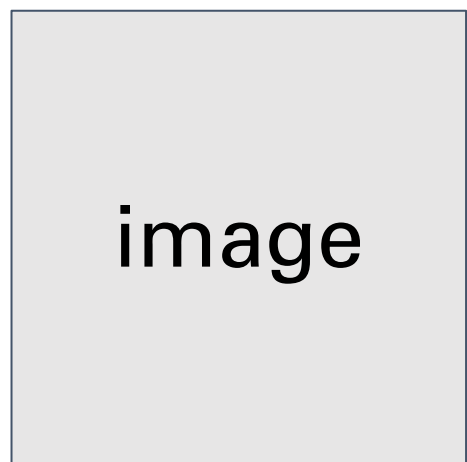
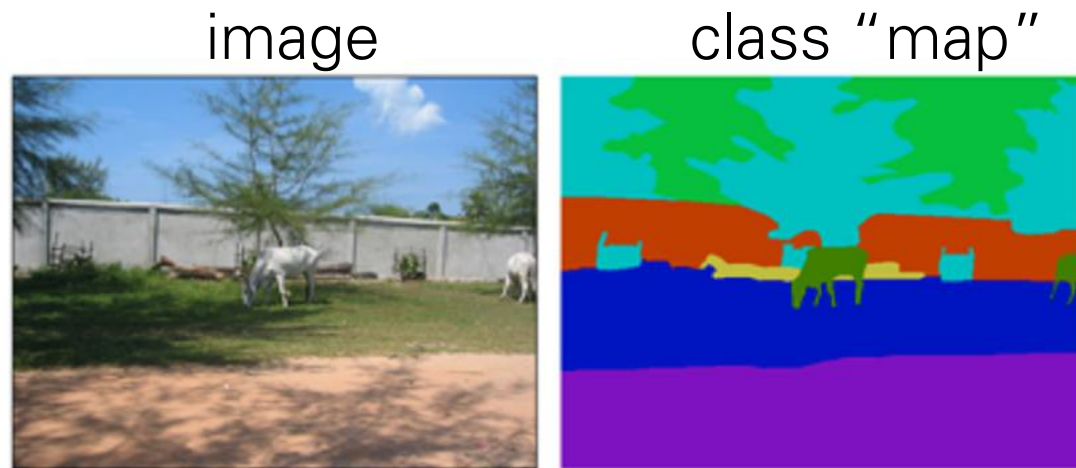
A block of compute with a few million parameters.

# Image Classification

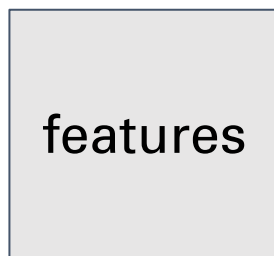
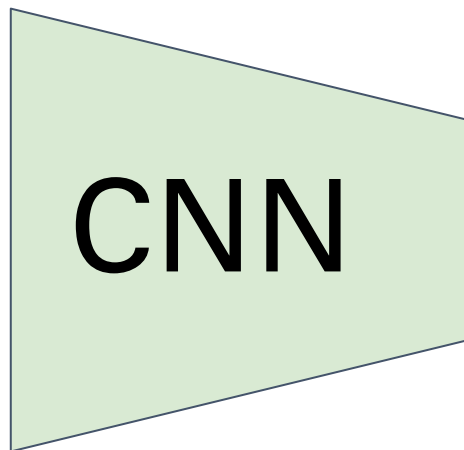
**thing** = a vector of probabilities for different classes



# Segmentation

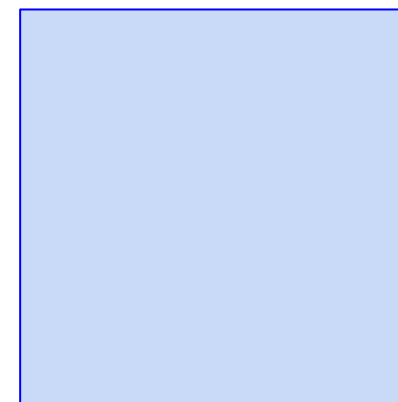


224x224x3



7x7x512

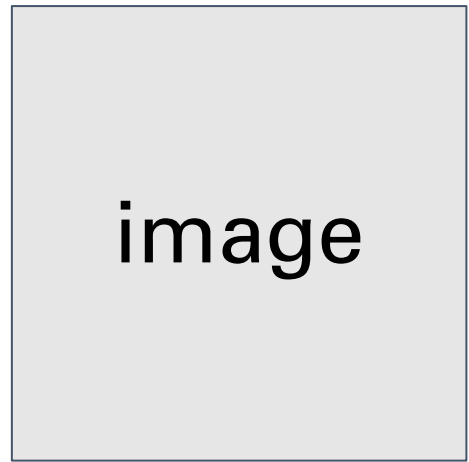
deconv layers



224x224x20  
array of class  
probabilities  
at each pixel.

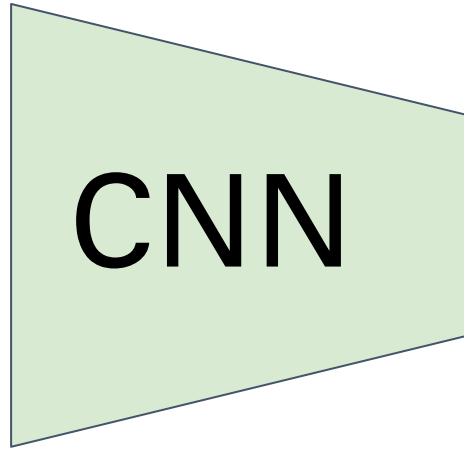


# Localization



image

224x224x3

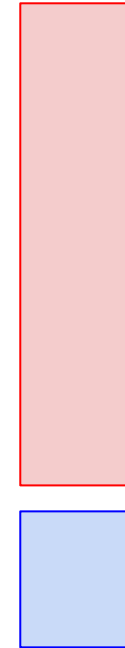


CNN



features

7x7x512

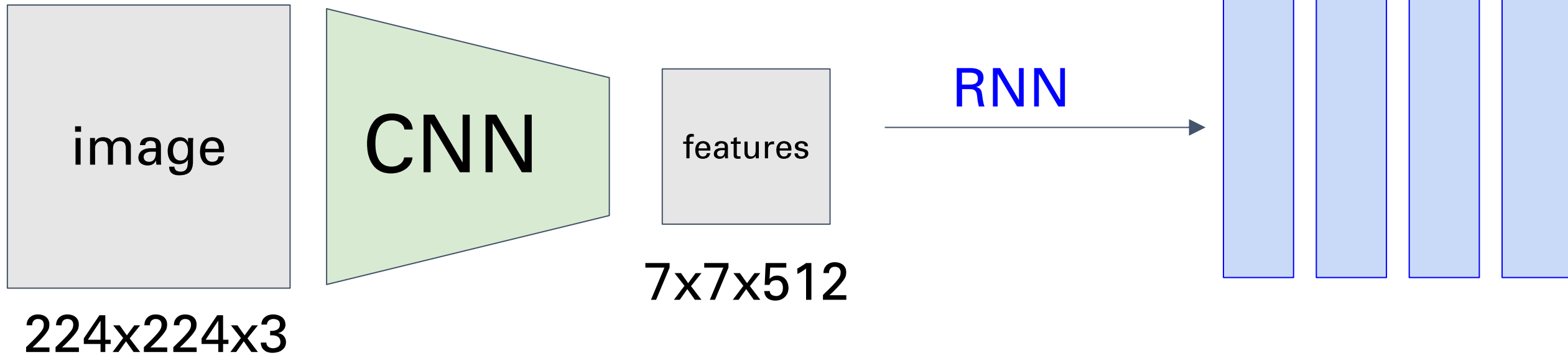


Class probabilities  
(as before)

4 numbers:

- X coord
- Y coord
- Width
- Height

# Image Captioning

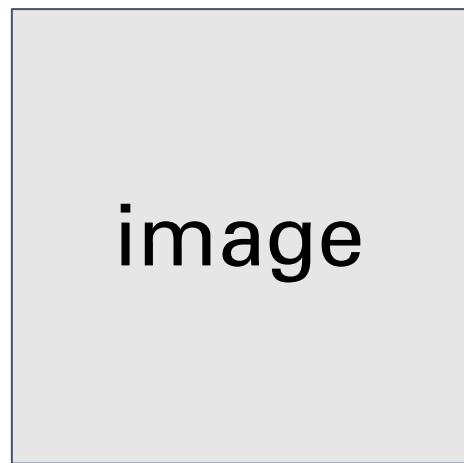


A sequence of 10,000-dimensional vectors giving probabilities of different words in the caption.

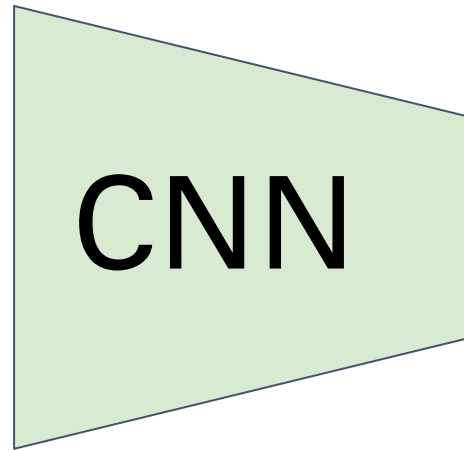
# Reinforcement Learning



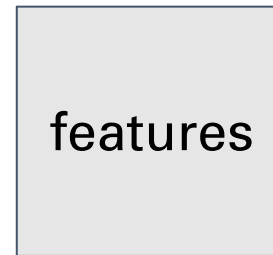
Mnih et al. 2015



image



CNN



features

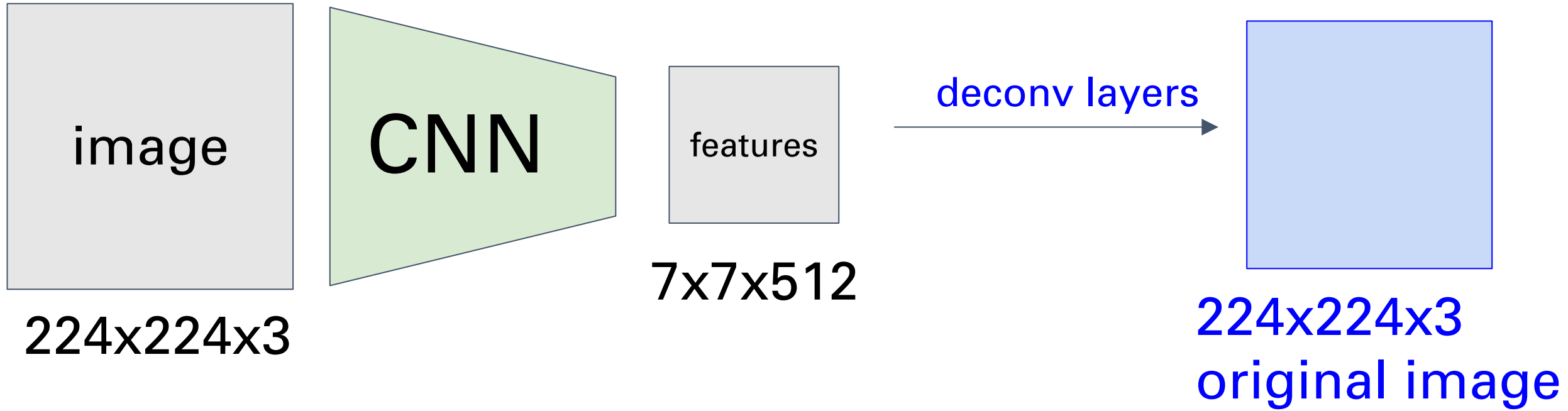
fully connected



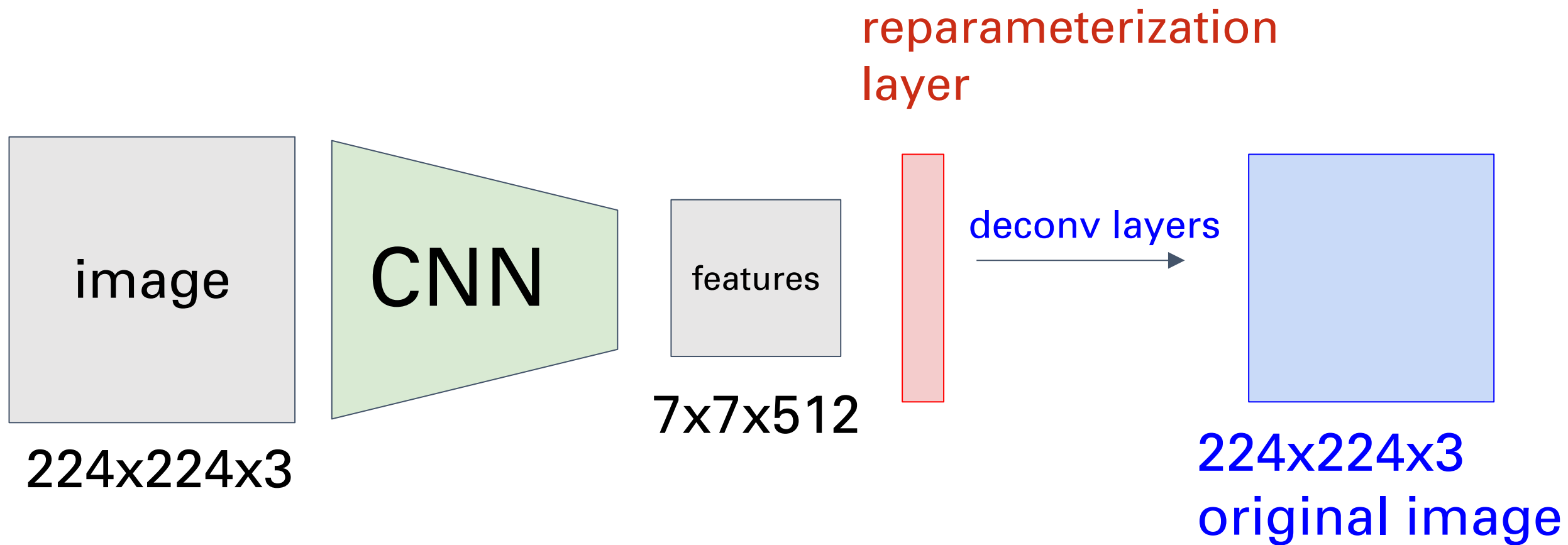
e.g. vector of 8 numbers giving probability of wanting to take any of the 8 possible ATARI actions.

160x210x3

# Autoencoders

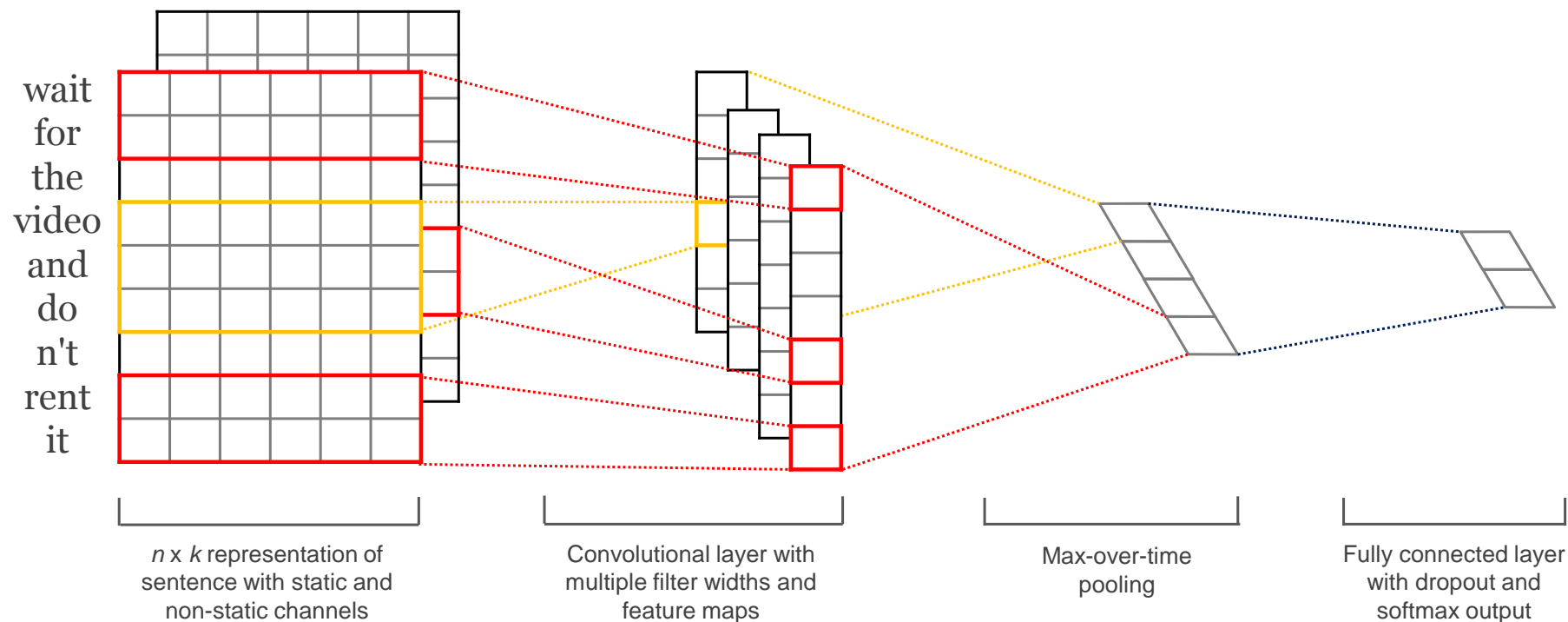


# Variational Autoencoders



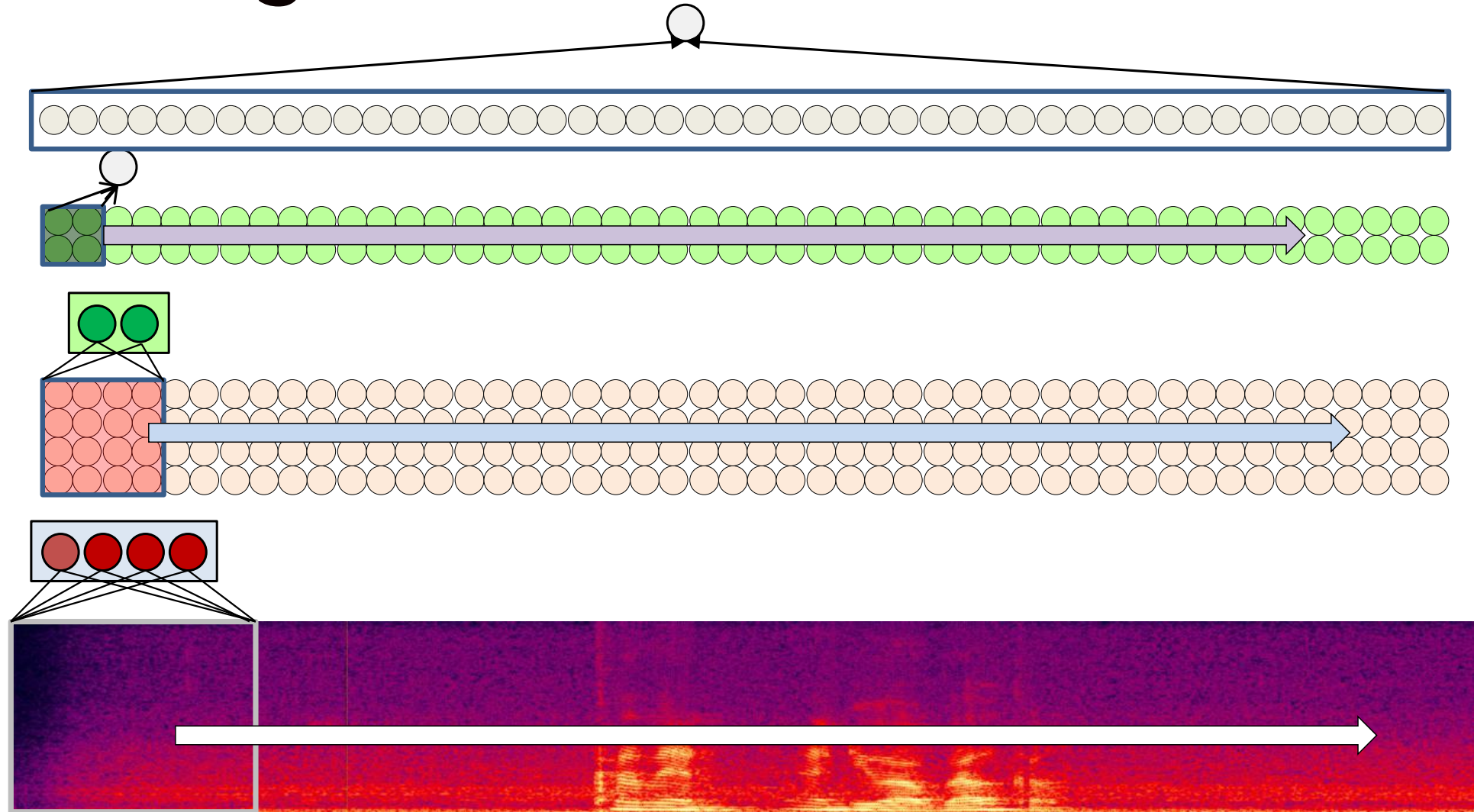
[Kingma et al.], [Rezende et al.], [Salimans et al.]

# Addressing other tasks...



- 1D convolution  $\approx$  Time Delay Neural Networks (Waibel et al. 1989, Collobert and Weston 2011)
- Two main paradigms:
  - **Context window modeling:** For tagging, etc. get the surrounding context before tagging
  - **Sentence modeling:** Do convolution to extract n-grams, pooling to combine over whole sentence

# Addressing other tasks...



- CNNs for audio processing: MFCC features + Time Delay Neural Networks

**Next lecture:**  
Understanding and Visualizing  
ConvNets