Loss Landscape created with data from the training process of a convolutional network, Javier Ideami

# COMP547 DEEP UNSUPERVISED LEARNING

#### Lecture #2 – Neural Networks Basics and Spatial Processing with CNNs



Aykut Erdem // Koç University // Spring 2022

# Previously on COMP547

- course logistics
- course topics
- what is deep unsupervised learning



Frame: Professor Farnsworth (Futurama)

#### Good news, everyone!

- Half of the class has completed the survey so far!
  - It will be up until everyone completes
- My office hour will be on Tuesdays btw 11:00-12:00 (will skip next week)

### Lecture overview

- deep learning
- computation in a neural net
- optimization
- backpropagation
- training tricks
- convolutional neural networks

- Disclaimer: Much of the material and slides for this lecture were borrowed from
  - —Costis Daskalakis and Aleksander Mądry's MIT 6.883 class
  - —Bill Freeman, Antonio Torralba and Phillip Isola's MIT 6.869 class



- Criticism of Perceptrons (XOR affair) [Minsky Papert '69]
  - Effectively causes a "deep learning winter"



# (Early) Spring



ABALLEL DISTRIBUTED

PROCESSING

FED



# What enabled this success?

• Better architectures (e.g., ReLUs) and regularization techniques



• Enough computational power









# Deep learning

- Modeling the world is incredibly complicated. We need high capacity models.
- In the past, we didn't have enough data to fit these models. But now we do!
- We want a class of high capacity models that are easy to optimize.

Deep neural networks!

#### What is deep learning

#### REVIEW

10

#### Deep learning

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"Deep learning allows computational models that are composed of multiple processing layers to learn representations of data with multiple levels of abstraction." – Yann LeCun, Yoshua Bengio and Geoff Hinton

Y. LeCun, Y. Bengio, G. Hinton, "Deep Learning", Nature, Vol. 521, 28 May 2015











Neural net



Deep neural net



### Gradient descent

$$egin{aligned} & heta^* = rgmin_{ heta} \sum_{i=1}^N \mathcal{L}(f_{ heta}(\mathbf{x}_i), \mathbf{y}_i) \ & \overbrace{J( heta)} \end{aligned}$$

#### Gradient descent



#### Gradient descent

$$egin{aligned} & heta^* = rgmin_{ heta} \sum_{i=1}^N \mathcal{L}(f_{ heta}(\mathbf{x}_i), \mathbf{y}_i) \ & \overbrace{J( heta)} \end{aligned}$$

One iteration of gradient descent:

$$\theta^{t+1} = \theta^t - \eta_t \frac{\partial J(\theta)}{\partial \theta} \bigg|_{\theta = \theta^t}$$
  
learning rate





 $y_j = \sum_i w_{ij} x_i$ 







# Example: linear regression with a neural net





$$f_{\mathbf{w},b}(\mathbf{x}) = \mathbf{x}^T \mathbf{w} + b$$











$$y = \mathbf{x}^T \mathbf{w} + b$$

$$(y) = \begin{cases} 1, & \text{if } y > 0 \\ 0, & \text{otherwise} \end{cases}$$

g



$$\hat{y} = \mathbf{x}^T \mathbf{w} + b$$
$$g(\hat{y}) = \begin{cases} 1, & \text{if } \hat{y} > 0\\ 0, & \text{otherwise} \end{cases}$$

$$\mathbf{w}^*, b^* = rgmin_{\mathbf{w},b} \mathcal{L}(g(\hat{y}), y_i)$$



$$\hat{y} = \mathbf{x}^T \mathbf{w} + b$$

$$g(\hat{y}) = \begin{cases} 1, & \text{if } \hat{y} > 0 \\ 0, & \text{otherwise} \end{cases}$$

$$\mathbf{w}^*, b^* = rgmin_{\mathbf{w},b} \mathcal{L}(g(\hat{y}), y_i)$$



### Computation in a neural net – nonlinearity



# Computation in a neural net – nonlinearity

- Interpretation as firing rate of neuron
- Bounded between [0,1]
- Saturation for large +/- inputs
- Gradients go to zero
- Outputs centered at 0.5 (poor conditioning)
- Not used in practice



# Computation in a neural net – nonlinearity

- Bounded between [-1,+1]
- Saturation for large +/- inputs
- Gradients go to zero
- Outputs centered at 0
- Preferable to sigmoid

tanh(x) = 2 sigmoid(2x) - 1

Tanh

$$g(y) = \frac{e^y - e^{-y}}{e^y + e^{-y}}$$


## Computation in a neural net – nonlinearity

- Unbounded output (on positive side)
- Efficient to implement:  $\frac{\partial g}{\partial y} = \begin{cases} 0, & \text{if } y < 0\\ 1, & \text{if } y \ge 0 \end{cases}$
- Also seems to help convergence (see 6x speedup vs tanh in [Krizhevsky et al.])
- Drawback: if strongly in negative region, unit is dead forever (no gradient).
- Default choice: widely used in current models.

Rectified linear unit (ReLU)

$$g(y) = \max(0, y)$$



### Computation in a neural net – nonlinearity

- where  $\alpha$  is small (e.g. 0.02)
- Efficient to implement:  $\frac{\partial g}{\partial y} = \begin{cases} -a, & \text{if } y < 0\\ 1, & \text{if } y \ge 0 \end{cases}$
- Also known as probabilistic ReLU (PReLU)
- Has non-zero gradients everywhere (unlike ReLU)
- α can also be learned (see Kaiming He et al. 2015).

Leaky ReLU  $g(y) = \begin{cases} \max(0, y), & \text{if } y \ge 0\\ a \min(0, y), & \text{if } y < 0 \end{cases}$ 5 4 3 0 -2 -40 2 y

# **Stacking layers**



$$\theta = \{ \mathbf{W}^{(1)}, \dots, \mathbf{W}^{(L)}, \mathbf{b}^{(1)}, \dots, \mathbf{b}^{(L)} \}$$

## **Representational power**

- 1 layer? Linear decision surface.
- 2+ layers? In theory, can represent any function. Assuming non-trivial non-linearity.
  - Bengio 2009,

http://www.iro.umontreal.ca/~bengioy/papers/ftml.pdf

- Bengio, Courville, Goodfellow book
   <a href="http://www.deeplearningbook.org/contents/mlp.html">http://www.deeplearningbook.org/contents/mlp.html</a>
- Simple proof by M. Neilsen
   <a href="http://neuralnetworksanddeeplearning.com/chap4.html">http://neuralnetworksanddeeplearning.com/chap4.html</a>
- D. Mackay book

http://www.inference.phy.cam.ac.uk/mackay/itprnn/ps/482.491.pdf

• But issue is efficiency: very wide two layers vs narrow deep model? In practice, more layers helps.



 $f(\mathbf{x}) = f_L(\dots f_2(f_1(\mathbf{x})))$ 

## **Classifier layer**

Last layer dolphin cat grizzly bear angel fish "clown fish" argmax chameleon clown fish iguana elephant . .

## Loss function



## Loss function



## Loss function







Probability of the observed data under the model

$$H(\mathbf{y}, \hat{\mathbf{y}}) = -\sum_{k=1}^{K} y_k \log \hat{y}_k$$









#### Tensors

$$\mathbf{h}^{(1)} \in \mathbb{R}^{N_{\texttt{batch}} \times C^{(1)}}$$

#### "Tensor flow"

$$\mathbf{h}^{(1)} \in \mathbb{R}^{N_{\texttt{batch}} \times H^{(1)} \times W^{(1)} \times C^{(1)}}$$



$$\mathbf{h}^{(2)} \in \mathbb{R}^{N_{\texttt{batch}} \times H^{(2)} \times W^{(2)} \times C^{(2)}}$$



# Regularizing deep nets

- Deep nets have millions of parameters!
- On many datasets, it is easy to overfit we may have more free parameters than data points to constrain them.
- How can we regularize to prevent the network from overfitting?
  - 1. Fewer neurons, fewer layers
  - 2. Weight decay
  - 3. Dropout
  - 4. Normalization layers
  - 5. ...

#### **Recall: regularized least squares**

$$f_{\theta}(x) = \sum_{k=0}^{K} \theta_k x^k$$

ridge regression, a.k.a., Tikhonov regularization

#### Probabilistic interpretation: R is a Gaussian prior over values of the parameters.

#### Recall: regularized least squares

$$\theta^* = rgmin_{ heta} \sum_{i=1}^N \mathcal{L}(f_{ heta}(\mathbf{x}_i), \mathbf{y}_i) + R( heta)$$

"We prefer to keep weights small."



$$\boldsymbol{\theta} = \{\mathbf{W}^{(1)}, \dots, \mathbf{W}^{(L)}, \mathbf{b}^{(1)}, \dots, \mathbf{b}^{(L)}\}$$

Randomly zero out hidden units.



$$\theta = \{\mathbf{W}^{(1)}, \dots, \mathbf{W}^{(L)}, \mathbf{b}^{(1)}, \dots, \mathbf{b}^{(L)}\}$$



$$\boldsymbol{\theta} = \{\mathbf{W}^{(1)}, \dots, \mathbf{W}^{(L)}, \mathbf{b}^{(1)}, \dots, \mathbf{b}^{(L)}\}$$



Prevents network from relying too much on spurious correlations between different hidden units.

Can be understood as averaging over an exponential **ensemble** of subnetworks. This averaging smooths the function, thereby reducing the effective capacity of the network.

#### Gradient descent



$$heta^* = rgmin_{ heta} \sum_{i=1}^N \mathcal{L}(f_{ heta}(\mathbf{x}_i), \mathbf{y}_i) \ \overbrace{J( heta)}^{N}$$

#### One iteration of gradient descent:

$$\theta^{t+1} = \theta^t - \eta_t \frac{\partial J(\theta)}{\partial \theta} \Big|_{\theta = \theta^t}$$
  
learning rate

#### Optimization



- What's the knowledge we have about J?
  - We can evaluate  $J(\theta)$  Gradient
  - We can evaluate  $J(\theta)$  and  $\dot{\nabla}_{\theta} J(\theta)$
  - We can evaluate  $\,J( heta)\!,\,\,
    abla_ heta J( heta)\!,\,\, 
    abla_ heta J( heta)\!,\,\, and\,\, H_ heta (J( heta))$
- Black box optimization
- First order optimization

Hessian

Second order optimization



# Stochastic gradient descent (SGD)

- Want to minimize overall loss function *J*, which is sum of individual losses over each example.
- In Stochastic gradient descent, compute gradient on sub-set (batch) of data. If batchsize=1 then θ is updated after each example. If batchsize=N (full set) then this is standard gradient descent.
- Gradient direction is noisy, relative to average over all examples (standard gradient descent).
- Advantages
  - Faster: approximate total gradient with small sample
  - Implicit regularizer
- Disadvantages
  - High variance, unstable updates

#### Momentum

- Basic idea: like a ball rolling down a hill, we should build up speed so as to make faster progress when "on a roll"
- Can dampen oscillations in SGD updates
- Common in popular variants of SGD
  - Nesterov's method
  - RMSProp
  - Adam



Raiders of the Lost Ark (excerp (Source: Lucasfilm/Paramount Pictures, 198

#### Why Momentum Really Works





We often think of Momentum as a means of dampening oscillations and speeding up the iterations, leading to faster convergence. But it has other interesting behavior. It allows a larger range of step-sizes to be used, and creates its own oscillations. What is going on?

GABRIEL GOHApril. 4Citation:UC Davis2017Goh, 2017

#### [https://distill.pub/2017/momentum/]

## **Comparison of gradient descent variants**



[http://ruder.io/optimizing-gradient-descent/]

# Forward pass

- Consider model with L layers. Layer l has vector of weights  $\mathbf{W}^{(l)}$
- Forward pass: takes input  $\mathbf{x}^{(l-1)}$  and passes it through each layer  $f^{(l)}$ :

 $\mathbf{x}^{(l)} = f^{(l)}(\mathbf{x}^{(l-1)}, \mathbf{W}^{(l)})$ 

- Output of layer l is  $\mathbf{x}^{(l)}$ .
- Network output (top layer) is  $\mathbf{x}^{(L)}$ .



# Forward pass

- Consider model with L layers. Layer l has vector of weights  $\mathbf{W}^{(l)}$
- Forward pass: takes input  $\mathbf{x}^{(l-1)}$  and passes it through each layer  $f^{(l)}$ :

 $\mathbf{x}^{(l)} = f^{(l)}(\mathbf{x}^{(l-1)}, \mathbf{W}^{(l)})$ 

- Output of layer l is  $\mathbf{x}^{(l)}$
- Network output (top layer) is  $\mathbf{x}^{(L)}$ .
- Loss function  $\mathcal{L}$  compares  $\mathbf{x}^{(L)}$  to  $\mathbf{y}$ .
- Overall energy is the sum of the cost over all training examples:  $J = \sum_{i=1}^{N} \mathcal{L}(\mathbf{x}_{i}^{(L)}, \mathbf{y}_{i})$

$$\begin{array}{c} & & & \\ & & \\ \hline \mathcal{L}(\mathbf{x}^{(L)}, \mathbf{y}) \\ \text{(output)} & \mathbf{x}^{(L)} \\ & & \\ f^{(L)}(\mathbf{x}^{(L-1)}, \mathbf{W}^{(L)}) \\ & & \\ & & \\ & & \\ f^{(l)}(\mathbf{x}^{(l-1)}, \mathbf{W}^{(l)}) \\ & & \\ & & \\ & & \\ f^{(l)}(\mathbf{x}^{(l-1)}, \mathbf{W}^{(l)}) \\ & & \\ & & \\ & & \\ f^{(2)}(\mathbf{x}^{(1)}, \mathbf{W}^{(2)}) \\ & & \\ & & \\ & & \\ f^{(1)}(\mathbf{x}^{(0)}, \mathbf{W}^{(1)}) \\ & & \\$$

T

## Gradient descent

• We need to compute gradients of the cost with respect to model parameters  $\mathbf{W}^{(l)}$ .

• By design, each layer is differentiable with respect to its parameters and input.

# **Computing gradients**

 To compute the gradients, we could start by writing the full energy J as a function of the network parameters.

$$J(\mathbf{W}) = \sum_{i=1}^{L} \mathcal{L}(f^{(L)}(\dots f^{(2)}(f^{(1)}(\mathbf{x}_i^{(0)}, \mathbf{W}^{(1)}), \mathbf{W}^{(2)}), \dots \mathbf{W}^{(L)}), \mathbf{y}_i$$

And then compute the partial derivatives... instead, we can use the chain rule to derive a compact algorithm: **backpropagation** 



# Backpropagation

• Forward pass: for each training example, compute the outputs for all layers:

$$\mathbf{x}^{(l)} = f^{(l)}(\mathbf{x}^{(l-1)}, \mathbf{W}^{(l)})$$

• Backwards pass: compute loss derivatives iteratively from top to bottom:

$$\frac{\partial \mathcal{L}}{\partial \mathbf{x}^{(l-1)}} = \frac{\partial \mathcal{L}}{\partial \mathbf{x}^{(l)}} \cdot \frac{\partial f^{(l)}(\mathbf{x}^{(l-1)}, \mathbf{W}^{(l)})}{\partial \mathbf{x}^{(l-1)}}$$

• Compute gradients w.r.t. weights, and update weights:

$$\frac{\partial \mathcal{L}}{\partial \mathbf{W}^{(l)}} = \frac{\partial \mathcal{L}}{\partial \mathbf{x}^{(l)}} \cdot \frac{\partial f^{(l)}(\mathbf{x}^{(l-1)}, \mathbf{W}^{(l)})}{\partial \mathbf{W}^{(l)}}$$


# Convolutional Neural Networks

### **Convolutional Neural Networks**

LeCun et al. 1989

Neural network with specialized connectivity



Tailored to processing natural signals with a grid topology (e.g., images).



### Image classification



### image **x**

label y















			Bird





Sky	Sky	Sky	Sky	Sky	Sky	Sky	Bird
Sky	Sky	Sky	Sky	Sky	Sky	Sky	Sky
Sky	Sky	Sky	Sky	Sky	Sky	Sky	Sky
Bird	Bird	Bird	Sky	Bird	Sky	Sky	Sky
Sky	Sky	Sky	Bird	Sky	Sky	Sky	Sky













(Colors represent one-hot codes)

This problem is called **semantic segmentation** in computer vision





An equivariant mapping: f(translate(x)) = translate(f(x)) Translation invariance: process each patch in the same way.

W computes a weighted sum of all pixels in the patch











W is a convolutional kernel applied to the full image!





### Convolution





### Fully-connected network

Fully-connected (fc) layer



### Locally connected network



Often, we assume output is a **local** function of input.

If we use the same weights (**weight sharing**) to compute each local function, we get a convolutional neural network.

### **Convolutional neural network**

#### Conv layer



Often, we assume output is a **local** function of input.

If we use the same weights (**weight sharing**) to compute each local function, we get a convolutional neural network.

## Weight sharing

#### Conv layer



Often, we assume output is a **local** function of input.

If we use the same weights (**weight sharing**) to compute each local function, we get a convolutional neural network.



- Constrained linear layer (infinitely strong regularization)
- Fewer parameters —> easier to learn, less overfitting







#### Conv layers can be applied to arbitrarily-sized inputs

## Five views on convolutional layers

1. Equivariant with translation (stationarity) f(translate(x)) = translate(f(x))

2. Patch processing (Markov assumption)

3. Image filter

- N/A
- 4. Parameter sharing



5. A way to process variable-sized tensors



### **Multiple channels**

#### Conv layer



 $\mathbb{R}^{N \times C} \to \mathbb{R}^{N \times 1}$ 

### **Multiple channels**

Conv layer



 $\mathbb{R}^{N \times C^{(0)}} \to \mathbb{R}^{N \times C^{(1)}}$ 

### Multiple channels

Conv layer



 $\mathbb{R}^{N \times C^{(l)}} \to \mathbb{R}^{N \times C^{(l+1)}}$ 



 $\mathbb{R}^{H \times W \times C^{(l)}} \rightarrow \mathbb{R}^{H \times W \times C^{(l+1)}}$ 

[Figure from Andrea Vedaldi]

### "Tensor flow"

$$\mathbf{x}^{(l)} \in \mathbb{R}^{N_{\texttt{batch}} \times H^{(l)} \times W^{(l)} \times C^{(l)}}$$

$$(I)M \times (I)H$$

$$\mathbf{x}^{(l+1)} \in \mathbb{R}^{N_{\texttt{batch}} \times H^{(l+1)} \times W^{(l+1)} \times C^{(l+1)}}$$



----

Pooling



Pooling



 $z_k = \max_{j \in \mathcal{N}(j)} g(y_j)$ 

 $z_k = rac{1}{|\mathcal{N}|} \sum_{j \in \mathcal{N}(j)} g(y_j)$ 

## Pooling – Why?

Pooling across spatial locations achieves stability w.r.t. small translations:



## Pooling – Why?

Pooling across spatial locations achieves stability w.r.t. small translations:





large response regardless of exact position of edge

## Pooling – Why?

Pooling across spatial locations achieves stability w.r.t. small translations:


#### CNNs are stable w.r.t. diffeomorphisms





["Unreasonable effectiveness of Deep Features as a Perceptual Metric", Zhang et al. 2018]

 $\approx$ 

# Pooling – Why?

Pooling across feature channels (filter outputs) can achieve other kinds of invariances:



[Derived from slide by Andrea Vedaldi]

#### Computation in a neural net



 $f(\mathbf{x}) = f_L(\dots f_2(f_1(\mathbf{x})))$ 

#### Downsampling

Filter Pool and downsample



#### Downsampling

Filter

Downsample



 $\mathbb{R}^{H^{(l)} \times W^{(l)} \times C^{(l)}} \to \mathbb{R}^{H^{(l+1)} \times W^{(l+1)} \times C^{(l+1)}}$ 

### Strided convolution

#### Conv layer



**Strided convolutions** combine convolution and downsampling into a single operation.

#### Computation in a neural net



$$f(\mathbf{x}) = f_L(\dots f_2(f_1(\mathbf{x})))$$

# **Receptive fields**





#### **Effective Receptive Field**

Contributing input units to a convolutional filter.

#### @jimmfleming // fomoro.com



[http://fomoro.com/tools/receptive-fields/index.html]

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To appear in: Handbook of Video and Image Processing, 2nd edition ed. Alan Bovik, @Academic Press, 2005.

#### 4.7 Statistical Modeling of Photographic Images

D @ Q Search

rameters (possibly random variables themselves) govern

#### Eero P. Simoncelli

New York University

January 18, 2005

The set of all possible visual images is huge, but not all of these are equally likely to be encountered by an imaging tain degree of adaptability of the model to different types



Why CNNs?

**Fig. 1.** (a) Scatterplots of pairs of pixels at three different spatial displacements, averaged over five examples images. (b) Autocorrelation function. Photographs are of New York City street scenes, taken with a Canon 10D digital camera, and processed in RAW linear sensor mode (producing pixel intensities are in roughly proportional to light intensity). Correlations were computed on the logs of these sensor intensity values [41].

#### [http://6.869.csail.mit.edu/fa18/notes/simoncelli2005.pdf]

# Why CNNs?

Statistical dependences between pixels decay as a power law of distance between the pixels.

It is therefore often sufficient to model local dependences only.  $\rightarrow$  Convolution

More generally, we should allocate parameters that model dependences in proportion to the strength of those dependences.  $\rightarrow$  Multiscale, hierarchical representations

[For more discussion, see "Why does Deep and Cheap Learning Work So Well?", Lin et al. 2017]

# Why CNNs?

Capturing long-range dependences:



# Deep Neural Networks for Visual Recognition



Error: 4.4%

#### 2012: AlexNet 5 conv. layers

11x11 conv, 96, /4, pool/2
*
5x5 conv, 256, pool/2
*
3x3 conv, 384
*
3x3 conv, 384
*
3x3 conv, 256, pool/2
★
fc, 4096
*
fc, 4096
*
fc, 1000

Error: 15.3%

2014: VGG 16 conv. layers



#### Error: 8.5%

#### VERY DEEP CONVOLUTIONAL NETWORKS FOR LARGE-SCALE IMAGE RECOGNITION

https://arxiv.org/pdf/1409.1556.pdf

Small convolutional kernels: 3x3 ReLu non-linearities >100 million parameters.





# **Chaining convolutions**





25 coefficients, but only 18 degrees of freedom



# **Dilated convolutions**





25 coefficients9 degrees of freedom

=





49 coefficients18 degrees of freedom

[https://arxiv.org/pdf/1511.07122.pdf]



Figure 1: Systematic dilation supports exponential expansion of the receptive field without loss of resolution or coverage. (a)  $F_1$  is produced from  $F_0$  by a 1-dilated convolution; each element in  $F_1$  has a receptive field of  $3 \times 3$ . (b)  $F_2$  is produced from  $F_1$  by a 2-dilated convolution; each element in  $F_2$  has a receptive field of  $7 \times 7$ . (c)  $F_3$  is produced from  $F_2$  by a 4-dilated convolution; each element in  $F_3$  has a receptive field of  $15 \times 15$ . The number of parameters associated with each layer is identical. The receptive field grows exponentially while the number of parameters grows linearly.

2016: ResNet >100 conv. layers

#### **Deep Residual Learning for Image Recognition**



Error: 4.4%

3x3 conv, 51

fc 1000

If output has same size as input:



If output has a different size:



## **Residual Learning**



• The loss surface of a 56-layer net using the CIFAR-10 dataset, both without (left) and with (right) residual connections.

Hao Li et al., "Visualizing the Loss Landscape of Neural Nets". ICLR 2018

# Other good things to know

- Check gradients numerically by finite differences
- Visualize hidden activations should be uncorrelated and high variance



Good training: hidden units are sparse across samples and across features.

[Derived from slide by Marc'Aurelio Ranzato]

# Other good things to know

- Check gradients numerically by finite differences
- Visualize hidden activations should be uncorrelated and high variance



Bad training: many hidden units ignore the input and/or exhibit strong correlations.

[Derived from slide by Marc'Aurelio Ranzato]

# Other good things to know

- Check gradients numerically by finite differences
- Visualize hidden activations should be uncorrelated and high variance
- Visualize filters



Good training: learned filters exhibit structure and are uncorrelated.

[Derived from slide by Marc'Aurelio Ranzato]



$$\hat{h}_k = rac{h_k - \mathbb{E}[h_k]}{\sqrt{ extsf{Var}[h_k]}}$$

Keep track of mean and variance of a unit (or a population of units) over time.

Standardize unit activations by subtracting mean and dividing by variance.

Squashes units into a **standard range**, avoiding overflow.

Also achieves **invariance** to mean and variance of the training signal.

Both these properties reduce the effective capacity of the model, i.e. regularize the model.



Normalize w.r.t. a single hidden unit's pattern of activation over training examples (a batch of examples).



Normalize w.r.t. the mean and variance of the activations of all the hidden units (neurons) on this layer (c).



Normalize w.r.t. the mean and variance of the activations of all the hidden units (neurons) on this layer (c) that process this particular location (h,w) in the image.



Might as well...



QQ 🖞 🖉 🗸 🗂 🙆 Q search

#### Published as a conference paper at ICLR 2021

#### CHARACTERIZING SIGNAL PROPAGATION TO CLOSE THE PERFORMANCE GAP IN UNNORMALIZED RESNETS

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#### ABSTRACT

Batch Normalization is a key component in almost all state-of-the-art image classifiers, but it also introduces practical challenges: it breaks the independence between training examples within a batch, can incur compute and memory overhead, and often results in unexpected bugs. Building on recent theoretical analyses of deep ResNets at initialization, we propose a simple set of analysis tools to characterize signal propagation on the forward pass, and leverage these tools to design highly performant ResNets without activation normalization layers. Crucial to our success is an adapted version of the recently proposed Weight Standardization. Our analysis tools show how this technique preserves the signal in networks with ReLU or Swish activation functions by ensuring that the per-channel activation means do not grow with depth. Across a range of FLOP budgets, our networks attain performance competitive with the state-of-the-art EfficientNets on ImageNet.

#### 1 INTRODUCTION

BatchNorm has become a core computational primitive in deep learning (Ioffe & Szegedy, 2015), and it is used in almost all state-of-the-art image classifiers (Tan & Le; 2019; Wei et al., 2020). A number of different benefits of BatchNorm have been identified. It smoothens the loss landscape (Santurkar et al., 2018), which allows training with larger learning rates (Bjorck et al., 2018), and the noise arising from the minibatch estimates of the batch statistics introduces implicit regularization (Luo et al., 2019). Crucially, recent theoretical work (Balduzzi et al., 2017; De & Smith, 2020) has demonstrated that BatchNorm ensures good signal propagation at initialization in deep residual networks with identity skip connections (He et al., 2016b;a), and this benefit has enabled practitioners to train deep ResNets with hundreds or even thousands of layers (Zhang et al., 2019).

However RatchNorm also has many disadvantages. Its hebayior is strongly dependent on the batch

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rXiv:2102.06171

#### Q Q 🖞 🖉 🗸 🖒 🛇 Q Search

#### High-Performance Large-Scale Image Recognition Without Normalization

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#### Abstract

Batch normalization is a key component of most image classification models, but it has many undesirable properties stemming from its dependence on the batch size and interactions between examples. Although recent work has succeeded in training deep ResNets without normalization lavers, these models do not match the test accuracies of the best batch-normalized networks, and are often unstable for large learning rates or strong data augmentations. In this work, we develop an adaptive gradient clipping technique which overcomes these instabilities, and design a significantly improved class of Normalizer-Free ResNets. Our smaller models match the test accuracy of an EfficientNet-B7 on ImageNet while being up to 8.7× faster to train, and our largest models attain a new state-of-the-art top-1 accuracy of 86.5%. In addition, Normalizer-Free models attain significantly better performance than their batch-normalized counterparts when finetuning on ImageNet after large-scale pre-training on a dataset of 300 million labeled images, with our best models obtaining an accuracy of 89.2%.2

#### 1. Introduction

The vast majority of recent models in computer vision are variants of deep residual networks (He et al., 2016b;a), trained with batch normalization (Ioffe & Szegedy, 2015).



Figure 1. ImageNet Validation Accuracy vs Training Latency. All numbers are single-model, single crop. Our NFNet-F1 model achieves comparable accuracy to an EffNet-B7 while being 8.7× faster to train. Our NFNet-F5 model has similar training latency to EffNet-B7, but achieves a state-of-the-art 86.0% top-1 accuracy on ImageNet. We further improve on this using Sharpness Aware Minimization (Foret et al., 2021) to achieve 86.5% top-1 accuracy

However, batch normalization has three significant practical disadvantages. First, it is a surprisingly expensive computational primitive, which incurs memory overhead (Rota Bulò et al., 2018), and significantly increases the time required to evaluate the gradient in some networks (Gitman & Ginsburg, 2017). Second, it introduces a discrepancy between the behaviour of the model during training and at inference time (Summers & Dinneen, 2019; Singh & Shrivastava, 2019).

# Next Lecture: Sequential Processing with RNNs